Experimental Observation of the Aubry Transition in Two-Dimensional Colloidal Monolayers

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(Received 20 November 2017; revised manuscript received 1 February 2018; published 28 March 2018)

The possibility to achieve entirely frictionless, i.e., superlubric, sliding between solids holds enormous potential for the operation of mechanical devices. At small length scales, where mechanical contacts are well defined, Aubry predicted a transition from a superlubric to a pinned state when the mechanical load is increased. Evidence for this intriguing Aubry transition (AT), which should occur in one dimension (1D) and at zero temperature, was recently obtained in few-atom chains. Here, we experimentally and theoretically demonstrate the occurrence of the AT in an extended two-dimensional (2D) system at room temperature using a colloidal monolayer on an optical lattice. Unlike the continuous nature of the AT in 1D, we observe a first-order transition in 2D leading to a coexistence regime of pinned and unpinned areas. Our data demonstrate that the original concept of Aubry not only survives in 2D but is relevant for the design of nanoscopic machines and devices at ambient temperature.


In the expanding fields of nanoscience, where the competition of length scales is of key importance, Aubry’s theoretical concept [1,2], how to achieve frictionless sliding, is one of the most challenging topics in nanotribology [3], with immediate technological applications. The nowadays pervasive tribological concept of superlubricity was originally inferred from the one-dimensional (1D) Frenkel-Kontorova (FK) class of models [4], describing a chain of interacting particles subject to a periodic substrate potential. Aubry showed that, in the thermodynamic limit and at zero temperature, the 1D incommensurate chain-substrate interface may undergo a second-order transition between an unpinned and a pinned state at a critical value of the substrate corrugation, i.e., contact strength, \( U_0 \). In the unpinned state, the minimum force required to achieve sliding, i.e., the static friction, should vanish: The interface incommensurability can indeed prevent asperity interlocking and collective stick-slip motion of the interface atoms, with a consequent negligibly small frictional force.

After remaining locked away for several decades, Aubry-type signatures were recently observed experimentally in finite 1D linear laser-cooled ion chains on corrugated potentials [5–8]. In contrast, the demonstration and characterization of the Aubry transition in extended and mismatched two-dimensional (2D) monolayers at finite temperature, corresponding to more realistic conditions, is still lacking. Previous experimental work on 2D systems including telescopic dynamics [9] and water flow [10] in carbon nanotubes, sliding of graphite flakes [11–13] and mesas [14–16], graphene nanoribbons [17], cluster nanomanipulation [18,19], or rare-gas island inertial motion [20] has demonstrated superlubricity, i.e., an ultralow static friction, scaling sublinearly with the contact size. However, without the possibility of tuning interaction parameters, the nature of the Aubry transition at 2D interfaces cannot be unraveled and does not disclose how a change from a superlubric to a pinned state occurs.

Here, we report the first microscopically resolved experimental study of the Aubry transition by investigating an extended colloidal layer driven over a laser-generated periodic potential. Unlike conventional substrates, here all relevant physical parameters, such as the lattice periodicity and the contact strength, can be controlled in situ [21]. Unlike 1D, a sliding 2D crystal will develop a misalignment angle
relative to the optical lattice, which is crucial for its frictional properties. Our results demonstrate that, around the critical contact strength, the 2D Aubry transition brings about the occurrence of a novel phase separation with a coexistence region between pinned and free-sliding colloidal patches. The frictional rheology of the monolayer is especially interesting and heterogeneous in this two-phase region, which we also characterize by means of molecular-dynamics (MD) simulations mimicking the experimental conditions.

Our experiments were performed at $T_0 \approx 298$ K, with a suspension of micron-sized polystyrene particles interacting via a repulsive screened Coulomb potential (see Methods section in the Supplemental Material [22]). The colloids form a 2D hexagonal crystal with lattice constant $a_C$ at the bottom of the sample cell. A periodic substrate is created by interfering three partial laser beams, as sketched in Fig. 1(a). This optical landscape provides a hexagonal substrate potential, Fig. 1(b), whose amplitude $U_0$ can be tuned by the laser intensity. The laser lattice constant $a_L$ is set by the intersection angle of the laser beams and allows us to adjust the mismatch ratio $\varepsilon = a_L/a_C$. Particle positions are tracked by video microscopy with a resolution of about 50 nm [Fig. 1(b)]. A controlled driving force $F$ of the monolayer is exerted by viscous Stokes forces, which arise when the sample cell is translated horizontally relative to the (resting) interference pattern [22].

Figure 1(c) shows experimental mobilities $\mu$ of an incommensurate ($\varepsilon = 0.84$) colloidal monolayer vs driving force for different corrugation amplitudes $U_0$ in the superlubric (red and orange symbols), coexistence (green symbols), and statically pinned phase (blue and black symbols). The dashed line shows the maximum mobility ($U_0 = 0$), while the dotted line shows the minimum threshold mobility to detect sliding. The pink arrow points at the crossing of this threshold mobility, defining the value of $F_s$ for this value of $U_0$.

(d) Static friction force $F_s$ vs $U_0$ obtained from experiments (solid symbols) and simulations (open symbols); the shaded area shows the coexistence region, across which Aubry transition takes place. (e) The monolayer mobility under the action of the smallest experimentally accessible driving force $F_{\text{min}} \approx 1$ fN; the critical corrugation $U_c = 34k_BT_0$ is defined by the sharp drop in the mobility (arrow).
amplitude. To obtain system-independent quantities, $F_s$ is normalized to that of a single colloid in the same corrugation potential $F_{1s}$, and $U_0$ to the critical corrugation amplitude $U_c$, where the monolayer becomes pinned at $F_{\text{min}}$ [Fig. 1(e)]. In agreement with the predictions by Aubry, our data show the disappearance of static friction below $U_0/U_c \approx 1$. Above this transition, $F_s$ increases almost linearly and eventually saturates. The open symbols, which were obtained by numerical simulations with parameters adjusted to our experimental conditions [22], show excellent agreement with our data.

Because the Aubry transition is a structural phase transition, it must affect the monolayer microstructure. For stiff monolayers, minimization of the free energy is achieved by rotation of the lattice relative to the substrate by the Novaco angle $\theta_{\text{Nov}}$ [23–24]. Because most particles are slightly displaced from substrate minima after rotation, they become superlubric (unpinned). Contrary to very stiff monolayers, where $\theta_{\text{Nov}}$ has a sharp-defined value that depends on the mismatch ratio (for $\varepsilon = 0.84$, one obtains $\theta_{\text{Nov}} \approx 5^\circ$) [25], for deformable monolayers, the misfit angle $\theta$ locally varies across the monolayer. Such behavior is confirmed by our experiments as seen by typical particle configurations for different substrate amplitudes [Figs. 2(a)–2(c)]. Red or blue colored particles belong to superlubric domains, which are rotated by $|\theta| > \frac{1}{2} \theta_{\text{Nov}} = 2.5^\circ$, while grey particles correspond to pinned regions (see Methods section in Ref. [22]). With increasing $U_0$, the colloidal lattice becomes increasingly locally aligned with the substrate, as seen by the grey (aligned) domains that proliferate at the expense of

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**FIG. 2.** Structural response and emergence of coexistence region. (a)–(c) Configurations representative of (a) the superlubric phase, (b) the coexistence region, and (c) the pinned phase. The color scheme follows the local bond-orientation angle $\theta_i$ relative to the crystalline directions of the corrugation potential (S.M.). (d)–(f) The local-angle distribution, obtained for corrugation (d) $U_0 = 0.63U_c$ (unpinned, i.e. superlubric configuration), (e) $U_0 = 1.25U_c$ (coexistence region), and (f) $U_0 = 11.3U_c$ (statically pinned region). (g) Corrugation dependence of the fraction $f_{\text{tilt}}$ of tilted (red+blue) colloids. In the simulations the presence of hysteresis, due to slow numerical equilibration, helps identify the coexistence region, characterized by a change of slope in experiment.
tilted regions. For $U_0 = 11.3 U'_c$ [Fig. 2(c)] essentially only pinned particles are observed. Figures 2(d)–2(f) show how the misfit-angle distribution gradually changes as a function of $U_0$. Simulations suggest that the Aubry transition in 2D is of first order, which implies the coexistence of pinned and superlubric regions [26]. The structural features of the three phases are evident in the structure factor analysis reported in Figs. S2 and S3 [22]. Upon ramping $U_0$ up and down, simulations exhibit a clear hysteresis in the fraction $f_{\text{tilt}}$ of superlubric particles [Fig. 2(g)]. From the range where error bars show no overlap, the coexistence range between the pinned and unpinned particles can be estimated. Even if, unlike simulations, experimental data are sufficiently well equilibrated and do not show hysteresis, they nonetheless show clear evidence for coexistence [Fig. 2(b)].

Within the 1D FK model, a superlubric-pinned transition is structurally characterized by the displacement of all particles away from the maxima of the corrugation potential [Figs. 3(a)–3(c)]. Following the disorder parameter of Refs. [27,28], we evaluate the fraction $\Psi$ of colloids at positions where the local substrate potential is above that of the saddle points, namely, the white triangles of Fig. 3(d). This fraction should be 25% for randomly placed colloids or for $U_0 = 0$, and it decreases with increasing $U_0$. This is in agreement with our experimental and simulation data [Figs. 3(e)–3(h)]. It should be emphasized that the $U_0$ dependence of $\Psi$ is in good agreement with the corresponding $f_{\text{tilt}}$ behavior in Fig. 2. Both quantifiers support the existence of a first-order Aubry transition at $U_0/U'_c \approx 1$.

An important novelty in 2D compared to 1D is that depinning can occur inhomogeneously, nucleating at specific points in the sample. This is especially expected in the phase-coexistence region where, for a given applied force, superlubric patches tilted at the Novaco angle are likely to unpin earlier than nontilted regions. To explore such behavior, we have simulated a configuration near the right end of the coexistence region ($U_0 = 1.2 U'_c$). After applying a weak

![Graph and images](image-url)

FIG. 3. Local energetics across the Aubry transition. For increasing $U_0$, a substrate-mismatched 1D FK chain evolves from a configuration in which (a) minima and maxima regions are populated (superlubric), (b) no particles can be found sitting close to any maximum (pinning threshold), and (c) only regions around the minima are occupied (strongly pinned). (d) The 2D corrugation-potential profile (dark/light = low/high energy); the repulsive regions correspond to the area between the green (saddle-energy contour level) and the black (Wigner-Seitz cell) hexagons. (e) For the 2D colloid crystal, we show the fraction $\Psi$ of colloids in the repulsive regions as a function of $U_0$, illustrating the statistical crossover from superlubric to pinned. (f)–(h) Experimental particle positions folded within the Wigner-Seitz cell of the corrugation lattice.
force $F < F_s$, $F$ is abruptly increased to $F = 1.09 \, F_s$. The red line in Fig. 4(a) reports how the monolayer progressively depins in time. This progressive depinning is understood when examining the simulation movie (S.M.) in Ref. [22], with the local-angle labeling showing a progressive extension of the red and blue unpinned regions. Figures 4(b) and 4(c) report two snapshots of that movie, representative of the mostly pinned initial state and the mostly sliding steady state, respectively. Arrows showing individual particle displacements indicate that initial depinning occurs mainly at the interface regions between the two phases.

Our experimental approach provides a versatile way of studying the conditions under which superlubricity occurs in extended 2D contacts. In addition, we obtain previously unattainable insights into the microstructural changes occurring during the Aubry transition. For example, the observation of a first-order transition from a superlubric to a pinned state demonstrates that, in contrast to a smooth transition in 1D, as well as in an interesting model of a crystal grain boundary [29], the Aubry transition may remain sharp at finite temperatures for 2D contacts. The first-order character in our case is boosted by the local angular compliance coupled to the Novaco-McTague rotation. In a different 2D system lacking that compliance, such as a graphene flake on a crystal surface, the first-order character is likely to be weakened. In particular, for micromechanical and nanomechanical devices whose contact areas are rather free from defects, asperities, and long-range elasticity effects [30–32], this should allow for drastic variations in the frictional behavior induced by tiny changes of the mechanical load.

It is a pleasure to acknowledge discussions with Davide Mandelli. Work in Trieste was carried out under ERC Grant No. 320796 MODPHYSFRICT. The COST Action MP1303 is also gratefully acknowledged.


