Magnonic proximity effect in insulating ferromagnetic and antiferromagnetic trilayers

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The design of spin-transport-based devices such as magnon transistors or spin valves will require multilayer systems composed of different magnetic materials with different physical properties. Such layered structures can show various interface effects, one class of which is proximity effects, where a certain physical phenomenon that occurs in one layer leaks into another one. In this work a magnetic proximity effect is studied in trilayers of different ferro- and antiferromagnetic materials within an atomistic spin model. We find the magnetic order in the central layer—with lower critical temperature—is enhanced, even for the case of an antiferromagnet surrounded by ferromagnets. We further characterize this proximity effect via the magnon spectra which are specifically altered, especially for the case of the antiferromagnet in the central layer.

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I. INTRODUCTION

Spintronics is based on the increasing efforts to replace or supplement electronic devices by devices that exploit spin-transport phenomena. Especially, in magnonic devices one would try to avoid charge currents, utilizing magnons—the elementary excitations of a magnet’s ground state—for the transport phenomena. Especially, in magnonic devices one would try to avoid charge currents, utilizing magnons—the elementary excitations of a magnet’s ground state—for the spin transport [1–4]. The great potential of this idea has been demonstrated, for instance, by the magnon transistor [1], which forms a building block for magnon-based logic [2]. A further development in this context is the use of antiferromagnets [5,6] which, for instance, allow one to build a spin-valve structure [7], a multilayer system designed to pass spin waves through only the central antiferromagnetic layer when the two outer ferromagnetic layers are magnetized in the same direction. For antiparallel magnetization, the magnons are blocked.

One type of spin-transport experiment in antiferromagnets is to monochromatically pump spin waves from a ferromagnet via ferromagnetic resonance into an antiferromagnet and detect the signal via the inverse spin-Hall effect in an attached heavy metal layer [8–10]. Alternatively, one can excite thermal spin waves via the spin-Seebeck effect [11–13].

In either method, the setup in total is necessarily a trilayer system, where two layers are magnetically ordered and the two materials may have different ordering temperatures. This raises a question about the temperature dependence of the spin transport, especially when the two critical temperatures are quite different and proximity effects at the interface may play a role. Experiments in such systems exist, including temperature ranges well above the critical temperature of one of the constituents. Surprisingly, even then, there seems to be a spin current above the Néel temperature of the antiferromagnet, as demonstrated, e.g., in [13,14].

For a deeper understanding of the temperature-dependent magnetic behavior of these multilayer systems, it is necessary to study the impact of one layer on the magnetic behavior of the other, a class of effects that is called the magnetic proximity effect [15]. Magnetic proximity effects have been investigated in bilayers composed of an itinerant ferromagnet coupled to a paramagnet, where magnetic moments are induced in the paramagnet [16–18], but they are rather ubiquitous for all kinds of heterostructures and also core-shell nanoparticles [19–23]. Typical signatures of proximity effects are magnetization in a paramagnetic constituent, an enhanced ordering temperature in the material with the lower ordering temperature, increased coercivity, and also the occurrence of an exchange bias effect [15].

Theoretically, proximity effects in bilayers of ferro- and antiferromagnets have been investigated using mean-field techniques [24], Monte Carlo simulations [25], and multiscale techniques [26]. However, these studies neglect the influence of magnons that might pass the interface of a magnetic bilayer as they can be treated only via spin dynamics calculations. It is hence the purpose of this study to investigate the magnetic proximity effect including magnon spectroscopy, adding to a more complete understanding of the temperature-dependent magnetic behavior of bi- and trilayers close to the interface.

The outline of this work is as follows: in Sec. II we describe our model and the two setups which we treat in the following: a magnetic trilayer system built of three ferromagnets in which the central layer has a lower Curie temperature and a corresponding ferromagnet-antiferromagnet-ferromagnet system. We investigate the temperature dependence of the spatially resolved order parameters and susceptibility in Secs. III A and III B and the magnon spectra in Sec. III C. We show that each property can probe this proximity effect, especially in the vicinity of the critical temperature of the central layer, and discover a magnonic contribution to the proximity effect that rests on the different spectra and polarizations of magnons in the different layers.

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critical temperature

satisfying a lower exchange constant

where every magnetic atom at position

close to the critical temperature.

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direction (the three layers are denoted A, B, and C) composed

with the Heisenberg exchange interaction $J_{jk}$ restricted to

nearest neighbors (NN) and uniaxial anisotropy parameterized

by the anisotropy constant $d_z > 0$. The equation of motion is

the Landau-Lifshitz-Gilbert equation [27] with Gilbert damp-

ing $\alpha$ [28,29],

$$\partial_t S_i = -\frac{\gamma}{\mu_s}(1 + \alpha^2)[S_i \times H_I + \alpha S_i \times (S_i \times H_I)]$$

with gyromagnetic ratio $\gamma > 0$ and the effective field

$$H_I = -\frac{\partial H}{\partial S_i} + \xi_i.$$  (3)

The coupling to the heat bath at temperature $k_B T$ [30] leads
to thermal fluctuations in the form of Gaussian white noise $\xi$
satisfying $\langle \xi_i \rangle = 0$ and

$$\langle \xi_i(t)\xi_{k,t}(t') \rangle = \frac{2\mu_s k_BT}{\gamma} \delta_{ik} \delta_{t,t'} (t-t'),$$  (4)

with $\beta, \xi \in \{x, y, z\}$. These stochastic differential equations

are solved numerically using the stochastic Heun algo-

rithm [31]. The simulations are implemented in a highly
efficient code developed in C/C++ and CUDA, running on

graphics processing units. A high degree of optimization is

necessary because of the rather large system size (about $N \approx 10^5$ spins) in combination with very long equilibration times

close to the critical temperature.

The system of interest is a trilayer stacked along the $z$
direction (the three layers are denoted A, B, and C) composed

of spins arranged on a simple cubic lattice with lattice constant
$a$ (see Fig. 1). The Heisenberg coupling constant varies

along the system by a factor of 10; within each layer it takes

isotropic values $J_{jk} = J_A, \pm J_B, J_C$, where $10 J_C = J_A = J_B$.

This choice results in very different critical temperatures. At

the interfaces we choose a coupling of intermediate strength

$J_{jk} = J/k/2$ for lattice sites $j, k$ at the interfaces of layers A and

B as well as layers B and C. There are two different setups: a

purely ferromagnet trilayer (termed FM-FM-FM) with $J_B > 0$

and a layered antiferromagnet (IAFM) sandwiched between

two ferromagnets (denoted FM-IAFM-FM). In the latter case,

the exchange is ferromagnetic, $J_B = J_B > 0$, in the $x-y$

plane and antiferromagnetic along the $z$ direction, $J_{jk} = -J_B < 0$.

The use of the layered antiferromagnet ensures the interfaces

are ideal in either case (parallel alignment of the spins in the

ground state), corresponding to completely uncompensated

interfaces.

As a test case, we choose the following values for

our model parameters: $J_A = J_C = 10$ meV, $J_B = 1$ meV, and

$d_z = 0.1$ meV. Furthermore, $\gamma = \gamma_0$, the free electron’s gyro-

magnetic ratio, and $\mu_s = \mu_B$, Bohr’s magneton.

III. RESULTS

We study the magnetic trilayers outlined above with re-

spect to the magnetic proximity effect in terms of three

aspects: their temperature-dependent order parameter profiles,

their temperature-dependent susceptibility profiles, and their

magnon spectra.

A. Magnetization of a ferromagnetic trilayer

In the first step, we consider the equilibrium order param-

eter profile along the $z$ direction. For a ferromagnet this is the

magnetization, which we resolve monolayerwise along the $z$
direction,

$$\langle m_z(z) \rangle = \frac{1}{N_{xy}} \sum_{r_j} (S_{j,z})$$  (5)

with $N_{xy}$ being the number of spins per monolayer and $\langle \cdots \rangle$
denoting the thermal average, which we calculate in our sim-

ulations as the time average.

Figure 2 depicts this magnetization for the FM-FM-FM

system. Vertical lines indicate the interfaces at $z = 32a$ and

$z = 64a$, separating the central layer B with low exchange

constant $J_B$ from the outer layers A and C with a coupling

constant that is 10 times higher. We tested two very different

values of the damping constants $\alpha = 0.005$ and $\alpha = 0.5$, cor-

responding to the blue and green lines in Fig. 2, respectively.

There is only a small difference visible close to the transition

damping $k_B T_c \approx 1.5 J_B$, where the curve for the smaller
damping is not fully converged to its equilibrium profile. We

conclude that, apart from this small deviation, our results are

equilibrium properties that do not depend on $\alpha$.

The outer layers show a rather stable magnetization with

respect to an increasing temperature due to the higher ex-

change constant, while the central layer undergoes a phase

transition where the magnetization drops to zero. However,

there is a significant difference from a bulk material with

exchange constant $J_B$ (indicated as black dashed lines): while

for low temperatures magnetization values of the bulk and

the central layer of the trilayer are in good agreement, the

magnetization of the central layer remains significantly higher

in the vicinity of the critical temperature. Especially, there is

residual magnetization in the central layer directly at the cri-

tical temperature, the first signature of a magnetic proximity

effect.
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FIG. 2. Magnetization profiles along the $z$ axis in a FM-FM-FM trilayer with coupling ratio $J_B / J_A = 0.1$ for different temperatures. To illustrate the influence of the damping constants we present in the left part our data for $\alpha = 0.005$ (blue) and in the right part only data for $\alpha = 0.5$ (green). For each temperature, the corresponding bulk value of the equilibrium magnetization with coupling constant $J_B$ is shown as a black dashed line for comparison. The corresponding critical temperature is $k_B T_c \approx 1.5$ meV.

Analyzing the magnetization profiles further, we find an enhanced difference from the bulk value closer to the interfaces. The magnetization decays exponentially from the high value of the outer layer to the low value in the middle of the central layer. The corresponding temperature-dependent decay constant which quantifies the penetration depth of the magnetic order is shown in Fig. 3. These data, with a peak at the critical temperature, clearly demonstrate the occurrence of a critical behavior. From these observations we conclude that the magnetic order of the outer layers with the higher coupling constant penetrates into the central layer—a signature of the magnetic proximity effect. The length scale of this proximity effect is the correlation length of the system, a quantity which in our case is only of the order of a few lattice constants, although it should diverge at the critical temperature. Furthermore, its value might be much larger in materials with a larger range of the exchange interaction, beyond nearest neighbors.

In this study, we consider only symmetric trilayers (with identical coupling constants in the right and left layers), although experimentally, asymmetric cases might be more realistic. For a smaller difference in the coupling constants, $J_B / J_A = 0.5$, we observe qualitatively the same proximity effect, but it is weaker. The result is a smaller decay constant, which is then comparable to curves of lower temperatures of the system with $J_B / J_A = 0.1$. In an asymmetric case one would thus expect an asymmetric order parameter profile with a stronger proximity effect (steeper decay) on the side with the lower coupling ratio and a weaker proximity effect on the other side.

The proximity effect can also be observed in the monolayer-dependent magnetic susceptibility,

\[
\chi_{zz}^{FM}(z) = \frac{\mu_0^2 N}{k_B T} \left( \langle m_z(z)M_z \rangle - \langle m_z(z) \rangle \langle M_z \rangle \right)
\]

with $m_z(z)$ being the layer magnetization and $M_z$ being the total magnetization of the trilayer. Note that this statistical definition equals the response-function definition $\chi_{zz}^{FM}(z) = \delta \mu_z m_z(z) / \delta B_z$ for a homogeneous magnetic field $\mathbf{B} = B \mathbf{e}_z$.

As shown in Fig. 4, the critical behavior of the susceptibility in the central layer is suppressed, especially for those monolayers close to the interface (blue line). In the middle of the central layer, there remains a maximum of the susceptibility around the expected critical temperature of the central

FIG. 3. Temperature-dependent penetration depth of the magnetic order, averaged from fitting exponential decays from the left and right interfaces. Error bars are smaller than the symbol sizes.

FIG. 4. Temperature dependence of the monolayerwise susceptibility of the central layer of the FM-FM-FM exchange trilayer. For this calculation a thinner central layer of 11 atomic monolayers is used. The first layer (blue line) is directly at the interface, and the highest number (yellow line) denotes the monolayer in the middle of the central layer.
layer, which is reminiscent of the critical behavior of the corresponding bulk system.

B. Comparison to a FM-IAFM-FM trilayer

In the following, our previous results for a purely ferromagnetic trilayer are compared to the FM-IAFM-FM setup, with an antiferromagnet in the central layer. In the latter case, the order parameter of the central layer B is the Néel vector \( \langle \mathbf{m}_z \rangle \), where \( \mathbf{m}_z \) are the corresponding sublattice magnetizations. In the outer layers A and C, the normal magnetization remains the order parameter as before.

In Fig. 5 the space- and temperature-dependent order parameter profiles of the two trilayers are compared (symbols for the AFM and lines for the FM). Interestingly, they do not show any significant difference. This is due to the fact that equilibrium properties result solely from the Hamiltonian of the system. For the case of a two-sublattice AFM (with sublattices \( S^A, B \)) with only nearest-neighbor interaction there exists a transformation \( J \rightarrow -J, S^B \rightarrow -S^B \) which maps the system to the corresponding ferromagnet. The Hamiltonian is symmetric with respect to this transformation, and hence, the profiles are equal in equilibrium. Note, however, that the argument above is solely classical and quantum corrections may lead to additional effects in which equilibrium properties of FMs and AFMs deviate.

However, even in the central layer, including its proximity effect, we observe the same behavior for the Néel vector of the central AFM in the FM-IAFM-FM trilayer as for the magnetization of the central FM in the FM-FM-FM trilayer: this is quite surprising since it means that a FM can generate even antiferromagnetic order via a proximity effect. Looking at the exchange fields, however, it becomes clear that because of the fully uncompensated interface, the nearest-neighbor exchange interaction of the FM acts on the layered AFM as a field that induces layerwise the same order as in a FM. Nevertheless, as we will show in the following, the magnon spectra in the two investigated trilayers will be affected differently by the proximity effect.

C. Magnon spectra

In a further step, the magnonic spectra are calculated by a Fourier transform of the N spins in time,

\[
\hat{S}_i(\omega) = \frac{1}{\sqrt{2\pi}} \int [S_i,z(t) - i S_i,x(t)] e^{-i \omega t} dt,
\]

where the spin-wave amplitude for our easy-axis magnets is given by the \( x \) and \( y \) components of the spins. For our numerical study, this property is calculated by a fast Fourier transform at discrete instances in time. The frequency- and temperature-dependent amplitude \( I(\omega, T) \) is then calculated as an average over all lattice sites,

\[
I(\omega, T) = \frac{1}{N} \sum_i |\hat{S}_i(\omega)|^2.
\]

This quantity is proportional to the magnon number \( n(\omega, T) = \text{DOS}(\omega, T) f(\omega, T) \), where DOS is the density of states per volume and \( f \) is the magnon distribution function in our classical spin model given by the Rayleigh-Jeans distribution \( f(\omega, T) = \frac{k_B T}{\hbar \omega} \). Consequently, the quantity \( I(\omega, T) \) corresponds to a measurement of the magnon spectra, for instance, by Brillouin light scattering [32].

Figure 6 (left panel) shows the magnon spectra for the central layer of the FM-FM-FM trilayer (black solid lines) compared to a bulk ferromagnet (blue dashed lines) for increasing temperatures (top to bottom). Correspondingly, the right panel depicts the FM-IAFM-FM trilayer case with the same color code. Despite the fact that, as shown before, the two different order parameters follow exactly the same behavior, the spectra differ. The ferromagnet has only a single magnon branch with positive frequencies, whereas the antiferromagnet has two with opposite signs. Furthermore, the dispersion relation and hence the density of states are different [13].

To reveal distinctive features we compare the trilayer spectra to the corresponding bulk spectra. Figure 6 also depicts the numerical bulk spectra (calculated by simulations of a pure bulk system) and, for low temperatures, the theoretical bulk spectra, calculated from the dispersion relations for linear spin-wave theory. These dispersion relations for a three-dimensional simple cubic ferromagnet and layered antiferromagnet respectively read [13,33]

\[
\frac{\mu_s}{\gamma} \omega_{\text{FM}}(k) = 2d_z + 2J \sum_{\theta \in \{x,y,z\}} [1 - \cos(ak_\theta)]
\]

and

\[
\frac{\mu_s}{\gamma} \omega_{\text{AFM}}(k) = \pm \sqrt{4 J_1 + 2d_z - 2J \sum_{\theta \in \{x,y\}} \cos(ak_\theta) - [2J(\cos(dk_\theta) - 1)]^2}
\]

For the layered AFM, one has to include contributions from the antiferromagnetic coupling between the layers (along
the z direction) and ferromagnetic coupling within the layers (x-y direction). From these dispersion relations follow, by integration, the density of states and, multiplied by the Rayleigh-Jeans distribution, the theoretical curves in Fig. 6.

Comparing trilayer systems and the bulk, we find distinct features at high and low frequencies. High frequencies are around the maximal frequencies of the spectra of the central layer. These maximal frequencies can be read from the dispersion relations, and they are $\omega_{\text{FM}}^{\text{max}} \approx 36 \text{ ps}^{-1}$ for the FM and $\omega_{\text{lAFM}}^{\text{max}} \approx 31 \text{ ps}^{-1}$ for the lAFM. Remarkably, there are occupied states above this upper band edge. These are most likely magnons from the outer FM layers, which have a 10 times larger frequency range due to the higher coupling constant. These magnons can penetrate the central layer in the form of evanescent waves. Consequently, even within the allowed frequency regime of the central layer, there are more high-frequency states occupied in the central layer than in the corresponding bulk magnet. In the spectrum of the IAFM this manifests as a peak at $\omega \approx 28 \text{ ps}^{-1}$.

In the low-frequency regime, there are significant deviations from a pure bulk spectrum. Not only is the amplitude here much lower in the central layer, but also the position of the first maximum appears to be located at slightly higher frequencies. For the ferromagnetic trilayer we conclude that the low-frequency magnons can easily leave the central layer. Since ferromagnetic magnons reduce the overall magnetization, the absence of magnons leads to the observation of increased magnetization compared to the bulk value. This is perfectly in accordance with the observation from the order parameter curves (Sec. III A).

For the IAFM the resulting picture is more complicated since only magnons with positive frequency can propagate into the outer FM layers, affecting the spectra asymmetrically even though magnons with negative frequencies can still migrate into the FM as evanescent waves. Indeed, we find a slight asymmetry with respect to positive and negative frequencies. However, this asymmetry is not due to this effect alone since, because of the odd number of monolayers within the IAFM, one of the sublattices is favored and therefore so is one of the branches.

A closer look also reveals further features: the IAFM has a temperature-dependent band gap. The central layer of the trilayer exhibits the same effect, but close to the critical temperature, e.g., for $k_B T = 1.4 \text{ meV}$, the central layer still has a visible band gap, whereas in the bulk it has essentially vanished. Thus, it seems that the outer FM layers effectively

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FIG. 6. Magnon spectra of the central layer (solid black lines) of a FM-FM-FM trilayer (left) and of a FM-lAFM-FM trilayer (right) with coupling ratio $J_B/J_A = 0.1$ at different temperatures, compared to the corresponding bulk spectra (blue dashed lines). For the lowest temperature, a theoretical curve calculated in the limit of low temperatures is added (red dotted line).
cool the central IAFM, stabilizing the magnetic order and therefore weakening the effect of the vanishing band gap at the critical temperature.

IV. CONCLUSION

We investigated and compared magnetic proximity effects in FM-FM-FM and FM-IAFM-FM exchange trilayers numerically within a semiclassical spin model. The advantage of this model is that it allows us to simulate systems with a large number of interacting spins on all relevant timescales even close to the critical temperature. It is, however, an approximation. Besides the difference in the occupation function for the magnons mentioned earlier, a quantum description arguably would result in quantitative differences, mostly via for the magnons mentioned earlier, a quantum description

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small number of interacting spins on all relevant timescales.

In addition we studied the

lower critical temperature. This is true even for a central

with higher critical temperature into the central layer with

the same for both types of trilayers. In addition we studied the

susceptibility profiles, finding suppressed critical behavior in the vicinity of the interface, which is another signature of the magnetic proximity effect.

Most interestingly, magnon spectroscopy uncovered additional features which could be summarized as magnonic proximity effects: in the central layer there is a magnon occupation above the allowed frequency range, and an additional peak close to the upper band edge of the AFM can be observed. These effects are due to high-frequency spin waves from the outer layers with higher exchange coupling, which penetrate the central layer as evanescent modes. Nevertheless, the overall magnon number is lower—a cooling effect due to the influence of the outer layers—and the temperature dependence of the frequency gap is weakened. Most importantly, the magnon spectrum of the central AFM becomes asymmetric since in the outer ferromagnetic layers only one polarization is allowed, an effect that was already exploited in a magnonic spin valve [7]. Our findings thus contribute to the understanding of magnetic equilibrium and spin-transport phenomena in magnetic bi- and trilayers, especially at higher temperatures approaching the critical temperature of one of the layers [13,14].

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