

# Experimental and theoretical studies on inorganic magic clusters: $M_4X_6$ ( $M = W, Mo, X = O, S$ )

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## Abstract

Studies using ultraviolet photoelectron spectroscopy (UPS) and density functional theory (DFT) demonstrate that  $M_4X_6$  ( $M = W, Mo$  and  $X = O, S$ ) clusters show large gaps (about 2 eV) between the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO), indicative of their high stability and chemical inertness. In particular,  $W_4O_6$  has a lower symmetry and a larger HOMO–LUMO gap than other hitherto discovered magic clusters. Although the similarity between the electronic structures of  $W_4O_6$  and  $Mo_4S_6$  may be regarded as an indication that both clusters have similar geometric structures, our detailed DFT-calculations reveal otherwise. This result implies that synergetic approach using theoretical and experimental methods are essential to shed light on cluster geometries.

Geometric, electronic and chemical properties of nanostructures are often much different compared to their bulk counterparts. Among various nanoclusters, the interest on so-called ‘magic clusters’ has been increasing since the discovery of  $C_{60}$  [1]. Magic clusters exhibit closed electronic shell configurations, resulting in large gaps between the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO), high ionization potentials and low electron affinities, which are shown to be a prerequisite for chemical inertness and high stability of the clusters [1–15]. In the case of alkali metal-like clusters, the magic numbers with large HOMO–LUMO gaps can be explained by the electron shell model [14]. Besides these electronic properties, compact and highly symmetric structures are often observed for magic clusters [1–15]. Therefore, magic clusters are regarded as potential candidates for building blocks of new cluster materials, i.e.,

one may be able to synthesize cluster assemblies [16], in which original geometric structures of the free magic clusters remain unchanged. Well-known examples for magic clusters are  $C_{60}$  [1],  $Na_8$  [5],  $Al_{13}^-$  [6,7],  $Sb_4$  [8],  $Au_{20}$  [9], and  $Au_{55}$  [10] and some of these magic clusters are actually shown to form cluster materials [8].

Recently, attempts to synthesize new cluster materials have been extended to inorganic complexes [17]. For example, fullerene-like structures consisting of  $MoS_2$  units were synthesized previously [18], and it was shown that  $Al_{13}H$  exhibits a HOMO–LUMO gap of 1.4 eV [11]. In the present work, electronic and geometric structures of inorganic clusters consisting of 4 metallic and 6 non-metallic atoms ( $M_4X_6$ ,  $M = W, Mo$  and  $X = O, S$ ) are introduced.  $W_4O_6$  clusters show a large HOMO–LUMO gap in the anion ultraviolet photoelectron spectroscopy (UPS), which is also confirmed by theoretical calculations.  $W_4O_6$  shows a relatively low symmetry compared to other hitherto discovered magic clusters such as  $C_{60}$  and  $Au_{20}$ . Also, for  $W_4S_6$  and  $Mo_4S_6$ , large HOMO–LUMO gaps were found using UPS, and

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theoretical calculations are in line with experimental observations. Electronic structures of both isoelectric  $M_4O_6$  and  $M_4S_6$  are analogous, yet interestingly the geometric structure of  $M_4S_6$  differs significantly from that of  $W_4O_6$ .

$W_4O_m^-$ ,  $W_4S_m^-$  or  $Mo_4S_m^-$  ( $m = \text{integer}, 1-6$ ) clusters were produced by exposing W and Mo to  $O_2$  (for oxide clusters) or  $H_2S$  (for sulphide clusters) in the pulsed arc cluster ion source (PACIS) [19]. It is important to mention that exposure of Mo to  $H_2S$  at about 600 K results in formation of  $MoS_2$  nanostructures without H impurities [20]. The cluster temperature is sufficiently high when W and Mo react with  $H_2S$  reagents in our PACIS source, excluding the possibility that the  $M_nS_m^-$  structures are contaminated by H impurities. The inorganic clusters formed in the cluster source are then cooled down in the extender, and at the UPS measurement stage, the temperature of the clusters is estimated to be room temperature. The mass of the clusters was selected by means of a time-of-flight (TOF) mass spectrometer, and the UPS spectra of the mass-selected clusters were taken using UV laser pulse (photon energy = 4.66 or 6.4 eV).

Theoretical investigations on  $Mo_4S_m^-$  clusters have been performed applying the generalized gradient approximation (GGA) for the exchange-correlation potential in the density functional theory (DFT) as prescribed by Becke's three parameter hybrid functionals using the non-local correlation provided by the Lee, Yang, and Parr (commonly referred as B3LYP). The 6-311G\*\* basis set for S and 3-21G\*\* for Mo have been used. For  $W_4O_m^-$ , we used GGA for exchange-correlation potential prescribed by Becke-Perdew-Wang (commonly known as BPW91). The atomic orbitals were presented by a Gaussian basis. We used the 6-311G\* basis set for O and the Stuttgart relativistic effective core potential basis set for W. The structures of both neutral and anionic clusters have been optimized globally without any symmetry constraint and by starting with various geometries. For all the calculations, GAUSSIAN 98 code has been used. Details of the calculations of the clusters will be described elsewhere [21,22].

In Fig. 1, UPS spectra of  $W_4O_m^-$  for  $m = 0-6$  are displayed. The pure  $W_4$  cluster shows an electron affinity of 1.5 eV without any distinct indication of a HOMO-LUMO gap in the binding energy range between 0 and 6 eV. As the number of oxygen atoms attached to the tungsten host increases from 0 to 4, electron affinity increases gradually (from 1.5 to 1.9 eV). HOMO-LUMO gaps cannot be clearly discriminated in the UPS spectra for  $n = 0-4$ , whereas for  $W_4O_5^-$ , a single distinct peak is observed at 3.0 eV, followed by the second peak at 4.5 eV, which can be attributed to the HOMO and LUMO of the neutral cluster, respectively. Correspondingly, the HOMO-LUMO gap of the  $W_4O_5$  cluster is determined to be 1.5 eV. For  $W_4O_6$ , the electron affinity

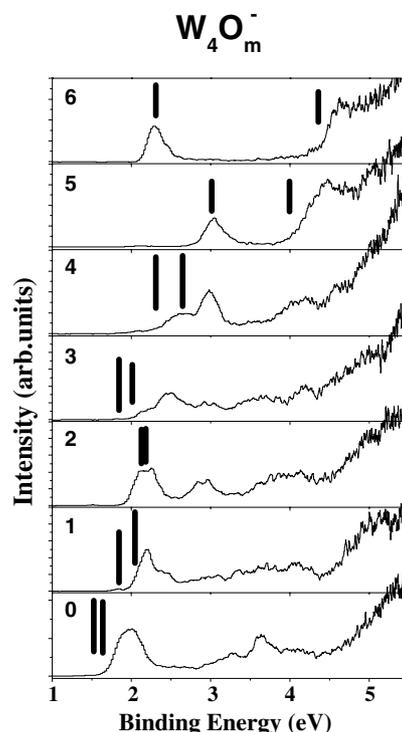


Fig. 1. UPS spectra of  $W_4O_m^-$  cluster anions with  $m = 0-6$  are compared with theoretically calculated vertical detachment energies (lines in the spectra) (photon energy = 6.4 eV). The vertical detachment energies correspond to the transition energies from the anion ground states with spin state  $M$  to the neutral counterparts with  $M' = M \pm 1$ , which are in a geometry identical to that of the anion ground state. Good agreements between theory and experiments can be found, suggesting a high reliability of the geometric structures suggested by DFT-calculations.

becomes much lower and the HOMO-LUMO gap (2.2 eV) becomes larger compared to those of  $W_4O_5$ . Considering that a large HOMO-LUMO gap and a correspondingly low electron affinity is an indication for a closed electronic shell configuration, one can suggest that  $W_4O_6$  clusters should exhibit a high stability and chemical inertness, and thus might be suitable for building blocks of cluster materials. The HOMO-LUMO gap cannot be distinguished in the UPS spectra, when number of oxygen atoms exceeds 7 (not shown here) [22].

To shed light on detailed geometric and electronic structures of  $W_4O_m$  clusters, theoretical calculations were performed (Fig. 2). The bare  $W_4$  cluster shows a tetrahedral structure, which does not undergo significant relaxation with increasing number of oxygen atoms from 1 to 4. In contrast to the first four oxygen atoms, addition of the fifth oxygen atom significantly weakens the W-W bonding in the  $W_4$  framework, resulting in insertion of two oxygen atoms in the  $W_4$  framework to form two W-O-W bonds, thus leaving three W-W bonds. The sixth oxygen atom forms a third W-O-W bond in a  $W_4O_6$  cluster (neutral as well as anion), leading to the formation of a hexagonal ring structure in a  $W_4O_6$

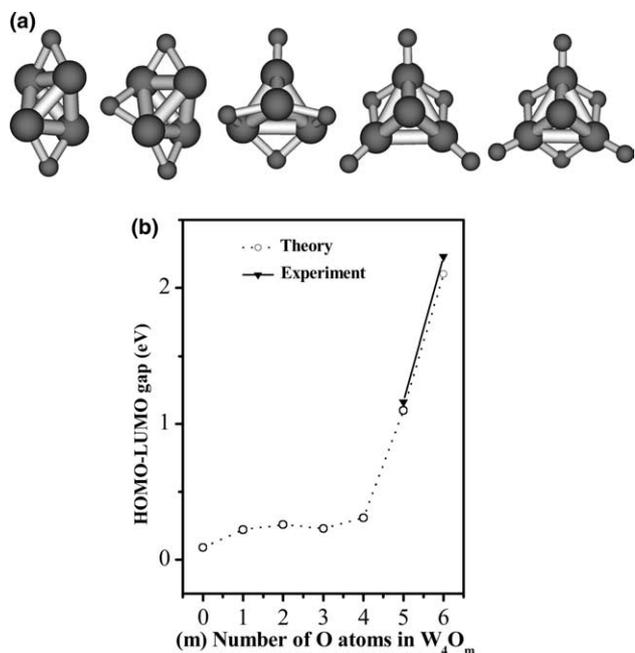


Fig. 2. (a) Optimized structures of  $W_4O_m$  with  $m = 2-6$ . Larger spheres correspond to W atoms, whereas smaller ones represent O. (b) The calculated HOMO-LUMO gaps are compared with experimentally determined values. For  $m = 0-4$ , the HOMO-LUMO gaps cannot be discriminated in the experimental UPS spectra.

cluster. The hexagonal ring structure seems to be an energetically favored arrangement of W and O atoms, since the  $W_3O_3$  hexagonal ring was also found to be a fundamental building block of amorphous  $WO_3$  films [23]. Therefore, it is suggestive that the tungsten oxide clusters containing this hexagonal ring is more robust than other tungsten oxide clusters without similar ring structures. In fact, a  $W_3O_9$  cluster, which is the most abundant unit of tungsten oxide vapors (indicating that  $W_3O_9$  is the most stable unit among various tungsten oxide clusters), also contains a hexagonal  $W_3O_3$  ring, confirming a high stability of the  $W_3O_3$  ring [24]. For more detailed explanations about the geometric structures of  $W_4O_m$  and their anionic counterparts, see [22].

To check the reliability of the theoretical approach used here, we have calculated the vertical detachment energies of  $W_4O_m^-$  clusters. As it is displayed in Fig. 1, theoretically calculated vertical detachments energies agree with the binding energies of the peaks in the UPS spectra within 0.2 eV, confirming that the geometric structures of  $W_4O_m$  illustrated in Fig. 2 are accurate. It is important to note that the HOMO-LUMO gap of  $W_4O_6$  is 2.2 eV, which is even larger than those of  $Na_8$  (1.1 eV) [5],  $C_{60}$  (1.5 eV) [4],  $Au_{20}$  (1.8 eV) [9], and  $W@Au_{12}$  (1.6 eV) [25], implying that  $W_4O_6$  clusters can be more stable and chemically inert than these aforementioned magic clusters.

Considering valence electronic structures, S and O are isoelectronic, as Mo and W are. Since electronic

structures and chemical properties of clusters are often dominated by the number of valence electrons, one may expect  $W_4S_6$ ,  $Mo_4O_6$  and  $Mo_4S_6$  to be magic just as  $W_4O_6$  is. To obtain a better understanding of the structures of  $M_4S_m^-$  clusters, UPS spectra of  $W_4S_m^-$  and  $Mo_4S_m^-$  clusters were collected (Fig. 3). The general trend for the development of the UPS spectra of  $W_4S_m^-$  with increasing number of S atoms ( $m$ ) is analogous to that found for  $W_4O_m^-$  clusters (Fig. 1). With increasing  $m$  from 1 to 5, the electron affinity gradually increases, whereas the  $W_4S_6^-$  clusters show a lower electron affinity compared to that of  $W_4S_5^-$ . No indications for large HOMO-LUMO gaps can be observed for  $W_4S_m^-$  with  $m = 1-5$ ; however, the  $W_4S_6^-$  cluster exhibits a distinct HOMO-LUMO gap of 1.7 eV. A similar trend can also be found for the  $Mo_4S_m^-$  clusters, yielding a HOMO-LUMO gap of about 2.0 eV for  $Mo_4S_6^-$  (Fig. 3). This result implies that  $M_4S_6$  should also be extraordinarily stable and chemically inert like  $W_4O_6$ .

To get an understanding of the geometric and electronic structures of  $Mo_4S_m^-$  clusters, theoretical calculations were also performed. The optimized ground state structures of these clusters are shown in Fig. 4a. Analogous to  $W_4$ ,  $Mo_4$  exhibits a tetrahedral structure. In contrast to the case of  $W_4O_m^-$ , the geometries of  $Mo_4S_m^-$  clusters undergo a sudden transformation when three S atoms are attached to the  $Mo_4$  frame, leading to the conversion of the metallic tetrahedron frame to a rectangular ring. In  $Mo_4S_4^-$  the nearly tetrahedral structure of the  $Mo_4$  unit is retained. The same holds for  $Mo_4S_5^-$ . Finally, all edges of the  $Mo_4$  tetrahedron are bridged by S in the  $Mo_4S_6^-$  cluster, yielding a three dimensionally compact and symmetric tetrahedral structure. The

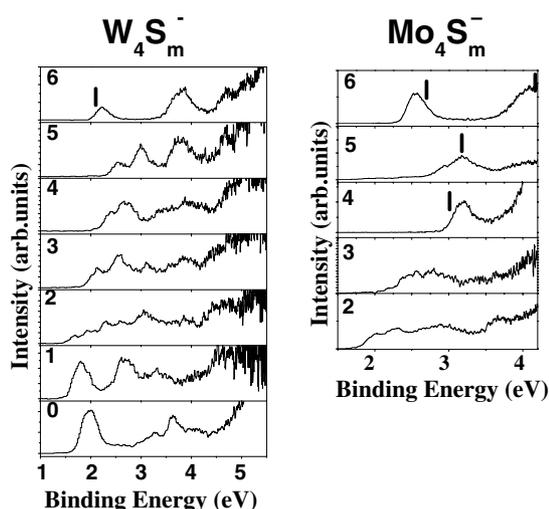


Fig. 3. UPS spectra of  $W_4S_m^-$  (photon energy = 6.4 eV) and  $Mo_4S_m^-$  (photon energy = 4.66 eV) cluster anions with  $m = 0-6$  are shown. For  $Mo_4S_m^-$  ( $4 \leq m \leq 6$ ) and  $W_4S_6^-$  theoretically determined vertical detachment energies (lines in the spectra) are compared with experimental data.

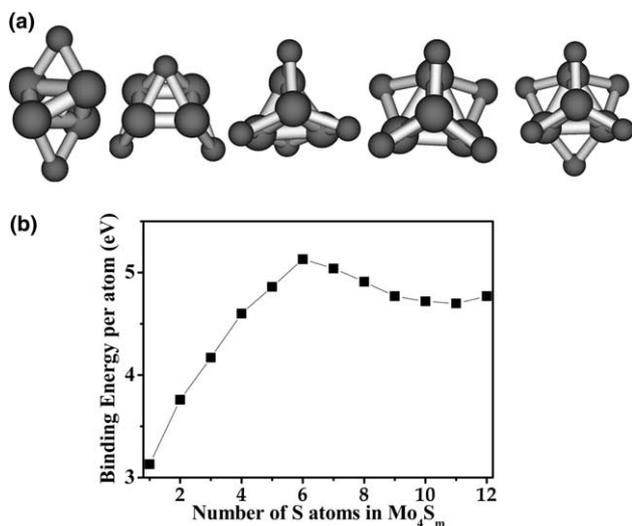


Fig. 4. (a) Optimized structures of  $\text{Mo}_4\text{S}_m$  with  $m = 2-6$ . (b) The calculated binding energies per atoms of  $\text{Mo}_4\text{S}_m$  with  $m = 1-12$ .

structure of  $\text{Mo}_4\text{S}_6$  is much different from that of  $\text{W}_4\text{O}_6$ , which has a much lower symmetry with three terminal O atoms attached to the  $\text{W}_3\text{O}_3$  hexagonal ring (Fig. 2). It seems that S tends to have bridge bonding with metal atoms, whereas O can form double bonds with a metal atom. Theoretically calculated vertical detachment energies are consistent with the experimental data (Fig. 3). The theoretically determined HOMO–LUMO gap of  $\text{Mo}_4\text{S}_6$  is the largest among the  $\text{Mo}_4\text{S}_m$  clusters studied in the present work, in line with the experimental data.

In Fig. 4b, the binding energies per atom for  $\text{Mo}_4\text{S}_m$  clusters are plotted versus number of S atoms ( $m$ ). The binding energy of the  $\text{Mo}_4\text{S}_6$  cluster represents a maximum in the series  $\text{Mo}_4\text{S}_m$  ( $m = 1 \dots 12$ ), indicating that the  $\text{Mo}_4\text{S}_6$  clusters is indeed the most stable, and therefore, most likely chemically inert.

Currently, no detailed theoretical calculations on  $\text{W}_4\text{S}_m^-$  clusters exist. However, the structural similarities between  $\text{MoS}_2$  and  $\text{WS}_2$  in bulk form as well as in nanocomposites have been verified in previous studies, suggesting that the structural evolution of W tetramer upon addition of S may be analogous to the case of the Mo tetramer [26]. According to our preliminary theoretical calculations, the electron affinity of  $\text{W}_4\text{S}_6$  with the same geometry as that of  $\text{Mo}_4\text{S}_6$  amounts to 2.1 eV, which is in line with the experimental data in Fig. 3, suggesting that the geometric structure of  $\text{Mo}_4\text{S}_6$  in Fig. 4 can be also valid for  $\text{W}_4\text{S}_6$ .

$\text{W}_4\text{O}_6$  and  $\text{Mo}_4\text{S}_6$  show larger HOMO–LUMO gaps than other non-magic clusters consisting of the same elements. The electronic structures of clusters are generally sensitive to the geometric structure [9], and therefore analogous electronic structures of different clusters are often regarded as indicative of similar geometric structures, i.e., it could be tentatively suggested that these two clusters should exhibit identical structures. How-

ever, according to our detailed theoretical calculations, both clusters show different geometries, implying that the electronic structures of both clusters should be dominated by the number of valence electrons. Magic numbers of metallic clusters are generally explained by simple electron counting rules such as the one-electronic shell model for alkali and coinage metal clusters [14] or the 18-electron rule for d-metal complexes [25]. In a purely ionic model, considering that O and S act as two-electron acceptors and Mo and W atoms have 6 electrons in the valence d shells, 12 electrons are left in the  $\text{M}_4$  frameworks of the magic  $\text{M}_4\text{X}_6$  clusters. These 12 electrons, i.e. 2 electrons per tetrahedron edge (‘bond’) could be sufficient for the explanation of the bonding within the  $\text{M}_4$  framework. Another, less ionic description, but with some reminiscence to the jellium model could also explain the ‘magic’ character of the  $\text{M}_4\text{X}_6$  clusters. The tetrahedral  $\text{W}_4/\text{Mo}_4$  clusters have 24 valence electrons, corresponding to a closed jellium shell (20 electrons) plus 4 electrons left. In the case of the  $\text{M}_4\text{X}_6$  clusters these 4 additional electrons may be donated to sulfur or oxygen, leaving the 20 electrons at the  $\text{W}_4/\text{Mo}_4$  core of the clusters. This would correspond to formal charges of +1 and  $-2/3$  for W/Mo and S, respectively.

In conclusion, we have shown that  $\text{M}_4\text{X}_6$  with  $\text{M} = \text{W}, \text{Mo}$  and  $\text{X} = \text{O}, \text{S}$  show large HOMO–LUMO gaps and therefore they should be chemically inert and more stable than other non-magic clusters. These clusters can be candidates of building blocks of cluster materials. In particular,  $\text{W}_4\text{O}_6$  has a lower symmetry than other hitherto discovered magic clusters; however, it is more ‘magic’ than other magic clusters in terms of electronic structure. Similar electronic structures of  $\text{M}_4\text{S}_6$  and  $\text{M}_4\text{O}_6$  may be regarded as an evidence for identical geometric structure of both clusters; however, our detailed DFT-calculations show that both clusters have much different geometric structures, implying that synergistic approach between theory and experiment is inevitable to completely understand cluster geometries.

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