

Appearance of bulk properties in small tungsten oxide clusters

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Contrary to the conventional understanding that atomic clusters usually differ in properties and structure from the bulk constituents of which they are comprised, we show that even a dimer of tungsten oxide $(\text{WO}_3)_2$ possesses bulklike features and the geometry of a small cluster containing only 4 tungsten and 12 oxygen atoms bears the hallmarks of crystalline tungsten oxide, WO_3 . This observation, based on a synergistic approach involving mass distributions under quasisteady state conditions, photoelectron spectroscopy, and first principles molecular orbital theory, not only illustrates the existence of a class of strongly covalent or ionic materials whose embryonic forms are tiny clusters but also lends the possibility that a fundamental understanding of complex processes such as catalytic reactions on surfaces may be achieved on an atomic scale with clusters as model systems.

I. INTRODUCTION

As atoms are successively removed from materials, a point is reached when the properties of the remaining particle no longer resemble those of its bulk.¹⁻⁶ The length scale when this occurs is typically a few nanometers. Atomic clusters belong to this class of materials. It is well known that the geometries and electronic properties of clusters are very different from their bulk. For example, clusters of metallic elements exhibit fivefold symmetry and icosahedric growth,⁷ which is nonexistent in crystals. The building block of silicon clusters is a tricapped trigonal prism (TTP),^{8,9} which is completely different from the bulk diamond structure. Some of the most stable carbon clusters have the famous fullerene geometry¹ while bulk carbon exists in either planar or tetrahedral structures.

These interesting phenomena in nanodimensions raise a fundamental question: What is the critical cluster size at which electronic and geometric structures converge to the bulk properties? Previously, experimental and theoretical studies have been performed to provide an answer to this question. For coinage metals such as Au, Ag, and Cu, it has been observed that the clusters consisting of less than 50–60 atoms exhibit dissimilar electronic structures compared to the respective bulk counterparts, and only for larger clusters, bulklike electronic structures appear.¹⁰ In full shell systems the interaction between the neighboring groups in bulk is relatively weak, resulting in fast convergence to bulk properties. Among others, systems to be named are noble gases, alkali halides, water, etc. In contrast to the pure metal clusters and full shell systems, it is unclear so far, that how fast

the properties of inorganic materials such as oxides converge to the bulk properties as a function of cluster size.

In this paper we demonstrate the existence of a class of materials, characterized by strong covalent or ionic bond, where very small clusters have the similar properties as their bulk, and thus can be used as a prototype system to understand some of the complex issues in surface science at the atomic scale. We concentrate on transition metal oxides, in particular tungsten oxide, WO_3 in the present study. These materials are important for technological applications such as substrates for film growth, catalysis, and electrochromic devices. To shed light on variations of properties of oxide clusters as a function of cluster size, $(\text{WO}_3)_n$ with $n=1-4$ are studied theoretically as well as experimentally. In contrast to the generally accepted view for the metallic clusters that more than 50–60 atoms are required for the onset of the bulk structures, geometric and electronic structures of $(\text{WO}_3)_4$ cluster turned out to be nearly identical to that of the WO_3 bulk crystal, indicating that the electronic properties of oxide clusters can converge to the bulk properties more rapidly than the pure metal clusters.

We show that the interatomic bond lengths, atomic arrangements, relative trends in stabilities, electronic structure, and energy gap between the highest occupied and lowest unoccupied molecular orbitals (this corresponds to the indirect band gap in bulk semiconductors) of $(\text{WO}_3)_4$ cluster are nearly same as those in bulk tungsten oxide. In addition, a systematic study of W_2O_m ($m \leq 6$) clusters shows that the W–W bond is broken when the oxygen content reaches the bulk composition, namely, at $m=6$. The adiabatic electron affinities (AEA) and vertical detachment energies (VDE) of $(\text{WO}_3)_n$ ($n=1-4$) clusters are nearly the same indicating that the bulk bonding characteristics are developed even in the smallest cluster having the bulk composition. These re-

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sults are based upon a combined theoretical and experimental study. The theoretical calculations are carried out using molecular orbital theory and the density functional formalism while the experimental studies involve mass ion intensities and photoelectron spectroscopy.

We begin with a summary of the structure and properties of bulk WO_3 . It is a semiconductor¹¹ with an indirect band gap of 2.62 eV and direct band gap of 3.5 eV. Here the six valence electrons of W originating from its $5d^56s^1$ configuration bond covalently with divalent oxygen. The crystalline structure of WO_3 is complex: The basic building block is that of a simple cubic perovskitelike unit with the tungsten atom occupying the center of an octahedron containing corner and edge sharing oxygen atoms. As a function of temperature and pressure tungsten trioxide crystals exhibit at least five different phases (tetragonal→orthorhombic→monoclinic→triclinic→monoclinic). However, it is commonly accepted that WO_3 has a monoclinic lattice at room temperature. As the tungsten oxide crystal is vaporized,¹² it ejects W_3O_9 clusters indicating that these may be among the most stable structures having molecular architecture. For WO_3 clusters on surfaces, three-membered rings of these octahedral units are observed. The three W atoms are connected via oxygen atoms forming a regular triangle with W-O-W sides. The main question is; do the structural and electronic properties of small tungsten oxide clusters bear any resemblance to their bulk and if so what is the critical size?

Unfortunately, there are no experimental techniques at the current time that can unambiguously yield the atomic structure of clusters. However, this information can be obtained from first principles calculations based on molecular orbital theory. Using density functional formulation we have calculated the equilibrium geometries and electronic properties of $(\text{WO}_3)_n$, $n=1-4$ clusters as well as those of W_2O_m ($m \leq 6$) clusters. The accuracy of these structures are validated by comparing the calculated binding energies, AEA and VDE with experiments involving mass ion intensity distributions and photoelectron spectroscopy. We show that small tungsten oxide clusters indeed exhibit the same structural and electronic properties as its bulk. In Secs. II and III we outline our theoretical and experimental procedures, respectively. The calculated results are compared with experiment in Sec. IV and summarized in Sec. V.

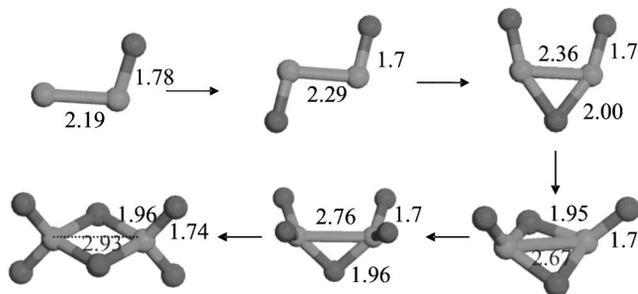


FIG. 1. Evolution of the equilibrium geometries of W_2O_m ($m=1-6$) clusters. The W-W and W-O bond lengths in angstrom are as noted. The lighter shaded atom signifies W and darker atom represents oxygen.

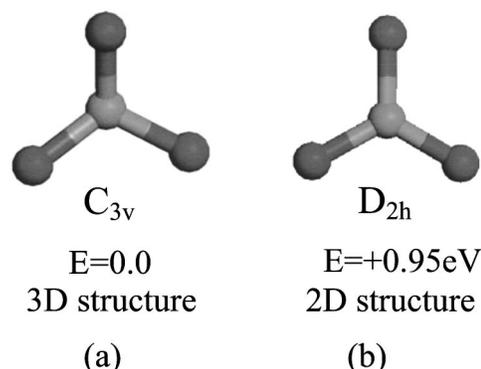


FIG. 2. Structural isomers of anionic WO_3 cluster. The relative energy E is given.

II. THEORY

The theoretical calculations are carried out using the generalized gradient approximation (GGA) for exchange-correlation potential in the density functional theory (DFT). The GGA form prescribed by Becke-Perdew-Wang (commonly referred to as BPW-91) was used. The atomic orbitals were represented by a Gaussian basis. We have used the 6-311G* basis set for oxygen and the Stuttgart relativistic effective core potential basis set for W.¹³ The structures for both neutral and anionic clusters were optimized globally without any symmetry constraint and by starting from various initial configurations. The GAUSSIAN98 code was used in all these calculations.¹⁴

We first investigate the minimum amount of oxygen needed to cleave the W-W bond in a tungsten oxide cluster. The simplest cluster in which to study the effect is W_2O_m , $m=1-6$ since there is only one W-W bond and at $m=6$, the cluster attains the bulk stoichiometric composition. In Fig. 1 we show the equilibrium geometries including some representative bond lengths of W_2O_m ($m=1-6$) clusters. With sequential addition of oxygen, two distinct types of W-O bonds emerge: an internal bond where the O atom is attached to two W atoms and a terminal bond where the O atom is attached to a single W atom. In the bulk, these terminal bonds are absent. We note that the W-O bond lengths remain essentially unchanged as a function of oxygen up-

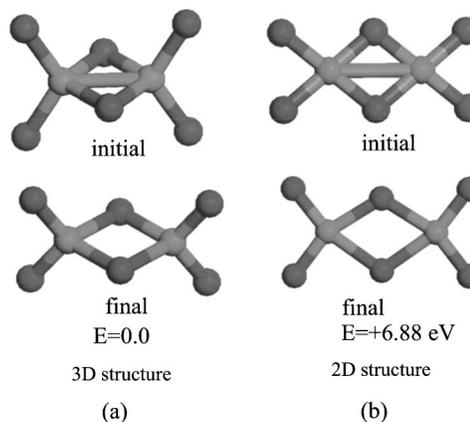


FIG. 3. Structural isomers of anionic $(\text{WO}_3)_2$ cluster.

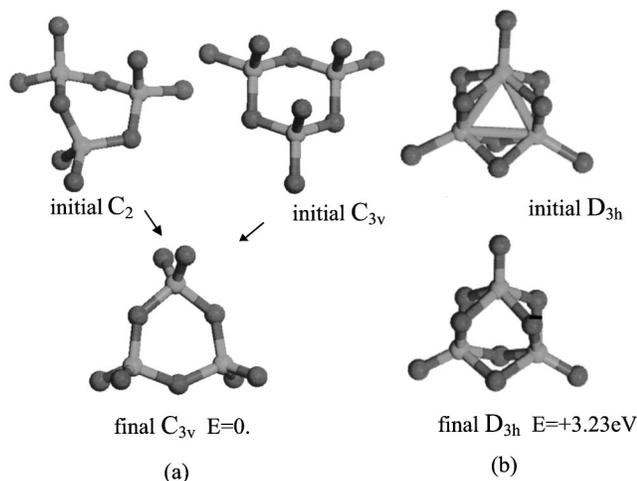


FIG. 4. Structural isomers of anionic $(\text{WO}_3)_3$ cluster.

take. The W–W bond length begins to increase with oxygen content and breaks when the oxygen concentration reaches the bulk limit, namely, W_2O_6 .

Next we discuss the geometries of the ground state and higher energy isomers of anion $(\text{WO}_3)_n$ clusters in Figs. 2–5. For clusters with $n=2, 3, 4$ we have given the initial starting geometries as well as final optimized geometries. In Fig. 2 we show the two isomers of WO_3 cluster. The three-dimensional structure (C_{3v}) is more stable than the two-dimensional structure (D_{2h}) by 0.95 eV. This is also true for $n=2$ (Fig. 3) where the three-dimensional structure is more stable than the two-dimensional structure, and the latter lies 6.88 eV higher in energy than the former. For $n=3$, we considered three initial starting geometries. The two initial geometries with C_2 and C_{3v} symmetries converged to the same structure upon relaxation [Fig. 4(a)]. When starting from the D_{3h} geometry, the resulting optimized structure in Fig. 4(b) lies 3.23 eV higher in energy than the structure in Fig. 4(a). For $n=4$, we found that eight different initial structures con-

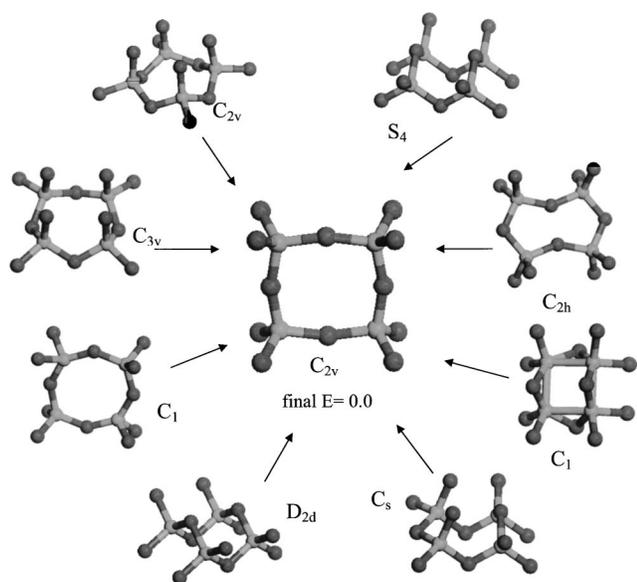


FIG. 5. Initial and final optimized structures of anionic $(\text{WO}_3)_4$ cluster.

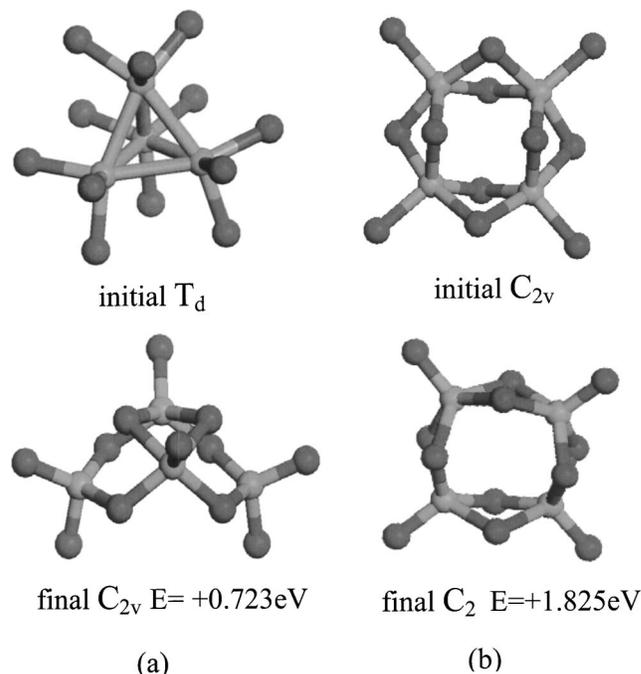


FIG. 6. Geometries of higher energy isomers of anionic $(\text{WO}_3)_4$ cluster. The relative energy E is respective to the ground geometry in Fig. 5.

verged to the same one (Fig. 5) with C_{2v} symmetry. We also found two other higher energy isomers of $(\text{WO}_3)_4$ cluster (see Fig. 6). These lie 0.72 eV and 1.83 eV above the ground state structure in Fig. 5. However, there are some common features shared by the ground state structures studied: (1) The W–W bond is always broken by oxidation. (2) As will be discussed later, the stable structures have large HOMO–LUMO (highest occupied molecular orbital–lowest unoccupied molecular orbital) gaps.

The ground state geometries of the anions of $(\text{WO}_3)_n$ clusters ($n=1-4$) are compared with the corresponding neutrals in Figs. 7–10. Note that the geometries of anion

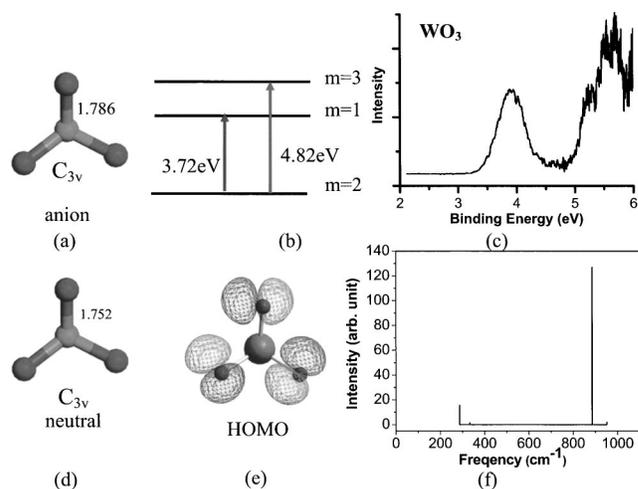


FIG. 7. Theoretical and experimental data on WO_3 cluster. (a) Ground state geometry of the anion. (b) The calculated vertical detachment energies from the anion ground state with spin multiplicity M to the neutral with spin multiplicity $M'=M\pm 1$. (c) Photodetachment spectra. (d) Ground state geometry of the neutral. (e) HOMO. (f) Vibrational spectrum.

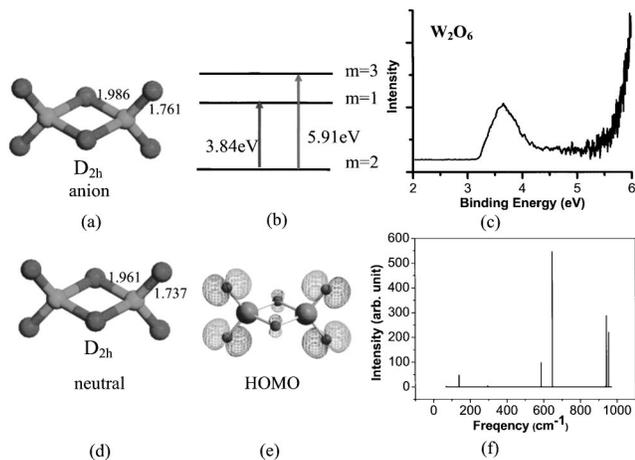


FIG. 8. Theoretical and experimental data on $(\text{WO}_3)_2$ cluster. See Fig. 7 for rest of the legend.

[Figs. 7(a)–10(a)] and neutral [Figs. 7(d)–10(d)] clusters are nearly the same with the anions having marginally enlarged bonds. There are no W–W bonds in any of these clusters. The internal W–O bond is slightly larger than the terminal W–O bond. The frequency calculations for the neutral structures given in Figs. 7(f)–10(f) show that all the frequencies are positive. Thus the structures are dynamically stable. The HOMOs of all the clusters given in Figs. 7(e)–10(e) are contributed by O-2*p* orbitals. The structure of W_3O_9 cluster [Fig. 9(d)], characterized by a ring with three W atoms and three O atoms forming regular triangles, is nearly identical to that observed on surfaces.

To further demonstrate how closely these clusters resemble the bulk structure, we compare the geometry of W_4O_{12} cluster with that cut out from the monoclinic structure of bulk tungsten oxide in Fig. 11. The internal W–O bond length in the W_4O_{12} cluster is 1.92 Å, which is very close to the bulk value of 1.89 Å. Since in the free cluster the terminal W–O bonds are different from the internal bond due to lack of proper coordination, and in bulk WO_3 the W–O bonds form zigzag chains with varying bond distances, we

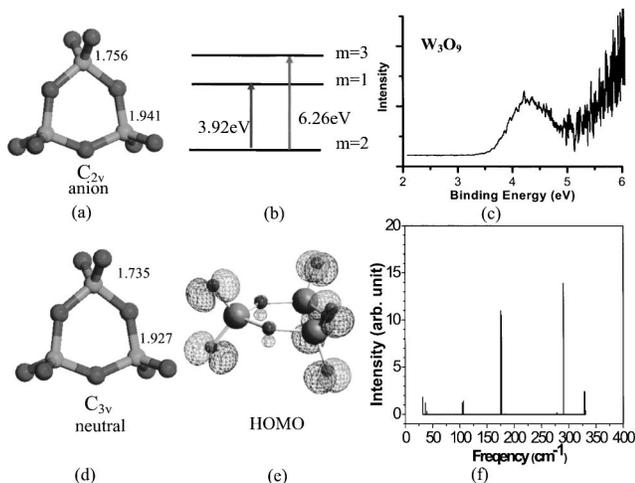


FIG. 9. Theoretical and experimental data on $(\text{WO}_3)_3$ cluster. See Fig. 7 for rest of the legend.

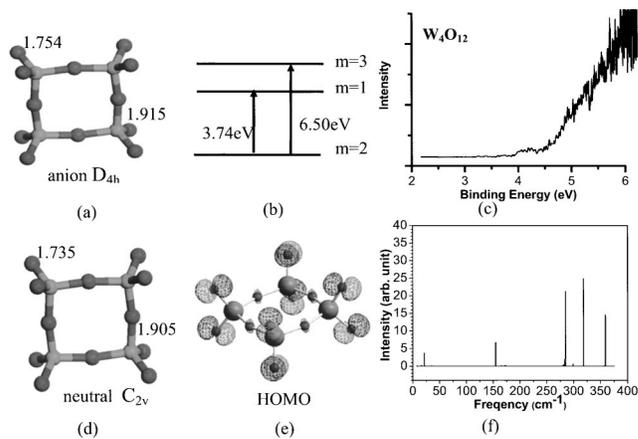


FIG. 10. Theoretical and experimental data on $(\text{WO}_3)_4$ cluster. See Fig. 7 for rest of the legend.

have calculated the average W–O bond length. For a free cluster, it is 1.83 Å while for the monoclinic crystal, the same average yields 1.80 Å. The nearest W–W interatomic distance in the W_4O_{12} cluster is 3.80 Å while it is 3.7 Å in bulk WO_3 . Similarly, the two O–W–O bond angles in W_4O_{12} cluster agree very well with those in the crystalline phase. These comparisons clearly demonstrate that the geometry of the W_4O_{12} cluster is as if it is a fragment of the bulk.

III. EXPERIMENTS

Unfortunately, no experimental technique exists that can verify the structural parameters predicted by theory. However, the accuracy of the theoretically determined structures can be established by comparing the calculated AEA, VDE, HOMO-LUMO gap, and relative stabilities of clusters with experiments involving photoelectron spectra and mass ion intensity distribution. Experimental setup used to obtain photoelectron spectra of tungsten oxide clusters are described in detail elsewhere.¹⁵ W_n anions are produced with a PACIS (pulsed arc cluster ions source) by vaporizing bulk W in the presence of oxygen. The anions are mass selected using a reflectron time-of-flight spectrometer (mass resolution $m/\Delta m = 400$). A mass-selected bunch is irradiated by a UV laser pulse ($h\nu = 4.66$ eV) and the kinetic energies of the detached electrons are measured using a “magnetic bottle”-type time-of-flight electron spectrometer. The energy resolution is about 2% corresponding to 20 meV at a kinetic energy of 1 eV. It is important to mention that binding energies of peaks in photoelectron spectra provide information on tran-

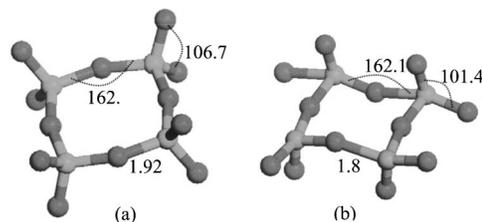


FIG. 11. Comparison between the equilibrium geometry of (a) W_4O_{12} cluster and (b) the corresponding fragment taken from the monoclinic phase of bulk WO_3 .

gen and water are negligibly small in the cluster source, and therefore protonation of the clusters in our experiments is unlikely.^{16,17}

To investigate the extent to which clusters yield the electronic properties of the bulk, we compare in Table I the calculated energy gaps with experiment. We obtain this gap first from the difference in the two calculated transition energies as described before. This can also be obtained directly from the single particle energy levels of the cluster as the difference between the energies of LUMO and HOMO. Note that in DFT these energy levels have no fundamental meaning. Yet, we have given these values in the last column of Table I not only to compare it with those obtained from total energy calculations, but also from experiment. We note that both calculated gaps increase with cluster size. For WO_3 and $(\text{WO}_3)_2$ clusters, the energy gaps calculated using two different procedures agree well with each other and with experiment. For $(\text{WO}_3)_3$ and $(\text{WO}_3)_4$ clusters, the experiments only predict a lower limit and both calculated gaps are consistent with this observation. It is interesting to note that for $(\text{WO}_3)_4$ cluster the gap calculated from transition energies agree with the bulk indirect gap while that calculated from the energy levels agree with the direct gap.

We have studied the relative stabilities of the neutral and anionic clusters by calculating their total energies and computing from it the energy gained in adding a WO_3 unit to a preexisting cluster having the same stoichiometric composition, namely,

$$\Delta E = -E(\text{WO}_3)_n + E(\text{WO}_3)_{n-1} + E(\text{WO})_3,$$

$$\Delta E^- = -E(\text{WO}_3)_n^- + E(\text{WO}_3)_{n-1}^- + E(\text{WO}_3)^-.$$

The relative energies ΔE of the neutral clusters are 4.52 eV, 4.61 eV, and 3.82 eV, respectively, for W_2O_6 , W_3O_9 , and W_4O_{12} . This indicates that formation of neutral W_3O_9 cluster is energetically preferred over that of other clusters. Thus, one would expect that in laser ablation of bulk tungsten oxide, the W_3O_9 units would be ejected. This is, indeed, what has been observed experimentally.¹² The relative energy gains ΔE^- , for the anionic $(\text{WO}_3)_n^-$ clusters are 4.96 eV, 4.59 eV, and 3.94 eV for $n=2, 3$, and 4, respectively. This implies that among anionic clusters, W_2O_6^- should be energetically more favored than $\text{W}_4\text{O}_{12}^-$. This is also consistent with the mass ion intensity distribution in Fig. 12.

V. CONCLUSIONS

In summary, we find that (1) the W–W bonds are broken when the oxygen content of the cluster reaches the bulk limit, namely, in $(\text{WO}_3)_n$ ($n=2,3,4$) clusters. (2) Among the neutral clusters studied, W_3O_9 is the most stable one while W_2O_6^- is more stable than W_2O_9^- and $\text{W}_4\text{O}_{12}^-$. (3) The W–O and W–W bond lengths and O–W–O bond angles of W_4O_{12} cluster are nearly the same as those in the bulk. (4) The

HOMO-LUMO gap calculated using the energy difference between the HOMO and LUMO energy levels agrees well with those obtained from the total energy difference. The “band gap” of W_4O_{12} cluster is very similar to that in the bulk as well. Thus W_4O_{12} is an embryonic form of bulk tungsten oxide. We should point out that previous mass spectroscopy studies of alkali halides have demonstrated that clusters with conspicuously high intensities (magic numbers) can be identified with small fragments of its bulk. Thus, the geometries of these magic clusters may resemble those of their bulk. However, no studies of their electronic properties, as reported here, have been carried out. They will be useful.

This demonstration that a small cluster of a class of materials with strong covalent or ionic bond, behaves same as their bulk has important implications. It is well known that an atomic level understanding of catalysis in bulk materials is difficult due to presence of defects and problems with proper characterization. In atomic clusters this does not arise as mass spectroscopy can identify the precise atomic composition of a cluster and photoelectron spectroscopy can yield accurate energies. Thus once one can identify the size of a cluster that has all the attributes of its bulk, its reaction kinetics can be studied with conventional cluster techniques. It is hoped that such a study can illustrate the reactivity of clusters that has relevance to bulk systems. It is important to point out that for such an understanding, the synergy between theory and experiment is necessary.

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