Field-induced ordering phenomena and non-local elastic compliance in two-dimensional colloidal crystals

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Abstract
Ordering phenomena in colloidal dispersions exposed to external one-dimensional, periodic fields or under confinement are studied systematically by Monte Carlo computer simulations. Such systems are useful models for the study of monolayers on a substrate. We find that the interaction with a substrate potential completely changes the miscibility of a binary, hard disc mixture at low external field amplitudes. The underlying ordering mechanisms leading to this laser-induced de-mixing differ, depending on which components interact with the substrate potential. Generic effects of confinement on crystalline order in two dimensions are studied in a model system of point particles interacting via a potential $\propto r^{-12}$. The state of the system (a strip of width $D$) depends very sensitively on the precise boundary conditions at the two confining walls. Commensurate, corrugated boundary conditions enhance both orientational order and positional order. In contrast, smooth repulsive boundaries enhance only the orientational order and destroy positional (quasi-)long range order. As external fields have a strong impact on the elastic behaviour of colloidal crystals there is a need to analyse the elastic response in such systems for the field-free case first. To this aim we study the strain–strain correlation functions in a two-dimensional crystal formed by super-paramagnetic colloids, as monitored by standard video microscopy.

Minimization trends in physics and technology have caused a lot of interest lately in monolayers and their interactions with a substrate. The assembly of nanoparticles into spatially extended regular structures is the first step towards a new generation of materials and devices. Colloidal dispersions in external fields or under confinement are valuable model systems for the systematic study of such settings, as they are experimentally directly accessible via laser scanning microscopy. In addition their effective interactions can be tailored to specific needs by various means. In two dimensions (2d) such systems are often used for the study of monolayers on a substrate. Monodisperse 2d colloidal systems with a substrate potential have been studied extensively in experiments [1, 2], computer simulations [3–8] and theory [9–11] over the last few decades. Re-entrant phase transition scenarios like laser-induced freezing (LIF) and laser-induced melting (LIM) have been observed in such settings. We address the question of how the addition of another length scale to such a system influences the intricate competition between adsorbate–adsorbate interaction and adsorbate–substrate interaction by studying a binary 50% mixture under the influence of a one-dimensional (1d) spatially...
periodic substrate potential in section 1. Another way to influence the order in 2d systems is by geometric confinement, which will be important in the development of novel devices. Depending on the precise settings confinement can either enhance or destroy ordered structures. In section 2 we deal with the generic effects of geometric confinement by analysing a system of model colloids confined within a quasi-one-dimensional strip between two parallel boundaries using Monte Carlo simulations. External fields not only influence the ordering, but also the elastic properties of the colloidal dispersions. These are also an important aspect in the search for novel material in soft matter physics. In order to gain a deeper understanding of the elastic response in such systems, we study the strain–strain correlation functions of a monodisperse, 2d, triangular colloidal crystal in section 3.

1. A binary mixture in a 1d spatially periodic potential

The intricate competition between adsorbate–adsorbate and adsorbate–substrate interactions is the origin of a complex phase behaviour observed in monodisperse monolayers on a substrate. Re-entrant phase transitions like LIF and LIM are known to occur in various systems (e.g. [2, 4, 5]). In this section we show that adding another competing length scale to such a set-up generates novel interesting phenomena [12–14]. We will concentrate in this section on a regime with low external potential amplitudes $V_0/(k_B T) \lesssim 1.5$. Following the approaches in the studies of monodisperse systems, we use an external potential given by

$$V(\vec{r}) = V_0 \sin \left( \frac{\vec{K} \cdot \vec{r}}{a} \right), \quad \vec{K} = \frac{4\pi}{a} (1, 0). \quad (1)$$

Here $a$ is the lattice parameter of the $S_1(AB)$ lattice [15], which provides the densest packing for the studied equimolar binary mixture (diameter ratio $\sigma_B/\sigma_A = 0.414$). All lengths are measured in units of $\sigma_A$, therefore the dimensionless number density $\varrho = \frac{N}{\sigma_A^2}$. A wavelength $\lambda = 2\pi/|\vec{K}|$, commensurate to the lattice planes of this crystalline structure, is chosen for the periodicity of the substrate potential. The situation is schematically illustrated in figure 1. The colloidal particles are modelled by hard discs. Monte Carlo simulations in the $NVT$ ensemble with periodic boundary conditions are employed. In order to facilitate equilibration we use a cluster move [16] and additional non-local moves, in which particle displacements, which are integer multiples of the potential wavelength, are attempted.

Even in the field-free case binary mixtures in 2d are known to show interesting phenomena. As has been recently observed experimentally [17], introducing small particles into a system of large particles breaks the spanning network of large particles. This results in a competition between free volume and configurational entropy and leads to clustering [18] and structural crossover [17, 19]. Nevertheless in a purely repulsive system the effect is too weak to drive phase separation. In general one needs to distinguish the following three cases:

(a) only the smaller component interacts with the external field;
(b) both components interact with the external field;
(c) only the larger component interacts with the external field.

For a detailed discussion of the phase behaviour for case (a), when only the smaller component interacts with the external potential, see [12]. In summary we find for this case that at intermediate to high external field amplitudes the coupling to the external field induces a coexistence of a $S_1(AB)$ crystal with an equimolar fluid. This regime is followed by a fissuring regime for higher dimensionless number densities $\varrho$, in which the larger component forms a square lattice. This lattice structure has a tendency to form fissures parallel to the modulation direction of the external field, in which the smaller components can accumulate.

For low potential amplitudes $V_0$ we find a novel phenomenon. In contrast to the monodisperse LIF scenario a laser-induced de-mixing sets in for all three cases. We observe a coexistence of a small component enriched fluid with a droplet of a monodisperse crystalline structure formed by the larger component. This is visualized in figure 2, where overlays of all configurations of the simulation (corrected for the centre-of-mass movement) are shown. The positions of the larger component are denoted by black (online: blue) points, while those of the smaller component are plotted in grey (online: orange). The data was taken at a number density $\varrho = 1.71$. A heuristic argument by Buhot et al [20] yields a diameter ratio of $\sigma_B/\sigma_A = 1/100$ as the upper limit for possible phase separation in binary hard disc mixtures. Nevertheless, exposing an equimolar binary mixture with diameter ratio $\sigma_B/\sigma_A = 0.414$ to an external field interferes with the competition of free volume and configurational entropy in a controlled way by introducing the constraint of energy minimization. Phase separation is induced. Subfigure 2(c) shows case (c) at $V_0/k_B T = 0.5$. The formation of the monodisperse lattice structure is induced directly by the interaction with the external field in this case. The resulting structure is aligned in its orientation with the minima of the potential. As the periodicity of the

Figure 1. Schematic illustration of the external, 1d spatially periodic substrate potential $V(\vec{r})$ and the $S_1(AB)$ lattice structure relative to it. The larger component of the binary mixture is displayed in black (online: blue), the smaller in grey (online: orange). $a$ is the lattice parameter of the $S_1(AB)$ lattice, while $V_0$ is the amplitude of the external potential.
external potential is not commensurate with a monodisperse triangular lattice of the larger component, a rhombic structure forms. In contrast at $V_0/k_B T = 0.6$ the monodisperse crystalline structure observed for case (a), when only the smaller component interacts with the external field, is a triangular lattice. This difference can be explained by the ordering mechanism, which leads to the de-mixing in this case. As the smaller component tries to optimize its alignment with the potential minima it forms chains along the $y$ direction. This chain formation has a lower number density than the fluid mixture. Under the constraint of a fixed overall number density, the larger component is thus indirectly induced to form a dense packing, i.e. a triangular lattice structure in order to facilitate the energy minimization of the smaller components. For case (b), when both components interact with the substrate potential, both types of ordering mechanisms are at work. Therefore only at even lower potential amplitudes do we observe a pure de-mixing, as shown in subfigure 2(b). The de-mixing is followed by a regime in which the competition of the ordering mechanisms leads to a domain growth of rhombic monodisperse and square lattice bi-disperse areas.

In conclusion, we have shown via Monte Carlo simulations that the miscibility of a binary hard disc mixture can be tuned in a controlled way by exposing the mixture to a one-dimensional spatially periodic potential. Weak external fields induce a phase separation into an ordered monodisperse phase of the larger component and a disordered fluid phase.

2. Confinement: a quasi-one-dimensional system

In this section we analyse the nature of the ordered phase for a model of colloidal particles confined within a quasi-one-dimensional (q-1d) strip between two parallel boundaries, or walls, separated a distance $D$ in two dimensions (2d).\(^4\) Using Monte Carlo simulations we find [22, 23] that at densities typical of the bulk 2d triangular solid the order in the q-1d strip is determined by the nature of the boundaries. While for a suitably corrugated boundary potential order is enhanced, for a uniformly repulsive smooth boundary potential only ordering normal to the walls is enhanced (‘layering’); parallel to the wall it is destroyed.

Ordering in strips and half-planes have been studied [24–28, 21, 29] in the past for spin systems primarily in the context of surface critical phenomena where both suppression or enhancement of order near free boundaries have been observed.

Studies of the nature of ordering for quasi-1d strips have been done for Wigner crystals [30], repulsive magnetorheological (MR) colloids [31, 32] and for colloids between walls in non-equilibrium situations [33], for instance. The former system is relevant, for example, for electrons on the surface of liquid helium that is confined in a quasi-1d channel, where unusual ordering phenomena were found [34], and for confined dusty plasmas [35]. MR colloids under confinement are of interest for microfluidic applications, see [31, 32] for references and discussions of further related systems. Unusual mechanical behaviour of a related system has also been reported [36], and in [31] it was noted that the properties of the confined system approach those of the unbounded system surprisingly slowly as the channel width is increased. Early experiments on a model hard disc system [37] also showed unconventional behaviour. Clearly, the understanding of confined 2d crystals is far from being complete, and it is the purpose of the present work to contribute to a resolution of these puzzles by combining simulations of a generic model with a suitable theoretical analysis.

For finite $D$, the system is quasi-one-dimensional, and hence one might argue that long range order (LRO) is destroyed, for systems with short range forces [24]. Indeed, a 1d harmonic crystal displays a fluid-like structure factor [38] and this accounts well for real quasi-1d chain compounds such as Hg$_{3−\delta}$AsF$_6$ (where $\delta \ll 1$) [39]. However, for confined colloidal crystals the situation should be more subtle, since the confinement between hard repulsive boundaries reduces fluctuations in the direction normal to the boundaries, causing a pronounced ‘layering effect’. Ordering is also strongly influenced by the boundaries, for example it is known that a boundary corrugation potential [24, 40] enhances the order parallel to the boundaries.

The interaction among colloidal particles may be conveniently parametrized by $V(r) = \epsilon (r/r_0)^n$ where the exponent may vary from $n = \infty$ in the case of hard sphere colloids [41–44] to $n = 3$ for super-paramagnetic [45, 46] dipolar colloids. We have chosen a potential with $n = 12$.

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\(^4\) For colloidal crystals in $d = 3$ confined in narrow slit pores, see [21].
and with a cutoff at $r_c = 5\sigma$, at a temperature $k_B T/\epsilon = 1$ (where $k_B$ is the Boltzmann constant) and density (choosing units such that $\sigma = 1$) $\rho = 1.05$. This choice retains the advantage of a smooth potential which is also sufficiently short ranged for computational convenience. Further, we believe that the phenomena reported here are independent of the detailed nature of the potential. At the chosen density melting in the bulk occurs for $k_B T/\epsilon \approx 1.35$ in this model [47]. We choose two types of wall potentials, with walls oriented parallel to lattice axes of the triangular lattice: (i) planar walls $V_{\text{wall}}(r) = \epsilon_{\text{wall}}(\sigma/|x - x_{\text{wall}}|)^{10}$ for a particle at position $\mathbf{r}$, where the $x$ direction is chosen perpendicular to the boundaries, and the positions $x_{\text{wall}}$ of the two walls are a distance $D$ apart that is an integer multiple of the distance $a\sqrt{3}/2$, $a$ being the lattice spacing of an ideal triangular lattice compatible with the chosen density. The strength of this potential is typically $\epsilon_{\text{wall}} = 0.0005k_B T$ (also much stronger wall potentials were tested). (ii) Structured walls causing a periodic corrugation of the potential were created by choosing two rows of particles fixed in the positions of this ideal triangular lattice, and these particles interact with the mobile particles with the same potential $V(r)$ as specified above. Summing up these potentials due to the fixed particles defines the corrugation potential $V_{\text{corr}}(r)$ (structured walls) of such structured boundaries. A sketch of the configurations in front of the two wall types is given in figure 3.

We use standard Monte Carlo methods [48], where single particles are selected at random to attempt a small random displacement in a square of linear dimension $\kappa = 0.206$ centred at the old position of the particle. Typical runs were performed for systems containing between $D \times L = 20 \times 20$ and $D \times L = 60 \times 60$ particles, carrying out $10^4$ Monte Carlo steps (MCS) per particle in each run. In the direction parallel to the walls, periodic boundary conditions are used. For the sake of comparison, runs for ‘bulk’ systems (with no walls and periodic boundary conditions in both directions) were also done. Some runs were also made for a strongly elongated geometry ($D \times L = 20 \times 500$) to probe the behaviour of displacement correlations at large length scales.

Both types of boundaries enhance the order in the $x$ direction near the walls. This enhancement of order in the direction normal to the walls is even more pronounced (and of larger range) when we approach the transition to the fluid phase [22, 23]. While in the bulk the well-defined orientational LRO and nonzero shear modulus of the 2d crystal have both disappeared in the fluid, some wall-induced orientational LRO persists in the thin strip [22, 23].

In contrast, in the direction parallel to the boundaries the behaviour in the two cases differs dramatically: for the structured boundary, the structure factor $S(q)$ exhibits the sharp Bragg peaks expected for a crystal5 (figure 4(a)). For the structureless repulsive boundary, a typical fluid-like structure factor results, which is almost in quantitative agreement with

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5 Note that for orderings commensurate with the corrugation potential the statement of Mermin [49] that crystals in $d = 2$ have only orientational LRO and no positional LRO does not apply here. This situation is reminiscent of the behaviour of thin films adsorbed on substrates where true LRO commensurate with the substrate corrugation potential can occur [40].
rather has $C_{33}(\text{bulk}) \sim 2C_{33}(n)$, which implies a vanishing shear modulus. The elastic constants could be determined directly from an analysis of the configurations of the particles applying the method of Sengupta et al [51, 52]. Particularly remarkably the increase of strip thickness (or number $n$ of rows in the strip, respectively) does not cause any visible approach to bulk behaviour. The question how, for the elastic constants, the thermodynamic limit is approached is intriguing. The planar boundary provides an elastic distortion of long range [53] to the crystal, and our results imply that in $d = 2$ this distortion disturbs the positional LRO.

This lack of positional LRO may be understood from a calculation of the displacement correlation function $B(y) = \langle |u_y(y) - u_y(0)|^2 \rangle$, where $u_y$ is the displacement away from a reference lattice in the direction parallel to the walls and the angular brackets signify ensemble averaging. Using a harmonic elastic Hamiltonian for the strip geometry, this may be written as

$$B(y) = 2 \sum_{q_y \text{ even}} \sum_{q_x = 2n_x} \langle |u_y^2| \rangle \left[ 1 - \cos(q_y y) \right].$$

$$\langle |u_y^2| \rangle = \frac{k_B T}{(\lambda + 2\mu - P)q^2 \hat{q}_y^2} + \frac{k_B T}{(\mu - P)q^2} (1 - \hat{q}_y^2).$$

(2)

Here, $n_x$ and $n_y$ are integers, $\hat{q}_y = q_y/q$ and the Lamé coefficients $\lambda$ and $\mu$ are those of a bulk soft disc solid at the same density, while $P$ is the overall (nonzero) hydrostatic pressure [51, 52]. The result of this calculation is shown in figures 6(a) and (b). We observe a crossover from the logarithmic increase of mean-square displacements $B(y) \propto \ln y$ with distance $y$ (characteristic for 2d solids) to a linear increase (1d systems [38]) at a distance of order $D \ln(D/a)$ [22, 23] which is cut off by the periodic boundary conditions for small systems. The direct evaluation of $B(y)$ for the soft disc system with periodic boundary conditions is also shown in figure 6(a) and agrees well with the harmonic calculation within the error bars of the former. The corresponding calculation with planar walls shows an enhancement of the displacement fluctuations parallel to the walls for the lattice layer closest to the wall figure 6(b).
This behaviour is quite similar to that seen in the XY model [29] with free boundary conditions. Fluctuations of the displacement perpendicular to the walls are, of course, suppressed.

In summary, we have demonstrated that confinement of 2d colloidal crystals by external boundaries has subtle effects on their structure. The least disturbance is caused by ‘structured boundaries’ (rows frozen in the perfect crystalline order). For planar boundaries, however, the positional LRO is destroyed, even for very thick strips. This phenomenon is not a standard surface-induced melting, however, since a very strongly layered structure (reminiscent of a smectic) is maintained. Just as the 2d XY model below $T_c$ is in a critical state (power-law decay of correlations implies infinite correlation length), the 2d crystal is in a similar critical state too, and therefore sensitive to boundary conditions over very large distances. We believe that these effects should be easily observable in experiments involving confined colloids.

### 3. Strain–strain correlation functions in a colloidal crystal

The knowledge of the elastic properties of these model systems is important in the search for novel materials in soft matter physics. Strain–strain correlation functions give access to more detailed information on the elastic behaviour of the system, as they describe the non-local mechanical response of a soft solid in two dimensions. Such non-local elastic effects are important for situations where strain gradients are large [54] or set-ups for which the relevant linear length scales of the solid are of the order of the coarse graining length scale of classical elasticity theory. Both of these criteria are satisfied in colloidal solids under usual experimental conditions [55]. We analyse the fluctuations of particle coordinates in order to gain knowledge of the elastic properties of the colloidal crystal. Recently there has been a lot of interest in obtaining the elastic moduli of soft solids [56, 57] from fluctuations of particle coordinates [51, 46, 58–60]. These methods have several advantages. Particle configurations of the colloidal crystal can be obtained by standard video microscopy [57] and for the calculation of the elastic moduli no external forces need to be applied, which may change the very properties that are being measured.

The description of a 2d crystal via a formulation of the elastic free energy as a functional of the strains opens up a way to derive analytic expressions for the strain–strain correlation functions $G_{ij}(\vec{x}, \vec{y})$ in the crystal. These are connected to the non-local compliance $\chi_{ij}$, which is defined as the strain $\varepsilon_{ij}(\vec{x})$ produced at position $\vec{x}$ due to a stress $\sigma_{ij}(\vec{x})$ at position $\vec{x}$ by $\chi_{ij} = (k_B T)^{-1} G_{ij}$. The starting point is the dimensionless elastic free energy functional

$$F = \frac{k_B T}{a^2} 2 \int d\vec{r} \sum_{i=1}^{3} \left[ a_i e_i^2 + c_i (\nabla e_i)^2 + c_i' (\nabla^2 e_i)^2 \right]. \tag{3}$$

Energy and length scales are set by $k_B T$ and the lattice parameter of the triangular lattice $a = (2/(\sqrt{3} \sqrt{3}))^{1/2}$, respectively. The coefficients $a_i (i = 1–3)$ are the elastic constants and $c_i$ and $c_i'$ set the length scales over which strain fluctuations decay. The functional is written in a harmonic form of those linear combinations of the strains, which are relevant for a solid in two dimensions: $e_1 = \partial u_x/\partial x + \partial u_y/\partial y$ (volume), $e_2 = \partial u_x/\partial x - \partial u_y/\partial y$ (deviatoric) and $e_3 = (\partial u_x/\partial y + \partial u_y/\partial x)/2$ (shear). Care is taken that the colloidal crystal reaches a thermodynamic equilibrium before the measurement. Therefore we can assume $\partial \sigma_{ij}/\partial x_j = 0$, which ensures the mechanical stability of the crystal. Within classical, linear elasticity theory the strains must fulfil St. Venant’s compatibility condition $V \times (\nabla \times e)^T = 0$, if there is to be a unique relation between the displacement field and the corresponding strains. Under these constraints only one strain variable is independent and the elastic free
energy functional can be written in terms of this strain variable in a harmonic form. Switching to a formulation in Fourier space, the equipartition theorem can be used to extract the analytic prediction for the corresponding strain–strain correlation function. For a more detailed presentation of the derivation see [61]. As an example we present a study of the shear fluctuations in a colloidal crystal. The analysed volume $V$ is embedded in a larger colloidal crystal; therefore these fluctuations can be studied by evaluating the fluctuations in $\theta = (\partial u_x / \partial x - \partial u_y / \partial y)$. The analytic prediction for the strain–strain correlation function corresponding to this strain variable is given by

$$G_{2020}(k \neq 0)^{-1} = (a_3 + c_3 k^2 + c'_3 k^4)$$

$$+ \sum_{j=1}^{2} (a_j + c_j k^2 + c'_j k^4)(\tilde{Q}_{j3}(\mathbf{k}))^2(\tilde{Q}_{30}(\mathbf{k}))^2;$$

$$G_{2020}(0)^{-1} = a_3/4.$$

Coupled strain variables are related to the independent strain variable via kernels $\tilde{Q}_{ij}$: $\tilde{e}_i = \tilde{Q}_{ij} \tilde{e}_j$. The kernels relevant for the analytic formulation of $G_{2020}$ are

$$\tilde{Q}_{20} = \frac{1}{2} \left( k^4_x - k^4_y / \left( k^2_x - k^2_y \right)^2 + k^2_x k^2_y \right) \left( 4a_1 + 2a_3 \right) / \left( a_1 + a_2 \right)$$

$$\tilde{Q}_{13} = (4a_2 - 2a_3) / \left( a_1 + a_2 \right) / \left( k_x k_y / \left( k^2 \right) \right)$$

$$\tilde{Q}_{23} = -(a_1 + 2a_3) / \left( a_1 + a_2 \right) / \left( k_x k_y / \left( k^2 - k^2_y \right) \right).$$

Experimental data was obtained with an experimental set-up, which is an improved version of [46]. Spherical colloids (diameter $d = 4.5 \mu m$) are confined by gravity to a water/air interface formed by a hanging water droplet. The field of view was $835 \times 620 \mu m^2$ containing typically $2 \times 10^3$ colloids, whereas the whole system has a size of $50 \text{mm}^2$ and contains about $3 \times 10^5$ colloids. The analysed volume $V$ contains 840 particles arranged in a triangular lattice. The particles are super-paramagnetic. Therefore a magnetic field $\mathbf{H}$ applied perpendicular to the water/air interface induces a magnetic moment $\mathbf{M} = \chi_M \mathbf{H}$ in each particle. This leads to a repulsive (inverse cubic) dipole–dipole pair interaction with the dimensionless interaction strength given by $\Gamma$, the ratio of potential to thermal energy. Thus $\Gamma$ can be interpreted as an inverse temperature. Coordinates of all particles at each time step are analysed and the trajectories are recorded for 2–3 h. The data was taken in the solid phase, as can be seen in figure 7, where an overlay of all configurations obtained during the measurement shows a triangular lattice structure. The boxed section is the analysed volume $V$. Strains are calculated with respect to the average particle positions, as reference (corrected for centre-of-mass motion and rotations of the system) using the scheme of Falk and Langer [62]. Figure 8(a) shows the measured strain–strain correlation function $G_{2020}$ in real space. Cuts in $k$ space along the $k_x$ or $k_y$ direction of $G_{2020}$ are fitted in order to obtain the shear modulus $\mu = 58.6 \text{mPa}$. A different approach [46] to measure the shear modulus of the colloidal crystal is to obtain the probability distribution of the strain variable $2 \theta$. An example of $P(2 \theta)$ measured over boxes of volume $V_B = 16.0a^2$ is shown in figure 9(b). The mean-square fluctuations in $2 \theta$ are obtained by fitting a normal distribution to the data and extracting its standard deviation. They are related to the shear modulus of the solid via $\mu = (V(\langle(2 \theta)\rangle^2))^{-1}$. The shear modulus obtained according
includes the defect pairs themselves. antidislocation pairs, as the chosen reference lattice already vector) contribution to the displacement from dislocation–show in figure 8(b) does not include the singular (Burger’s function may serve as a benchmark for characterizing soft crystals as it is sensitive to the presence of defect pairs.

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