Constraints on the distribution and energetics of fast radio bursts using cosmological hydrodynamic simulations

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ABSTRACT
We present constraints on the origins of fast radio bursts (FRBs) using large cosmological simulations. We calculate contributions to FRB dispersion measures (DMs) from the Milky Way, from the Local Universe, from cosmological large-scale structure, and from potential FRB host galaxies, and then compare these simulations to the DMs of observed FRBs. We find that the Milky Way contribution has previously been underestimated by a factor of ∼2, and that the foreground-subtracted DMs are consistent with a cosmological origin, corresponding to a source population observable to a maximum redshift z ∼ 0.6–0.9. We consider models for the spatial distribution of FRBs in which they are randomly distributed in the Universe, track the star formation rate of their host galaxies, track total stellar mass, or require a central supermassive black hole. Current data do not discriminate between these possibilities, but the predicted DM distributions for different models will differ considerably once we begin detecting FRBs at higher DMs and higher redshifts. We additionally consider the distribution of FRB fluences, and show that the observations are consistent with FRBs being standard candles, each burst producing the same radiated isotropic energy. The data imply a constant isotropic burst energy of ∼7 × 10^{40} erg if FRBs are embedded in host galaxies, or ∼9 × 10^{40} erg if FRBs are randomly distributed. These energies are 10–100 times larger than had previously been inferred. Within the constraints of the available small sample of data, our analysis favours FRB mechanisms for which the isotropic radiated energy has a narrow distribution in excess of 10^{40} erg.

Key words: hydrodynamics – methods: numerical – intergalactic medium – large-scale structure of Universe – radio continuum: general.

1 INTRODUCTION
Fast radio bursts (FRBs) are a newly identified and as-yet-unexplained class of transient objects (Lorimer et al. 2007; Thornton et al. 2013; Kulkarni et al. 2014). The 10 known FRBs currently in the literature are characterized by short (∼1 ms), bright (∼1 Jansky) bursts of radio emission; none have been seen to repeat, and all but two occurred at high Galactic latitude, |b| > 20°. The implied all-sky event rate is enormous, around 10 000 per day (Thornton et al. 2013).

The radio signals from FRBs experience a frequency-dependent dispersion delay as they propagate through ionized gas, just as is routinely seen for radio pulsars. However, for most observed FRBs, the very high dispersion measures (DMs), in the range 400–1100 pc cm^{-3}, are more than an order of magnitude larger than the DM contribution expected from the interstellar medium (ISM) of the Milky Way in these directions. The currently favoured interpretation is that the observed DMs seen for FRBs correspond primarily to free electrons in the intergalactic medium (IGM) along the line of sight (Dennison 2014; Luan & Goldreich 2014), with an additional but presumed small contribution from any host galaxy (Thornton et al. 2013). Simple assumptions about the density of the IGM then immediately imply that FRBs are at cosmological distances, corresponding to redshifts in the range 0.5–1 (Thornton et al. 2013).
# 2 Observations of FRBs

The observational data we consider are the 10 published FRBs as listed in Table 1, for each of which we provide Galactic coordinates, the observed value of $\text{DM}$, peak flux and fluence, and the central observing frequency at which the FRB was detected.

## 3 Foreground DM

The $\text{DM}$s observed for FRBs as listed in Table 1 must consist of several contributions, corresponding to the various astrophysical structures through which the radio signal has traversed. For our purposes, the $\text{DM}$ contributions both from the Milky Way Galaxy and from local large-scale structure are considered to be foregrounds, which we would like to remove to isolate the cosmological signal. Some of the foreground components are difficult to obtain from direct observations, and we use cosmological simulations to estimate the contribution of these components. We define the observed dispersion measure, $\text{DM}_{\text{obs}}$, as

$$\text{DM}_{\text{obs}} = \text{DM}_{\text{ISM}} + \text{DM}_{\text{halo}} + \text{DM}_{\text{LSS}} + \text{DM}_{\text{host}}$$

(1)

where $\text{DM}_{\text{ISM}}$ is the contribution from the Milky Way disc and spiral arms, $\text{DM}_{\text{halo}}$ is that from the Galactic halo, $\text{DM}_{\text{LSS}}$ is that from the Local Universe, $\text{DM}_{\text{host}}$ is any contribution from any host galaxy or other immediate environment of the FRB. We define

$$\text{DM}_{\text{cosmo}} = \text{DM}_{\text{LSS}} + \text{DM}_{\text{host}}$$

(2)

as the signal to be estimated from cosmological hydrodynamic simulations, with the remaining terms on the right-hand side of equation (1) representing the foreground signal that must be accounted for in order to derive $\text{DM}_{\text{cosmo}}$ from $\text{DM}_{\text{obs}}$. Fig. 1 shows full sky maps of the DM contributions of the various foreground components, as discussed in more detail in Sections 3.1–3.3.

### 3.1 The Galaxy Model

We calculate the foreground contribution from the Milky Way’s disc and spiral arms using the widely used NE2001 distribution (Cordes & Lazio 2002, 2003). This three-dimensional model of thermal
The values of $D_{\text{ISM}}$ calculated in Section 3.1 above only account for the foreground DM originating in the disc structure of the Milky Way; the NE2001 model lacks the contribution of a virialized dark matter halo with a hot gaseous atmosphere. As per equation (1), we must also consider the free-electron contribution of the surrounding Galactic halo, which we model using numerical simulations. To estimate $D_{\text{halo}}$, we use a cosmological simulation of a representative Milky Way-type galactic halo including hot thermal electrons. We use the existing simulations of Beck et al. (2013) to estimate the contribution to the DM. Fig. 1 shows an all-sky projection of the corresponding DM distribution.

The simulation of Beck et al. (2013) is based on initial conditions which were originally introduced by Stoehr et al. (2002). Briefly, the simulation is based on a large cosmological box with initial fluctuations of power spectrum index $n = 1$ and a fluctuation amplitude $\sigma_8 = 0.9$, in which a Milky Way-like dark matter halo is identified. We use the fully magneto-hydrodynamic simulation labelled GA2, which contains 1055 083 dark matter particles inside the virial radius at present redshift. The halo is comparable in mass with a numerical subgrid model for the self-consistent seeding of the stellar components by including multiphase gas particles, which follow the prescriptions of radiative cooling, supernova feedback, and star formation based on the work of Springel & Hernquist (2003) but without galactic winds. Furthermore, the simulation is extended with magnetic fields following the implementation of Dolag &斯塔斯金 (2009). In addition, Beck et al. (2013) further extend the original magneto-hydrodynamic calculation of Beck et al. (2012) with a numerical subgrid model for the self-consistent seeding of magnetic fields by supernova explosions.

The left-hand panel of Fig. 2 shows some resulting predictions for radial electron density distributions representative of the Galactic halo, overlapped with observational data and constraints covering the entire virial radius, as presented by Miller & Bregman (2013), Grechich & Putman (2009), Blitz & Robishaw (2000), Bregman & Lloyd-Davies (2007), and Gupta et al. (2012). Our simulated radial electron number density profile also agrees closely with the
As a function of distance for different starting radii, while the black line shows the electron density obtained using the mean gas mass within each cell under the assumption of full ionization of a primordial gas composition, while the blue lines show the median values, enveloped by the 10th and 90th percentiles of the electron density distribution within the simulation. The spikes in the simulated density profiles are caused by individual substructures within the simulated halo. The middle panel shows the corresponding integrated DM, the different lines indicating different inner radii used as the starting point for the integration. The right-hand panel shows the predicted distribution of DM_{halo} over all possible sightlines, for three possible values of the inner radius.

Recent work of Nuza et al. (2014), which is based on a constrained simulation of the Local Group. The middle panel of Fig. 2 shows the cumulative increase of DM_{halo} as a function of distance for different starting radii, while the right-hand panel shows the distribution of DM_{halo} over all sightlines for these radii. At small radii, our results are consistent with the constraints from pulsar DMs discussed in section 4.6 of Gaensler et al. (2008). Most interestingly, we find that the electrons in the hot Galactic halo make a non-negligible contribution to the total observed DMs for FRBs.

Our simulation of the halo has not been constrained to match the particular structure of the Milky Way, so we cannot calculate specific values of DM_{halo} for individual FRB sightlines as we did for DM_{igm} in Section 3.1. Rather, we use the results of Fig. 2 to determine an indicative value for DM_{halo}. To make such an estimate, we should ideally use a radius to begin the integration that corresponds to the outer edge of the NE2001 model. However, this outer edge is direction dependent and is not a well-defined concept. Given that the maximal extent of NE2001 from the Galactic Centre is \( \sim 17 \) kpc (see fig. 3 and table 3 of Cordes & Lazio 2002), we adopt from Fig. 2 a representative halo electron column DM_{halo} = 30 pc cm\(^{-3}\), as listed for all relevant FRBs in Table 1.

3.3 The Local Universe

To consider the possible contribution of local superclusters to the DMs observed for FRBs, we use the final output of a cosmological hydrodynamic simulation of the Local Universe. Our initial conditions are similar to those adopted by Mathis et al. (2002) in their study (based on a pure N-body simulation) of structure formation in the Local Universe. We first apply a Gaussian smoothing to the galaxy distribution in the IRAS 1.2-Jy galaxy survey on a scale of 7 Mpc, and then evolve this structure linearly back in time to \( z = 50 \) following the method proposed by Kolatt et al. (1996). We then use the resulting field as a Gaussian constraint (Hoffman & Ribak 1991) for an otherwise random realization of a flat ΛCDM model, for which we assume a present matter density parameter \( \Omega_m = 0.3 \), a Hubble constant \( H_0 = 70 \) km s\(^{-1}\) Mpc\(^{-1}\), and an root mean square (rms) density fluctuation \( \sigma_8 = 0.9 \). The volume constrained by the observational data covers a sphere of radius \( \sim 110 \) Mpc, centred on the Milky Way. This region is sampled with more than 50 million high-resolution dark matter particles and is embedded in a periodic box \( \sim 343 \) Mpc on a side. The region outside the constrained volume is filled with nearly 7 million low-resolution dark matter particles, allowing good coverage of long-range gravitational tidal forces.

Unlike in the original simulation of Mathis et al. (2002) where only the dark matter component was present, here we also follow the gas and stellar components. For this reason, we extend the initial conditions by splitting the original high-resolution dark matter particles into gas and dark matter particles with masses of \( m_{gas} \approx 0.69 \times 10^6 \) M\(_\odot\) and \( m_{dm} \approx 4.4 \times 10^9 \) M\(_\odot\), respectively; this corresponds to a cosmological baryon fraction of 13 per cent. The total number of particles within the simulation is then slightly more than 108 million and the most massive clusters are resolved by almost 1 million particles. The physics included in the simulation is exactly the same as that used in the Magneticum Pathfinder simulation (to be described in Section 4.1 below). The lower panel of Fig. 1 shows the local structures and superclusters (Perseus-Pisces, Virgo, and Centaurus are all prominent features) and the positions of the known FRBs. Table 1 lists DM_{local} for each FRB, defined as the DM contribution along each sightline from this Local Universe simulation. As can be seen, DM_{local} is relatively small in all cases, with none showing an excess that corresponds to any specified constrained structures. Since the sightlines are all through unconstrained regions, the values of DM_{local} have no specific significance, and are simply representative of the DM of low-contrast density enhancements in this local volume. The resulting dispersion from small-scale structure and the IGM is incorporated into the cosmological signal considered in Section 4, and we therefore assume henceforth that the specific contribution to DM from known structures in the Local Universe is DM_{LU} = 0.

4 COSMOLOGICAL DM

After subtraction of the various foreground contributions to the DM as defined in equation (1) and discussed throughout Section 3, the remaining excess dispersion is listed as DM_{cumbo} in Table 1.
all nine cases, this is by far the dominant contribution to the total observed DM.

In the following sections, we describe our derivation of $\Delta M_{\text{DM}}$ using hydrodynamic, cosmological simulations. As per equation (2), this cosmological contribution to the DM of an FRB is composed of two parts. The first is $\Delta M_{\text{DM}}$, the signal coming from the diffuse gas within the cosmic web between the source and the observer. The second component is $\Delta M_{\text{host}}$, the contribution from the host galaxy of the FRB. Here, due to limited spatial resolution, our simulations can only capture the hot atmosphere of virialized haloes. For early-type galaxies, the host contribution should thus be incorporated by our simulation. However, for late-type galaxies, the simulation does not capture the contribution of the gas within the galactic disc. To properly model this component, additional assumptions or modelling would be required. For the purposes of the present discussion, we disregard the disc contribution to $\Delta M_{\text{host}}$, because of the likely low inclination of the disc and because the $(1+z)^{-1}$ dilution of $\Delta M_{\text{host}}$ in the observer’s frame is larger than for all subsequently encountered disperse media. (Thornton et al. 2013; Gao, Li & Zhang 2014; McQuinn 2014).

### 4.1 The Magneticum Pathfinder

We use the two largest simulations from the Magneticum Pathfinder\(^1\) data set (Dolag et al., in preparation). These two simulations use 896 and 352\textsuperscript{3} Mpc\(^3\) boxes, simulated using 2\times 1526\(^3\) and 2\times 1584\(^3\) particles, respectively, where we adopt a WMAP7 (Komatsu et al. 2011) ΛCDM cosmology with $\sigma_8 = 0.809$, $h = 0.704$, $\Omega_m = 0.728$, $\Omega_b = 0.272$, $\Omega\Lambda = 0.0456$, and an initial slope for the power spectrum of $n_s = 0.963$. A visualization of a 100-Mpc thick slice from the largest box at redshift $z = 0$ is shown in Fig. 3. In Table 2, we summarize the details of the two simulations, including the dark matter particle mass, gas particle mass, and softening length. Up to four stellar particles are generated for each gas particle.

Our simulations are based on the parallel cosmological TreePM-smoothed particle hydrodynamics (SPH) code GADGET\(^3\) (Springel 2005). The code uses an entropy-conserving formulation of SPH (Springel & Hernquist 2002) and follows the gas using a low-viscosity SPH scheme to properly track turbulence (Dolag et al. 2005b). It also allows radiative cooling, heating from a uniform time-dependent ultraviolet (UV) background, and star formation with the associated feedback processes. The latter is based on a subresolution model for the multiphase structure of the ISM (Springel & Hernquist 2003).

Radiative cooling rates are computed through the procedure presented by Wiersma, Schaye & Smith (2009). We account for the presence of the cosmic microwave background and for UV/X-ray background radiation from quasars and galaxies, as computed by Haardt & Madau (2001). The contributions to cooling from 11 elements (H, He, C, N, O, Ne, Mg, Si, S, Ca, Fe) have been pre-computed using the publicly available CLOUDY photoionization code (Ferland et al. 1998) for an optically thin gas in (photo)ionization equilibrium.

In the multiphase model for star formation (Springel & Hernquist 2003), the ISM is treated as a two-phase medium, in which clouds of cold gas form from the cooling of hot gas and are embedded in the hot gas phase. Pressure equilibrium is assumed whenever gas particles are above a given threshold density. The hot gas within the multiphase model is heated by supernovae and can evaporate the cold clouds. 10 per cent of massive stars are assumed to explode as core-collapse supernovae (CCSNe). The energy released by CCSNe (10\textsuperscript{51} erg per explosion) is modelled to trigger galactic winds with a mass loading rate proportional to the star formation rate (SFR), to obtain a resulting wind velocity $v_{\text{wind}} = 350 \text{ km s}^{-1}$. Our simulations also include a detailed model of chemical evolution (Tornatore et al. 2007). Metals are produced by CCSNe, by Type Ia supernovae and by intermediate and low-mass stars in the asymptotic giant branch (AGB). Metals and energy are released by stars of different mass by properly accounting for mass-dependent lifetimes (with a lifetime function as given by Padovani & Matteucci 1993), the metallicity-dependent stellar yields of Woosley & Weaver (1995) for CCSNe, the yields of AGB stars from van den Hoek & Groenewegen (1997), and the yields of Type Ia supernovae from Thielemann et al. (2003). Stars of different mass are initially distributed according to a Chabrier (2003) initial mass function.

Most importantly, our simulations also include a prescription for black hole growth and for feedback from active galactic nuclei. As for star formation, accretion on to black holes and the associated feedback is tracked using a subresolution model. Supermassive black holes (SMBHs) are represented by collisionless ‘sink particles’ that can grow in mass either by accreting gas from their environments or by merging with other black holes. This treatment is based on the model presented by Springel, Di Matteo & Hernquist (2005) and Di Matteo, Springel & Hernquist (2005) including the same modifications as in the study of Fabjan et al. (2010) plus some further adaptations (see Hirschmann et al. 2014, for a detailed description).

We use the SUBFIND algorithm (Springel et al. 2001; Dolag et al. 2009) to define halo and subhalo properties. SUBFIND identifies substructures as locally overdense, gravitationally bound groups of particles. Starting with a halo identified through the Friends-of-Friends algorithm, a local density is estimated for each particle via adaptive kernel estimation, using a prescribed number of smoothing neighbours. Starting from isolated density peaks, additional particles are added in sequence of decreasing density. Whenever a saddle point in the global density field is reached that connects two disjoint overdense regions, the smaller structure is treated as a substructure candidate, and the two regions are then merged. All substructure candidates are subjected to an iterative unbinding procedure with a tree-based calculation of the potential. These structures can then be associated with galaxies, and their integrated properties (such as stellar mass or SFR) can then be calculated. Note that with an adopted resolution limit for our simulations of $3 \times 10^9 \text{ M}_\odot$, any detected galaxy is assumed to contain a central SMBH.

### 4.2 Calculating the cosmological DM

Within the simulation, we assume a primordial mixture of hydrogen and helium with a hydrogen mass fraction of 0.752, and when calculating the electron density we take into account the actual ionization state of the medium. We disregard star-forming particles in this calculation, since their multiphase nature means that their free electron density is not properly characterized. The cosmological frequency shift is taken into account when integrating the free electron density (Deng & Zhang 2014; McQuinn 2014), such that

$$
\Delta M_{\text{DM}}(z_{\text{max}}) = \int_0^{z_{\text{max}}} \frac{3 \pi^2 c^3 n_e(z) \Omega}{1 + z} \, d\Omega,
$$

where we integrate up to some maximum redshift of interest $z_{\text{max}}$.

To actually construct past light cones from the simulations, we follow the common approach to stack the comoving volumes (e.g.
Figure 3. The distribution of baryonic material in the largest box of the Magneticum Pathfinder simulation at redshift zero. The colour indicates the gas temperature, ranging from dark red (cold) to light blue (hot), combined with the stellar component (white). The image shows a 100-Mpc thick, 1300-Mpc wide slice through the simulation at $z = 0$.

Table 2. Properties of the two simulation runs from the Magneticum Pathfinder analysed in this study.

<table>
<thead>
<tr>
<th>Name</th>
<th>Box size (Mpc $h^{-1}$)</th>
<th>Resolution level</th>
<th>Initial particle number</th>
<th>$m_{\text{dm}}$ (M$_{\odot} h^{-1}$)</th>
<th>$m_{\text{gas}}$ (M$_{\odot} h^{-1}$)</th>
<th>$m_{\text{stars}}$ (M$_{\odot} h^{-1}$)</th>
<th>Softening length (dm, gas, stars) (kpc $h^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1300 Mpc/mr</td>
<td>896</td>
<td>mr</td>
<td>$2 \times 1526^3$</td>
<td>$1.3 \times 10^{10}$</td>
<td>$2.6 \times 10^8$</td>
<td>$6.5 \times 10^8$</td>
<td>10.0, 10.0, 5.0</td>
</tr>
<tr>
<td>500 Mpc/hr</td>
<td>352</td>
<td>hr</td>
<td>$2 \times 1584^3$</td>
<td>$6.9 \times 10^8$</td>
<td>$1.4 \times 10^8$</td>
<td>$3.5 \times 10^7$</td>
<td>3.75, 3.75, 2.0</td>
</tr>
</tbody>
</table>

placing them at the proper distance $w(z_i)$ of the simulations; see for example Roncarelli et al. 2007, Ursino, Galeazzi & Roncarelli 2010 for similar approaches). To avoid replications of similar structures, we randomized consecutive slices by rotating and shifting. Our simulation volumes however are big enough so that we do not need to duplicate the simulation volumes for our 36 different individual slices. The number of outputs produced in the simulation was chosen so that the required radial integration length ($w(z_{i+0.5}) - w(z_{i-0.5})$)
of the individual slices always fit entirely within the simulated volume, which is placed at the proper distance \( w(z) \) according to the assumed cosmology. The opening angle is chosen so that the orthogonal extent – which depends on the angular diameter distance at the redshift of a slice – always fits entirely within the simulated volume. The cosmological signal up to a maximum redshift \( z_{\text{max}} \) is thus approximated by the stacking of the individual slices:

\[
DM_{\text{cosmo}}(z_{\text{max}}) = \frac{\text{max}}{\text{max}} \sum_{i=0}^{n} w(z_{i} - 0.1) \frac{1}{1 + z_{i}} \, dl.
\]

We produce maps of the integrated electron density across each slice using \( \text{smac} \) (Dolag et al. 2005a), each resolved with 4096 \( \times \) 4096 pixels and covering a field of view of \( 13' \times 13' \) for the 1300 Mpc/hr simulation and \( 5' \times 5' \) for the 500 Mpc/hr simulation. Each of these slices represents the corresponding cosmological volume within the light cone, while the actual integration is done converting the simulation to physical units first. We are using this volume as well as the galaxies (and their properties) to weight our source models as introduced in Section 4.4.

### 4.3 Medium-resolution simulation

We first consider results from the 1300 Mpc/hr simulation, which covers a large cosmological volume at intermediate spatial resolution. This allows us to study the overall distribution of \( DM_{\text{cosmo}} \) down to the scale of galaxy groups. The resulting distribution of \( DM_{\text{cosmo}} \) as a function of \( z_{\text{max}} \) can be seen in the left-hand panel of Fig. 4, where we show the distribution of \( DM_{\text{cosmo}} \) in the light cone when integrating up to the indicated redshift. The nine observed values of \( DM_{\text{cosmo}} \) listed in Table 1 are shown as black diamonds in Fig. 4, confirming the conclusions of previous authors that FRBs occur at large cosmological distances, \( 0.5 \leq z \leq 1 \) (Ioka 2003; Inoue 2004; Lorimer et al. 2007; Thornton et al. 2013).

The dashed black lines shown in the left-hand panel of Fig. 4 indicate fits to the \( DM_{\text{cosmo}} \) distribution \( P(DM_{\text{cosmo}}) \) of the form:

\[
P(DM_{\text{cosmo}}) = A(z) \times \left[ DM_{\text{cosmo}} + DM_{\text{fit}}(z) \right] \times \exp \left( -\frac{DM_{\text{cosmo}} + DM_{\text{fit}}(z)}{\sigma(z)} \right)
\]

where the constants can be written as function of redshift,

\[
A(z) = 2 \times 10^{-11} z^{-9} + 1.3 \times 10^{-7} z^{-4} + 5 \times 10^{-7} (z - 2.325)^{2},
\]

\[
DM_{\text{fit}}(z) = -770 z^{1.3} + 31.2 \sqrt{z}.
\]

\[
DM_{0}(z) = -108 + 926 z + 67 z^{3},
\]

\[
\sigma(z) = 126.9 z + 2.03 - 27.4 z^{2}.
\]

Note that we only fit the distribution of \( DM_{\text{cosmo}} \) down to 1 per cent of the maximum value for each value of \( z \), since this captures the bulk of the signal and because at their highest values the distributions of \( DM_{\text{cosmo}} \) take on a complex shape that can only be fitted properly with a combination of several broken power laws. Note also that this tail towards large values of \( DM_{\text{cosmo}} \) is sensitive both to the largest supercluster structures present (and therefore to the size of the underlying cosmological simulation) and to the ability of the
simulation to properly capture the inner regions and cool cores of galaxy clusters (see also the left-hand panel of Fig. 5 and the associated discussion below).

The right-hand panel of Fig. 4 shows the expected cumulative distribution of DM_{cosmo} if the detected FRBs originate from random locations throughout the Universe (i.e. at a probability of incidence proportional to the comoving volume within the light cone) up to some maximum observable redshift \( z_{\text{max}} \). The observed cumulative distribution of DM_{cosmo} for FRBs, shown in black, closely matches the simulated distribution for \( z_{\text{max}} = 1 \). We quantify this in the inset to the right-hand panel of Fig. 4, where we show the result of a series of Kolmogorov-Smirnov (KS) tests between the observations and the simulated distributions as a function of \( z_{\text{max}} \). This demonstrates that the data only match the simulations in a narrow range around \( z_{\text{max}} = 0.9 \).

We emphasize that although the 1300 Mpc/hr simulation is currently the largest of its kind, the corresponding spatial resolution is not good enough to properly capture details in the halo structure (and especially precise stellar components of haloes) at scales below massive galaxies. We therefore only use the 1300 Mpc/hr simulation for the overall distribution of DM_{cosmo} (i.e. the component dominated by DM_{gal}), a regime for which the 1300 Mpc/hr simulation is superior to the higher resolution 500 Mpc/hr simulation because the former captures structures on much larger scales. We switch to the smaller, higher resolution 500 Mpc/hr simulation when stellar properties of the haloes get important (e.g. when trying to account for DM_{host}), as we next consider in Section 4.4.

4.4 High-resolution simulation

In Section 4.3, we used the medium-resolution 1300 Mpc/hr simulation to determine the distribution of DM_{cosmo} for FRBs distributed randomly over the cosmic volume out to some maximum observable redshift. We now use the high-resolution 500 Mpc/hr simulation to calculate the corresponding distribution of DM_{cosmo} when FRBs are embedded in potential host galaxies. We consider three simple models in which the spatial distribution of detectable FRBs within the simulation volume is correlated with the properties and locations of individual galaxies.

(i) FRBs trace the total stellar component, as might result if FRBs are produced by an evolved population such as merging neutron stars. In this case, we assume that the FRB rate is proportional to the stellar mass within each galaxy. To compute the spatial distribution of FRBs, we only allow FRBs to occur at pixels in our simulation at which we identify a galaxy, and we weight the rate of FRB occurrence by the corresponding stellar mass.

(ii) FRBs are associated with massive stars, as would result if FRBs are produced by supernovae or young neutron stars. We here assume that the FRB rate is proportional to the current SFR. We calculate the rate of FRBs by again only allowing an FRB to occur at a pixel associated with an individual galaxy, but we now weight the FRB rate by the current SFR of that galaxy.

(iii) FRBs are associated with activity or interactions around the SMBH in a galaxy’s nucleus. Again we assume FRBs can only occur at pixels associated with individual galaxies, but we give all such pixels equal weight.

In each case, we wish to compute the expected distribution of DM_{cosmo}, and compare this to the FRB observations given in Table 1 to see if we can discriminate between possible FRB mechanisms. We construct simulated distributions of DM_{cosmo} by identifying the position of galaxies within each slice of the light cone. The predicted value of DM_{cosmo} for an FRB occurring within a given galaxy (disregarding the disc contribution as discussed in Section 4) is then the contribution within the light cone up to the position of that galaxy, as per equation (4). Using the global properties of this
galaxy determined as described in Section 4.1, we then assign a relative probability for the occurrence of an FRB at this location by weighting the corresponding calculated value of $D_{\text{cosmo}}$ as per one of the three schemes described above.

The left-hand panel of Fig. 5 shows the contribution to $D_{\text{cosmo}}$ in the light cone from a slice at redshift $z \approx 0.5$ in the 500 Mpx/hr simulation, overplotted with the positions of the most massive galaxies (which correspond to the central galaxies in groups and clusters). The right-hand panel of Fig. 5 shows the distribution functions for $D_{\text{cosmo}}$ through all pixels in the full slice (black line) and only for pixels associated with galaxies above a threshold in stellar mass (colour coded). We also show the distribution of $D_{\text{cosmo}}$ for the same slice in the 1300 Mpc/hr simulation (dashed line), in order to illustrate the contribution of even larger structures that are only present in the larger cosmological box. These large structures manifest as an excess in the tail of the distribution at the largest values of $D_{\text{cosmo}}$. However, for the range in $D_{\text{cosmo}}$ corresponding to haloes of all masses, the overall distributions of $D_{\text{cosmo}}$ for the medium and high-resolution simulations are reasonably similar and the differences due to resolution and box size will not significantly alter any of our conclusions. In general, the range of values derived for $D_{\text{cosmo}}$ agrees with the estimates made by McQuinn (2014).

Note that the different models for the spatial locations of FRBs all utilize the same underlying distributions in $D_{\text{cosmo}}$, but give different weights to the individual pixels depending on the global properties of the galaxy associated with each pixel.

We perform this calculation for every slice of our light cone and thereby construct distributions of $D_{\text{cosmo}}$ as a function of $z_{\text{max}}$ for each of the three different weighting schemes described above. The resulting cumulative distributions of $D_{\text{cosmo}}$ are shown in the left-hand panel of Fig. 6, together with the corresponding observed cumulative distribution of $D_{\text{cosmo}}$ for the FRBs listed in Table 1.

There are only nine observed data points at present, collected in a very inhomogeneous way rather than from a single survey. Thus, we cannot draw robust conclusions from the present sample. Nevertheless, the left-hand panel of Fig. 6 shows clearly that the detected FRBs extend up to a maximum redshift $z_{\text{max}} \approx 0.6–0.9$, independent of their origin or detailed spatial distribution with respect to any host galaxies. We quantify this in the right-hand panel of Fig. 6, where we show the results of KS tests between the observed values of $D_{\text{cosmo}}$ and the simulated distributions as a function of maximum redshift for the three scenarios involving FRBs in host galaxies, and also for the random (unweighted) distribution of FRBs considered in Section 4.3. It is clear that all four possibilities are a reasonable match to the observations, although the best-fitting values of $z_{\text{max}}$ are smaller for FRBs in host galaxies than for FRBs distributed randomly (as expected given that the former involves sightlines biased towards high DMs as per Fig. 5). The differences in the best fits for $z_{\text{max}}$ for the three host-galaxy models are small, but the fact that case (i) gives a lower redshift than case (ii), and that case (ii) is lower than case (iii), can be understood qualitatively. If we adopt case (i) in which the frequency of FRBs tracks stellar mass, massive galaxies experience reduced star formation due to SMBH activity in these systems; thus in case (ii), FRBs occur on sightlines to lower mass galaxies, such that $D_{\text{host}}$ is lower and hence $z_{\text{max}}$ is higher. Finally, FRBs associated with SMBHs result in a set of sightlines that have no weighting at all for the size of the host galaxy, and therefore result in even larger values of $z_{\text{max}}$.

The similarities between the form of the cumulative $D_{\text{cosmo}}$ distributions of different weighting schemes at these redshifts (seen as the green curves in the left-hand panel of Fig. 6) means that even once we obtain a much larger sample of FRBs, it will be difficult

\[ z_{\text{max}} \]

\[ 0.6–0.9 \]

\[ z_{\text{max}} \]

\[ 4 \]

\[ 2 \]

\[ 2 \]

\[ 2 \]
Figure 7. The expected distribution of FRB fluences as a function of maximum redshift, $z_{\text{max}}$, assuming a nominal energy $E = 1.4 \times 10^{40}$ erg in the radio pulse. The left-hand panel shows simulations of the cumulative distribution of fluence as a function of maximum redshift for randomly distributed FRBs, while the right-hand panel shows the equivalent calculations when FRBs are associated with host galaxies and when the FRB rate depends on total stellar mass (solid line), SFR (dashed line), or the presence of a central black hole (dotted line). The colours correspond to a range of maximum redshifts as per the legend to Fig. 4. Observed FRB fluences are overplotted in black: the second curve from the right shows the fluences in Table 1, while the other six curves show fluences shifted up or down in successive steps of half a decade to provide a scaling to other values of $E$.

5 EXPECTED FLUENCES AND ENERGIES

We now consider the implications for the observed distribution of FRB fluences. We consider the same three possible spatial distributions for FRBs as discussed in Section 4.4, along with a uniform (random) distribution of FRBs within the comoving volume as in Section 4.3. However, while before we calculated distributions of DM from the simulations, here we infer fluences, and use these to test the hypothesis that FRBs are standard candles, each with the same emitted radio energy.

We assume that each FRB has the same isotropic total energy, $E$, where

$$
\frac{E}{4\pi D_{\text{lum}}^2(z_0)} = F_\nu v_\nu (1 + z_0),
$$

for an FRB of received fluence $F_\nu$ at an observing frequency $v_\nu$, where $D_{\text{lum}}$ is the luminosity distance for the FRB’s redshift, $z_0$.

Fig. 7 shows the expected cumulative distributions in fluences for a range of values of $E$ and as a function of maximum FRB redshift: the left-hand panel shows how such fluences should be distributed if FRBs are located randomly in the cosmic volume (see Section 4.3), while the right-hand panel shows the corresponding distribution if the number of FRBs per galaxy scales as the total stellar mass, as the SFR, or at an equal rate per massive galaxy (see Section 4.4). For comparison, the cumulative distribution of observed fluences from Table 1 is overplotted as black points, and also shifted up or down to mimic different values of the fiducial energy that we assign to the FRBs. Again having only nine data points does not allow robust conclusions, but overall the shapes of the predicted distributions in fluence are all similar to that observed, showing that the data at present are consistent with the FRB population being standard candles. This favours mechanisms that produce FRBs through a deterministic process with a small number of free parameters (e.g. blitzars or neutron–star mergers; Totani 2013; Falcke & Rezzolla 2014) over stochastic process such as flares or reconnection events that typically show a wide distribution of energies (Popov & Postnov 2013; Loeb, Shvartzvald & Maoz 2014; Lyubarsky 2014). The fluences for a uniform (random) distribution show very good agreement with the data. Models in which FRBs trace galaxies provide a slightly poorer match to the observed fluences, but this difference is not statistically significant, and none of the simulated distributions can be excluded. In Fig. 8, we show the value of the isotropic energy required to match the distribution of observed fluences as a function of maximum observed redshift, under the assumption that FRBs are standard candles, and for the same four models for the spatial distribution of FRBs as shown in Fig. 7. Note that this only depends on the spatial distribution of possible FRB hosts in the simulations. With the DM distributions considered in Sections 4.3 and 4.4, we can then infer $E \sim 7 \times 10^{40}$ erg for any of the three

to use their DMs to discriminate between different possible origins if the observed values of $\text{DM}_{\text{cosmo}}$ continue to mostly fall in the range $\sim 300–1000$ pc cm$^{-3}$. Conversely, as we approach $z_{\text{max}} \sim 2$ the distributions of $\text{DM}_{\text{cosmo}}$ diverge for the different weighting schemes (seen in blue in the left-hand panel of Fig. 6). The much higher SFR at these earlier epochs leads to larger differences in the weighting schemes between models, and thus to a broader range in the predicted distributions of $\text{DM}_{\text{cosmo}}$. If (through either improved sensitivity or simply a larger sample size) we can begin to detect an appreciable fraction of FRBs with $\text{DM}_{\text{cosmo}} \gtrsim 1000–1500$ pc cm$^{-3}$, we may be able to distinguish between the different models, especially between FRB mechanisms that track the SFR compared to other possibilities.
models in which FRBs trace large-scale structure, for which we found $z_{\text{max}} \sim 0.6–0.7$ in Fig. 6. For randomly distributed FRBs, for which we found $z_{\text{max}} \approx 0.9$ in Section 4.3, $E$ is slightly larger than this ($E \sim 9 \times 10^{40}$ erg). We note that these energies, inferred using equation (11), are one to two orders of magnitude larger than those reported in most other papers (e.g. Thornton et al. 2013; Keane & Petroff 2015), because these previous authors have omitted the factor $4\pi$ needed to calculate isotropic energies, and have multiplied by the observing bandwidth rather than the observing frequency. The latter is far less dependent on the specifics of the observations, and (in the absence of any spectral index information) is a better rough estimate of the integrated radio energy of the burst; see Section 3.1 of Kulkarni et al. (2014) for a more detailed treatment. The energies we have calculated are a very good match to the predicted energy release $E \approx 3 \times 10^{40}$ erg predicted by the blazar model for FRBs presented by Falcke & Rezzolla (2014) and also agree with $E \gtrsim 10^{40}$ erg expected from FRBs generated by magnetar flares (Kulkarni et al. 2014; Lyubarsky 2014).

We note from Table 1 that FRBs 110220 and 140514 occurred at almost the same position on the sky, but with different DMs and different fluences. If FRBs are standard candles, the simplest expectation along a single sightline is that an FRB with a higher DM is farther away and thus must have a lower fluence. This is the opposite to what is observed for these two sources, for which FRB 140514 has a lower observed DM than FRB 110220 but also a lower fluence. However, given the significant angular structure seen in the simulation (see Fig. 5), we cannot exclude large fluctuations in DM, even along sightlines separated by 0.1°. In addition, the reported fluences of FRBs have significant systematic uncertainties due to their unknown location within the telescope beam (see Spitler et al. 2014; Keane & Petroff 2015).

6 CONCLUSIONS

We have used a set of advanced cosmological hydrodynamic simulations to investigate the contributions to DMs of FRBs from the Milky Way disc and halo, from the Local Universe, from cosmological large-scale structure, and from potential host galaxies. Through this combination of calculations, we have made predictions for the expected DMs of FRBs distributed over different redshift ranges and for differing spatial distributions.

For the foreground (non-cosmological) contributions to DM, we obtain two main results.

(i) The Milky Way’s hot halo contributes an additional $\sim 30$ pc cm$^{-3}$ to the total DM, over and beyond the DM contribution from the Galactic disc predicted by the NE2001 model of Cordes & Lazio (2002, 2003). Except for FRBs at low Galactic latitudes ($|b| < 20°$), this means that the full Galactic contribution to FRM DMs is approximately double previous estimates.

(ii) By using a constrained simulation of the Local Universe, we exclude any significant contribution to FRB DMs from prominent structures out to a distance of $\sim 110$ Mpc.

From our simulations of DMs at cosmological distances, we can make four additional conclusions.

(iii) The observed DM distribution for the available sample of nine extragalactic FRBs is consistent with a cosmological population detectable out to a redshift $z_{\text{max}} \approx 0.6–0.9$, regardless of the specifics of how FRBs are distributed with respect to large-scale structure or the properties of their host galaxies.

(iv) If future observations can extend the FRB population to higher DMs and higher redshifts ($DM_{\text{cosmo}} \gtrsim 1000–1500$ pc cm$^{-3}$, $z_{\text{max}} \approx 2$) than for the currently known sample, we will be able to use the resulting DM distribution to determine whether FRBs are related to recent star formation or have some other origin.

(v) The distribution of observed FRB fluences is consistent with a standard-candle model, in which the radio emission from each FRB corresponds to the same isotropic energy release.

(vi) Under the assumption that FRBs are standard candles, the isotropic energy associated with each radio burst is $\sim 7 \times 10^{40}$ erg if FRBs are embedded in host galaxies and trace large-scale structure, or $\sim 9 \times 10^{40}$ erg if FRBs occur at random locations in the Universe. The blazar model, in which a supramassive young neutron star is initially supported against gravitational collapse through its rapid rotation, but then later implodes to form a black hole once it has spin down sufficiently (Falcke & Rezzolla 2014), is an FRB mechanism that may meet this joint requirement that FRBs are standard candles and that the radiated energy is $\gtrsim 10^{40}$ erg. A more statistically robust distribution of fluences resulting from additional FRB detections will be able to better test whether FRBs are indeed standard candles, while an extension to higher redshifts can test whether FRBs track the SFR as expected for the blazar model.

There are many additional issues that we have not considered in this initial study. From an observational perspective, the fluxes and fluences of FRBs are difficult to determine (e.g. Spitler et al. 2014), and the selection effects associated with the detectability of FRBs are still being understood (Lorimer et al. 2013; Burke-Spolaor & Bannister 2014; Petroff et al. 2014b; Keane & Petroff 2015). In addition, DMs and fluences are not the only information available: most FRBs show significant scattering (e.g. Thornton et al. 2013),
which in principle can provide additional constraints on their distances and environments (Macquart & Koay 2013; Katz 2014). In terms of foreground modelling, it is now well established that the NE2001 model is not a complete description of the Galactic electron distribution, especially at high latitudes (Gaensler et al. 2008). While any errors in NE2001 do not have a qualitative effect on the conclusions of our present study, improved foreground electron distributions will be needed if FRBs are to be used as precision probes of cosmology and dark energy (e.g. Gao et al. 2014; Zhou et al. 2014). In addition, the exact distribution of baryons around galactic haloes is still not well understood and depends on details of its implementation into numerical simulations (e.g. Ford et al. 2015), which could alter the DM signal expected from intervening, low-mass galaxies (e.g. McQuinn 2014). Looking to the future, not only can we expect larger numbers of FRBs, but we now know that FRBs are polarized (Petroff et al. 2015). This raises the prospect of detecting Faraday rotation for FRBs, so that we can simultaneously obtain both DMs and rotation measures. Such data can provide direct measurements of the magnetization of the IGM (Zheng et al. 2014; Macquart & Johnston 2015), and hence can potentially discriminate between different mechanisms for the origin of cosmic magnetism (e.g. Donnert et al. 2009).

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