Catalysts for Social Insurance: Education Subsidies vs. Real Capital Taxation

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Abstract

To analyze the optimal social insurance package, we set up a two-period life-cycle model with risky human capital investment, where the government has access to labor taxation, education subsidies and capital taxation. Social insurance is provided by redistributive labor taxation. Moreover, both education subsidies and capital taxation are used as catalyzers to facilitate social insurance by mitigating distortions from labor taxation. We derive a Ramsey-rule for the optimal combination of these two instruments. Relative to capital taxation, optimal education subsidies increase in their relative effectiveness to boost labor supply and in households' underinvestment into education, but they decrease in their relative net distortions. For their absolute levels, indirect complementarity effects, i.e., influencing the effectiveness of the other instrument, do matter. Generally, a decrease in capital taxes should go along with an increase in education subsidies.

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"Idleness and pride tax with a heavier hand than kings and parliaments. If we can get rid of the former, we may easily bear the latter."

(Benjamin Franklin, Letter on the Stamp Act, July 01, 1765)

1 Introduction

In all developed countries, the labor income tax plays an important role as revenue generator for financing public sector expenditures and as a means of income redistribution. As private insurance markets are incomplete (Sinn, 1996), labor taxation is furthermore crucial in providing social insurance against income risks due to uncertain outcomes in education and (productivity) shocks in labor markets (Eaton and Rosen, 1980). Since globalization has amplified income risks in the last years, the latter role has significantly gained importance. Moreover, we observe since the mid 1980’s that globalization has driven down both corporate and personal capital taxes by intensifying tax competition and increasing the elasticity of real savings (see, e.g., Winner, 2005). Furthermore, there is (anecdotal) evidence at least in Europe that education subsidies have decreased as well (i.e., that tuition fees increased). However, both (real) capital taxation and education subsidies are still additional policies for social insurance.

Now, this paper focuses on the insurance role of taxation and on the net efficiency costs, which are unavoidably created in the process. We derive the optimal social insurance package as combination of labor and capital taxation as well as educational policy. The new aspect will be on optimally combining the additional policies in order to foster insurance provision via boosting labor supply (i.e., to overcome the “idleness”, as Franklin put it). Analogously to catalyzers in chemical reactions, capital taxation and education subsidies facilitate providing social insurance by reducing efficiency costs, but they do not provide insurance themselves. Our findings are highly policy relevant, since we show that capital taxation and education subsidies are strategic substitutes. This calls the development described above and in particular the recent restrictive education policies in light of ongoing tax competition in question.

A big chunk of risk in labor income is due to uncertainty associated with education. Educational investment can both mitigate or aggravate the exposure to income risk.1 Thus, it is natural to bring educational choices into the picture. That leads to a dynamic set-up, where savings in real capital must enter. Since both decision margins are close substitutes (e.g., Nielsen and Sørensen, 1997), any policy which fosters (hampers) human capital investment will obviously harm (promote) real savings and vice versa. Hence, besides providing social insurance, designing an education policy and incorporating the

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1Empirical evidence that human capital investment cuts both ways with respect to exposure to risk is provided, e.g., by Palacios-Huerta (2004), Belzil and Hansen (2004), and Hartog (2005). The theoretical analysis dates back to Levhari and Weiss (1974).
The treatment of savings in real capital are some of the most important tasks of the modern welfare state.

The idea of perceiving supplementary instruments as catalyzers of social insurance via the labor income tax is – especially with respect to real capital taxation – only just developed. Important forerunners in absence of human capital investment are Jacobs and Schindler (2009) as well as Kocherlakota (2005). The former focus on linear tax instruments and point out that capital taxation mitigates labor tax distortions by intertemporal wealth and substitution effects, which increase opportunity costs of leisure. Following the ‘new dynamic public finance’ approach (see also Golosov et al., 2006), Kocherlakota shows in a non-linear taxation setting that there is a role for capital taxation, since capital taxes relax the incentive constraints for non-mimicking. Incorporating (unobservable) human capital formation, Hamilton (1987) states that positive capital taxation should overcome underinvestment in education, which is due to uninsurable risk and self-insurance, by decreasing intertemporal opportunity costs of educational investment, if (i) labor supply is exogenous and (ii) either savings are zero or absolute risk aversion is constant. His results are backed by Grochulski and Piskorski (2006), who apply non-linear tax instruments.

Turning to observable educational investment, Anderberg and Andersson (2003) state that education should be overprovided (underprovided) if it is a risk-decreasing (risk-increasing) activity. In doing so, educational policy exploits the insurance effect of human capital and it complements social insurance by income taxation. In their approach the government directly controls educational investment. Jacobs et al. (2010) make clear that the results from the former paper cannot be transferred to a decentralized setting. Individuals already exploit the insurance effect of education by self-insurance. Still, education subsidies are used for mitigating labor supply distortions by increasing the effective wage rate, but they do not provide insurance. Furthermore, the optimal level of education subsidies crucially depends on internalizing a fiscal externality, which stems from the interplay of labor taxation and over- or underinvestment into education.

To the best of our knowledge, only da Costa and Maestri (2007) and Anderberg (2009) analyze the simultaneous use of education subsidies and capital taxation. They apply a non-linear taxation setting and find a positive intertemporal wedge, indicating a role for capital taxation. However, their results differ as to whether the aggregate level of educational investment should be socially efficient. Moreover, it is generally difficult or even impossible to implement these optimal wedges through tax instruments.

Compared to these contributions, we here offer a comprehensive model allowing to derive the optimal capital taxation and optimal education subsidies simultaneously and to account for interactions between these two catalyzers. To that end, we apply a two-period life-cycle model, where ex-ante homogenous households invest in education, decide on savings and choose labor supply. In the second-period, income realizes according to a general earnings function, which depends on educational investment, labor supply.
and an idiosyncratic shock. The exposure to risk can be increasing or decreasing in human capital. In any case, second-period consumption is stochastic, and households are heterogenous ex-post. In line with the literature, we assume that insurance markets are missing. Nevertheless, the government can provide social insurance through redistributive income taxation. The policy package consists of a linear income tax accompanied by a lump-sum transfer, a proportional capital tax and linear education subsidies.

Our analysis leads to the new insights that firstly education subsidies and capital taxes differ both in the way how they boost labor supply and in the distortions they induce. The popular argument that only capital taxes should be used, because they were more effective in boosting labor supply, is as misleading as saying that only education subsidies would be the method of choice, since they were less distortive. We derive the explicit formula for the optimal education subsidy rate and the optimal capital tax rate, showing the trade-offs between their net complementarity effects on labor supply and their net distortions of educational investment and real savings respectively. Moreover, we identify “indirect complementarity effects”, which reflect offsetting interactions between the two catalyzers. In particular, the more education subsidies (capital taxation) worsen the efficiency gain of the other instrument, the less education subsidies (capital taxation) should be employed.

Secondly, by extending the model used by Hamilton (1987), we show that there is no longer a role for capital taxation in internalizing the (fiscal) effect of self-insurance by under- or overinvesting into education. Consequently, the additive property (Sandmo, 1975) holds and solely education subsidies are used to correct for inefficient educational investment, because they are the more efficient instrument to control for the education level. Only in the special case where education subsidies are not available, the Hamilton-intuition carries over. By incorporating endogenous labor supply and a general earnings function, we point out in this case that the Hamilton-result holds under much weaker conditions, but that capital taxes are used to boost labor supply, as well. Furthermore, the optimal capital tax rate can become negative, if there is severe overinvestment in education. In this case, discouraging excessive educational investment by a subsidy on capital income overcompensates its negative effects on labor supply.

Thirdly, we derive a Ramsey-type rule for the relative dependency on education subsidies compared to capital taxation. It shows that capital taxes and education subsidies are (strategic) substitutes. Thus, decreasing capital taxes (e.g., due to tax competition and globalization) should be accompanied by increasing education subsidies. This result is highly policy-relevant and should be kept in mind when discussing education-policy reforms. Fourthly, we complement results in the ‘new dynamic public finance’ literature (e.g., Anderberg, 2009). We show that the main results and the basic intuition in this strand of literature are still valid under linear tax instruments and informationally much less demanding requirements. The advantage of our setting is that the tax structure can
be directly implemented and that the driving forces behind the optimal instruments as well as their interaction can be explicitly characterized.

The remainder of the paper is structured as follows. Section 2 introduces the model and sets up the optimal tax problem. Section 3 derives the optimal social insurance package. As a benchmark case, we discuss first the optimal labor tax rate, if there are no other policies available. Then, we describe the optimal use of education subsidies and capital taxation as catalyzers and finally we analyze the optimal labor tax, when both education subsidies and capital taxation are optimally chosen. Section 5 concludes.

2 The Model

2.1 Technologies and Preferences

We analyze a two-period model, where a continuum of ex-ante identical households decide on their educational investment, consumption and second-period labor supply. We assume that individuals are endowed with an initial wealth \( \omega \) and with one unit of time in each period. We assume further that education \( e \) is a pure time investment and that there is no labor-leisure decision in the first period. Educational investment is observable and verifiable. Hence, educational costs, i.e., the forgone earnings, can be deducted against the income tax base and can be additionally taxed or subsidized by educational policy. Apart from investing in education, households can save or borrow in a perfect capital market. Savings are denoted by \( a \). The first-period budget constraint (before taxation and education subsidies) reads

\[
a = \omega + (1 - e) - c_1,
\]

where \( c_1 \) is consumption in the first period, and where we have normalized the first-period wage rate as well as the price of consumption to one.

In the second period, households supply labor \( l \) and consume their savings plus labor income. Gross labor income is represented by a general earnings function, depending on hours worked \( l \) and education \( e \):

\[
\Phi(\theta, l, e), \quad \Phi_e, \Phi_l > 0, \quad \Phi_{ee} < 0, \quad \Phi_{ll} \leq 0.
\]

\( \theta \) is an idiosyncratic shock drawn from a probability distribution \( f(\theta) \). Therefore, both income and the return to education are risky. We assume that, for any given value of \( \theta \), the marginal return to education \( \Phi_e \) is positive and decreasing. Similarly, the marginal return to labor effort \( \Phi_l \) is positive and non-increasing. Furthermore, the random variable \( \theta \) is

\footnote{Without any loss of generality we could also allow for direct resource costs of education. As long as all inputs are verifiable, this does not change the results (see also Bovenberg and Jacobs, 2003, 2005).}
assumed to have a positive effect on income: $\Phi_\theta > 0$. In the remainder of the analysis, we focus on the two cases identified in the literature (cf. Levhari and Weiss, 1974): (i) educational investment itself causes and amplifies income risks ($\Phi_{\theta e} > 0$), and (ii) educational investment hedges against income risks ($\Phi_{\theta e} < 0$). The budget constraint in the second-period (before taxation) is

$$c_2 = \Phi(\theta, l, e) + (1 + r) \cdot a,$$

where $c_2$ is consumption in the second period, and $r$ is the constant real interest rate.

Households derive utility from consumption and disutility from labor. They maximize a von Neumann-Morgenstern expected utility function. Following common practice in the optimal tax literature under risk we assume the utility function to be additively separable over consumption and labor supply (see, e.g., Cremer and Gahvari, 1995a, 1995b; Golosov et al., 2006; Diamond, 2006):

$$EU = \mathcal{E}[U(c_1, c_2, l)] = \mathcal{E}[u(c_1, c_2)] - v(l), \quad u_1, u_2, -v_1 > 0, \quad u_{11}, u_{22}, -v_{ll} \leq 0,$$

where $\mathcal{E}$ denotes the expectation operator, i.e., $\mathcal{E}[X] \equiv \int_{\Theta} X df(\theta)$, where $\Theta$ is the set of values for $\theta$. The sub-utility function of consumption is increasing and concave, whereas the disutility function of labor supply is increasing and convex. All functions are at least twice differentiable, and we assume the Inada conditions to hold.

Insurance markets to insure (idiosyncratic) income risks are imperfect and, for simplicity, we assume that they are missing. Market failure is due to moral hazard, adverse selection, and, as Sinn (1996, p. 261ff) points out, timing and contract problems. Perfect insurance contracts have to be signed before the veil of ignorance has lifted. However, this is hardly possible with respect to, e.g., human capital risks or innate abilities, where the parents would have to sign the contracts for their children or even for their children-to-be-born. Since a child would have to fulfill these obligations incontestably for all its life, this system would come close to bondage. Thus, Sinn (1996, p. 278) concludes that such insurance “cannot be provided privately unless the fundamentals of western civil law are called into question.”

Instead, the government can provide social insurance by redistributive taxation. We assume that this takes place through a linear income tax system with a marginal tax rate $t$ and a lump-sum transfer $T$, which can be seen as a negative income tax or basic income. Furthermore, educational investment is subsidized at a flat rate $s$ and it is in addition fully tax deductible. Last but not least, the return to savings is taxed at a flat

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3This assumption fulfills the requirements for the Atkinson-Stiglitz theorem to hold. Hence, any non-zero capital tax rate will be due to incomplete insurance markets and providing social insurance.

4Note that this assumption simplifies the analysis, but does only affect the level of taxation, not the optimal tax structure.
rate \( \tau \). Interest expenses on borrowing are subsidized at this rate, i.e., there is full loss off-set. Taken together, our model is similar to the set-up in Hamilton (1987). However, education can be directly subsidized or taxed in our approach, and we allow for a more general risk (and income) process, where education can either enforce or hedge against income risk.

The timing structure of the model is as follows: First, the government sets the proportional labor tax rate \( t \), the subsidy rate \( s \), the capital tax rate \( \tau \), and the lump-sum transfer \( T \). After the policies are announced, households choose educational investment \( e \), first-period consumption \( c_1 \), and labor supply \( l \) simultaneously, before risk realizes.\(^5\) After that, (income) risk realizes, incomes are earned and second-period consumption takes place. Thus, second-period consumption is stochastic, while first-period consumption, working time and education are deterministic.

### 2.2 Households

Due to perfect capital markets, a household faces an intertemporal budget constraint after income tax and education subsidies

\[
c_2 = (1 - t) \cdot \Phi(e, l, \theta) + R \cdot [\omega + (1 - t)(1 - (1 - s)e) - c_1] + T,
\]

where \( R = 1 + r \cdot (1 - \tau) \) represents the net interest factor. Subject to budget constraint (5) a household maximizes its expected utility function \( EU = \mathcal{E}[u(c_1, c_2)] - v(l) \) by choosing optimal intertemporal consumption, educational investment and second-period labor supply. Consequently, the maximization problem turns into

\[
\max_{c_1, l, e} \mathcal{E}[u(c_1, (1 - t) \cdot \Phi(e, l, \theta) + R \cdot [\omega + (1 - t)(1 - (1 - s)e) - c_1] + T)] - v(l),
\]

and the appropriate first order conditions are

\[
\begin{align*}
\mathcal{E}[u_1] - R \cdot \mathcal{E}[u_2] &= 0, \\
\mathcal{E}[u_2 \cdot \{((1 - t)\Phi_e(e, l, \theta) - R \cdot (1 - t)(1 - s))\}] &= 0, \\
\mathcal{E}[u_2 \cdot (1 - t)\Phi_l(e, l, \theta)] - v_l &= 0,
\end{align*}
\]

Equation (7) implies that for optimal intertemporal allocation of consumption the expected marginal rate of substitution meets the net interest factor, i.e., the standard Euler equation holds and we have

\[
\frac{\mathcal{E}[u_1]}{\mathcal{E}[u_2]} = R.
\]

\(^5\)It can be shown that a timing sequence, in which labor supply is chosen after uncertainty has been resolved, does not change any of the results qualitatively, cf. Cremer and Gavhari (1995a), and Anderberg and Andersson (2003).
From the first order condition for optimal educational investment \( (8) \) it follows by Steiner’s Rule that the risk-adjusted marginal return to educational investment is equal to the present value of marginal investment costs (after subsidization),

\[
(1 - \pi_e) \cdot \mathcal{E}[\Phi_e] = R \cdot (1 - s),
\]

where \( \pi_e = -\frac{\text{cov}(u_2, \Phi_e)}{\mathbb{E}[u_2^2]} \in (-1, 1) \) represents the risk premium in educational investment, measuring disutility from increased exposure to risk. \( \pi_e \) is positive, if education is risk-increasing, i.e., if \( \Phi_{\theta e} > 0 \). For instance, this holds for sector-specific human capital investment. It is negative, instead, if education serves as a hedge and provides insurance against income risks (e.g., general upper secondary education). This is the case, if \( \Phi_{\theta e} < 0 \).

As we have assumed educational investment to be observable and tax deductible, the tax system does not directly affect investment in education. However, taxation generally affects investment in education indirectly via labor supply: a tax-induced decrease in labor supply lowers the return to human capital investment as long as \( \Phi_{el} > 0 \). This is the case for all earnings functions discussed in the literature (cf. Jacobs and Bovenberg, 2008). As a result, taxation reduces the incentives for investing into education. Instead, education subsidies boost educational investment, since they reduce the marginal costs.

Missing insurance markets, however, drive a wedge between expected marginal return to education and the net investment costs, implying

\[
\mathcal{E}[\Phi_e] - R \cdot (1 - s) = \pi_e \cdot \mathcal{E}[\Phi_e] = \frac{\pi_e}{1 - \pi_e} \cdot R \cdot (1 - s) \geq 0 \quad \text{if} \quad \pi_e \geq 0.
\]

Facing uninsurable income risk, households use educational investment as self-insurance device to reduce their exposure to risk. If education is risk-increasing (risk-decreasing), households invest too less (much) in education from a social point of view, viz., the expected marginal return is higher (lower) than the marginal costs. This socially inefficient – but individually rational – investment will be the worse, the more risk-averse households are, i.e., the higher the risk premium in absolute terms would be.

Accordingly, the first order condition for labor supply \( (9) \) can be rearranged as

\[
(1 - \pi_l)(1 - t)\mathcal{E}[\Phi_l] = \frac{v_l}{\mathcal{E}[u_2]},
\]

where \( \pi_l = -\frac{\text{cov}(u_2, \Phi_l)}{\mathbb{E}[u_2^2]} \) mirrors the risk premium in labor supply. Hence, for optimal labor supply the risk-adjusted net wage rate equals the marginal rate of substitution between consumption and labor. The presence of risk acts as an additional tax on labor, if labor supply is a risk-increasing activity \( (\pi_l > 0) \), but it turns into a wage subsidy, in case higher labor supply reduces the exposure to income risk \( (\pi_l < 0) \).

Substituting optimal consumption, educational investment and labor supply in the
expected utility function, we receive the expected indirect utility function as

\[ V(T, t, s, R) = \mathcal{E}[u(\hat{c}_1, \hat{c}_2)] - v(\hat{l}), \]  

where a hat indicates the optimal values.

For later reference, we apply the Envelope theorem (Roy’s lemma) to find the derivatives of the indirect utility function as

\[ \frac{\partial V}{\partial T} = \mathcal{E}[u_2], \quad \frac{\partial V}{\partial t} = -\mathcal{E}[u_2 \cdot \{\Phi(e, l, \theta) + R \cdot (1 - (1 - s)e)\}], \]

\[ \frac{\partial V}{\partial s} = \mathcal{E}[u_2] \cdot R \cdot (1 - t) \cdot e \quad \text{and} \quad \frac{\partial V}{\partial R} = \mathcal{E}[u_2] \cdot [\omega + (1 - t)(1 - (1 - s) \cdot e) - c_1]. \]

### 2.3 Government

We assume a benevolent government with full (and credible) commitment. Hence, a time-inconsistency motive cannot appear. Without loss of generality, we abstract from an exogenous government revenue requirement. The government chooses policy instruments \( T, t, s \) and \( R \) to maximize the expected indirect utility \( V(T, t, s, R) \) of the households. The informational requirements for employing linear instruments are that only aggregate income, aggregate savings and aggregate education choices need to be verifiable to the government, i.e., taxes can be collected and subsidies can be paid in a withholding fashion (at firm level) and individual incomes need not to be observed.

By the law of large numbers, individual idiosyncratic risks cancel in the aggregate and we find that the government budget constraint is given by

\[ t \cdot [\mathcal{E}[\Phi(e, l, \theta)] + (1 + r) \cdot (1 - (1 - s) \cdot e)] + (1 + r - R) \cdot [\omega + (1 - t)(1 - (1 - s) \cdot e) - c_1] - (1 + r) \cdot s \cdot e = T \]

All tax revenue is deterministic at the aggregate level and it is used to finance the lump-sum transfer and education subsidies. We abstract from any systematic risk.\(^6\)

Taken together, the optimization problem can be displayed as:

\[ \max_{T, t, s, R} V(T, t, s, R) \quad \text{s.t. (15)} \]  

\(^6\)In case of additional systematic (aggregate) income risks, government’s tax revenue would turn risky, as well. This would require an additional insurance device in the form of public consumption for smoothing aggregate shocks over private and public consumption (see, e.g., Kaplow, 1994), but it should not affect our main findings on insuring the idiosyncratic part of risk.
Denoting the Lagrange multiplier as $\eta$, the first order conditions are represented by

\[
\frac{\partial V}{\partial T} + \eta \cdot \left\{ \Delta_e \cdot \frac{\partial e}{\partial T} + \Delta_l \cdot \frac{\partial l}{\partial T} + \Delta c_1 \cdot \frac{\partial c_1}{\partial T} - 1 \right\} = 0,
\]
(17)

\[
\frac{\partial V}{\partial t} + \eta \cdot \left\{ \Delta_e \cdot \frac{\partial e}{\partial t} + \Delta_l \cdot \frac{\partial l}{\partial t} + \Delta c_1 \cdot \frac{\partial c_1}{\partial t} + \mathcal{E} \left[ \Phi(.) \right] + R \cdot (1 - (1 - s) \cdot e) \right\} = 0,
\]
(18)

\[
\frac{\partial V}{\partial s} + \eta \cdot \left\{ \Delta_e \cdot \frac{\partial e}{\partial s} + \Delta_l \cdot \frac{\partial l}{\partial s} + \Delta c_1 \cdot \frac{\partial c_1}{\partial s} - R \cdot (1 - t) \cdot e \right\} = 0,
\]
(19)

\[
\frac{\partial V}{\partial R} + \eta \cdot \left\{ \Delta_e \cdot \frac{\partial e}{\partial R} + \Delta_l \cdot \frac{\partial l}{\partial R} + \Delta c_1 \cdot \frac{\partial c_1}{\partial R} - \omega + (1 - t)(1 - (1 - s) \cdot e) - c_1 \right\} = 0,
\]
(20)

where we have defined the (expected) tax wedges as

\[
\Delta_e = t \cdot \mathcal{E}[\Phi_e] - R \cdot (1 - s) - R \cdot s - \tau r
\]
\(= t \cdot \frac{\pi e}{1 - \pi e} \cdot R \cdot (1 - s) - R \cdot s - \tau r \),
(21)

\[
\Delta_l = t \cdot \mathcal{E}[\Phi_l],
\]
(22)

\[
\Delta c_1 = -\tau r.
\]
(23)

The tax wedges indicate the (expected) change in total tax revenue, based on behavioral responses of households, due to a marginal change in one of the tax instruments. Thereby, the second equality in equation (21) stems from applying the households’ first order condition (8) twice.

### 2.4 Decision Margins and Distortions

The task of the government is to provide social insurance (i.e., to redistribute between “winners” and “losers”). Income risk can be reduced by implementing a wage tax and granting a deterministic lump-sum transfer. However, this comes at the cost of distorting labor supply and creating a fiscal externality. The latter stems from the fact that the marginal return and the marginal costs of educational investment are not equalized due to self-insurance of households by under- or overinvesting into education. Consequently, a marginal increase of education creates a positive (negative) tax-revenue effect in case of underinvestment (overinvestment) in education (see Jacobs et al. 2010).

In order to alleviate these efficiency costs, both education subsidies and capital taxation can be applied as ‘catalyzers’ for social insurance via labor taxation. Education subsidies increase human capital investment and, thus, the effective wage rate. As a result, education subsidies alleviate labor tax distortions by increasing labor supply. However, this is paid by distorting educational investment.

Capital taxation fosters labor supply via two channels: First, it works as indirect
education subsidy by reducing the opportunity costs of human capital investment. Consequently, it encourages labor supply in the second period, but it distorts educational investment. Second, capital taxation reduces second-period consumption and boosts labor supply by increasing the marginal utility of income, viz., the opportunity costs of second-period leisure.\footnote{See Cremer and Gahvari (1995a) or Jacobs and Schindler (2009) for a detailed analysis of this effect.} However, the latter effect is paid by distorting intertemporal consumption choice.

In the following, we analyze how these three instruments can be combined optimally in order to balance the net distortions on all margins and to provide the optimal social insurance package. The main question to be answered is, how education subsidies and capital taxation can serve as catalyzers to facilitate income insurance.

## 3 The Social Insurance Package

### 3.1 Optimal Transfer Income

Following Diamond (1975), we define the expected net social marginal value of income, including the income effects on the tax base, as

\[
b \equiv \frac{\mathbb{E}[u_2]}{\eta} + \Delta_e \cdot \frac{\partial e}{\partial T} + \Delta_l \cdot \frac{\partial l}{\partial T} + \Delta_{c_1} \cdot \frac{\partial c_1}{\partial T}.
\]

Accordingly, rearranging the first order condition (17) leads to

\[
b \equiv \frac{\mathbb{E}[u_2]}{\eta} + \Delta_e \cdot \frac{\partial e}{\partial T} + \Delta_l \cdot \frac{\partial l}{\partial T} + \Delta_{c_1} \cdot \frac{\partial c_1}{\partial T} = 1. \tag{24}
\]

Hence, the optimal lump-sum transfer balances the net marginal value of income (from the society’s perspective) against its marginal revenue costs, which equal unity.

### 3.2 Labor Taxation Without Catalyzers

First, we derive as a benchmark case the optimal labor tax rate \( t \) without catalyzers, i.e., when the government can neither use education subsidies nor capital taxation. This case arises when neither educational investment nor savings are verifiable to the government. This corresponds to the set of instruments in Eaton and Rosen (1980).

Analogously to Feldstein’s distributional characteristic, we define the insurance characteristic

\[
\xi \equiv -\frac{\text{cov}(u_2, \Phi(.))}{\mathbb{E}[u_2] \cdot \mathbb{E}[\Phi(.)]} > 0 \tag{25}
\]

as the negatively normalized covariance between the marginal utility of income and income. The insurance characteristic \( \xi \) gives the marginal welfare loss of income risk and measures the government’s concern for insurance.

Moreover, we define the expected-utility compensated elasticities with respect to the labor tax rate as \( \varepsilon_{et} = \frac{\partial e}{\partial t} \cdot \frac{1}{e} \) and \( \varepsilon_{lt} = \frac{\partial l}{\partial t} \cdot \frac{1}{l} \). By applying the Slutsky equations and

\[
\begin{align*}
\varepsilon_{et} &= \frac{\partial e}{\partial t} \cdot \frac{1}{e} \\
\varepsilon_{lt} &= \frac{\partial l}{\partial t} \cdot \frac{1}{l}
\end{align*}
\]
equation (24) to eliminate the income effects and by inserting $s = \tau = 0$, the optimal labor tax rate can be derived from equation (18) as (see Appendices A and B.1)

$$\frac{t}{1-t} = \frac{\xi}{\omega_l \cdot (-\varepsilon_{lt}) - \pi_e \cdot \omega_e \cdot \varepsilon_{et}}.$$  (26)

Thereby, $\omega_l = \frac{\varepsilon_l^{[\Phi_l]}}{\varepsilon^{[\Phi]}}$ and $\omega_e = \frac{\varepsilon_e^{[\Phi_e]}}{\varepsilon^{[\Phi]}}$ are the expected earnings shares of labor and education in total earnings, respectively.

Equation (26) represents the standard trade-off between the welfare gain of providing insurance and the efficiency costs of doing so. The higher the benefits from social insurance, i.e., the higher is $\xi > 0$, the higher the optimal tax rate should be, ceteris paribus.

However, social insurance has to be paid by excess burden, in particular from distorting labor supply. We assume – as well as for all following elasticities – that all compensated elasticities maintain their signs under certainty; hence $\varepsilon_{lt} < 0$. The larger $(-\varepsilon_{lt}) > 0$ is ceteris paribus, the more labor taxation distorts labor supply and the lower the optimal tax rate should be.

Furthermore, the optimal labor tax rate depends on a fiscal externality $(\pi_e \cdot \omega_e \cdot \varepsilon_{et})$, which can be of any sign.\(^8\) Note that the labor tax elasticity of educational investment is negative, $\varepsilon_{et} < 0$, because an increase in labor taxation decreases (compensated) labor supply and therefore the utilization of human capital. In case of $\pi_e > 0$ ($\pi_e < 0$), where there is under- (over-)investment in education, a marginal decrease of educational investment decreases (increases) tax revenue. Therefore, increasing the labor tax rate causes a negative (positive) fiscal externality, calling for a lower (higher) labor tax rate.

### 3.3 Education Subsidies and Capital Taxation as Catalyzers

In case both educational investment and savings in real capital are observable and verifiable, the government can use both instruments as catalyzers for social insurance policy.

We define the expected-utility compensated elasticities with respect to the subsidy rate as $\varepsilon_{es} = \frac{\partial e}{\partial s} \frac{1-s}{e}$, $\varepsilon_{ls} = \frac{\partial l}{\partial s} \frac{1-s}{l}$, and $\varepsilon_{c1s} = \frac{\partial c}{\partial s} \frac{1-s}{c_1}$. Furthermore, the corresponding elasticities with respect to the after tax interest rate $R$ are denoted as $\varepsilon_{eR} = \frac{\partial e}{\partial R} \frac{R}{e}$, $\varepsilon_{lR} = \frac{\partial l}{\partial R} \frac{R}{l}$, and $\varepsilon_{c1R} = \frac{\partial c}{\partial R} \frac{R}{c_1}$.

The optimal education subsidies follow from combining the first order conditions (19) and (20) and applying the optimal lump-sum transfer (24) (see Appendix B.2) as

$$s = \frac{\varepsilon_{ls} - \varepsilon_{as} \cdot \frac{\varepsilon_{lR}}{\varepsilon_{aR}} \cdot \omega_l \cdot \frac{l}{\omega_e \cdot \frac{1}{1-\pi_e} + \frac{\pi_e}{1-\pi_e} \cdot \hat{t}}}{1-s}.$$  (27)

\(^8\)Though in principle the signs of some of these elasticities are ambiguous due to offsetting insurance effects, this assumption should hold under mild restrictions; see Jacobs and Schindler (2009) for a comprehensive discussion in a related setting as well as Jacobs and Bovenberg (2010) for signing elasticities in a deterministic model.

\(^9\)See Jacobs et al. (2010) for a detailed discussion of the fiscal externality.
By inserting expression (27) in equation (42), the optimal capital tax rate follows after some rearrangements as

$$\frac{\tau R}{\hat{t}} = \left[ \frac{\left( -\varepsilon eR \cdot \varepsilon eR \right) + \varepsilon eR \cdot \varepsilon eR \cdot \varepsilon es}{\varepsilon aR \cdot \varepsilon eR \cdot \varepsilon es} \right] \omega \cdot \hat{t}. \quad (28)$$

We define $\gamma_e = \frac{Re}{\varepsilon e}$ and $\gamma_{c1} = \frac{Rc1}{\varepsilon c1}$ as shares of expenditure on education and first-period consumption in total earnings, respectively. Moreover, we define the savings elasticity with respect to education subsidies as $\varepsilon_{as} = -\left( \gamma_e \cdot \varepsilon es + \gamma_{c1} \cdot \varepsilon c1s \right) < 0$, which comprises the expenditure-share weighted effects of education subsidies on educational investment and on first-period consumption. We assume that education subsidies increase first-period consumption ($\varepsilon_{c1s} > 0$). The reasoning is as follows: education subsidies increase total income by encouraging education and increasing labor supply. The resulting higher labor income increases consumption in both periods from consumption-smoothing. The savings elasticity with respect to the net interest rate is defined as $\varepsilon aR = -\left( \gamma_e \cdot \varepsilon eR + \gamma_{c1} \cdot \varepsilon c1R \right) > 0$. It is unambiguously positive, because a higher net interest rate $R$ renders both educational investment and first-period consumption less attractive.

The insurance characteristic $\xi$ does not enter either of the two optimal tax rules and both expressions hold for the optimal labor tax rate $\hat{t}$ as well as for an arbitrarily given tax rate $t > 0$. Accordingly, two straightforward results apply both to the optimal education subsidies and to the optimal capital taxation: First, neither catalyzer directly provides social insurance, since both capital tax payments and education subsidies received do not affect the variance of income, i.e., they do not vary across the states of nature. Moreover, all households are homogenous ex ante; consequently, there is no ability bias at work either (see Maldonado, 2008, and Jacobs and Bovenberg, 2008, for ability bias in a deterministic world with heterogenous households). Second, neither instrument is used if there is no social insurance. If the labor tax rate was zero, $t = 0$, the only insurance device available would be self-insurance by over- or underinvestment into education, which is optimally chosen by households. This insurance effect would be messed up by subsidizing education or taxing capital income. Furthermore, in case of $t = 0$ there would be no fiscal externality to be corrected for.

From equation (27) we find that, firstly, optimal education subsidies decrease in distortions caused, which are represented by the denominator in the first term on the right hand side. The more elastic educational investment is with respect to subsidies, $\varepsilon es > 0$, the higher the excess burden of this instrument will be. However, the availability of capital taxation allows for a mitigating complementarity effect: reducing distortions in educational investment can be traded against distorting real savings, $\frac{\varepsilon aR}{\varepsilon aR} < 0$, and this effect becomes the stronger the more the savings tax base responds to education sub-
sidies, $\varepsilon_{as} < 0$. Secondly, education subsidies increase in the marginal efficiency gains from boosting labor supply, as indicated by $\varepsilon_{ls} > 0$ in the numerator of the first term on the right hand side. Due to the complementarity between labor supply and education, education subsidies foster labor supply and counteract the negative incentive effects of labor taxation (see Bovenberg and Jacobs, 2005, Jacobs and Bovenberg, 2008). Thirdly, education subsidies interfere with the complementarity effect of capital taxation on labor supply. Capital taxation also alleviates distortions in labor supply, both via fostering education (Jacobs and Bovenberg, 2010) and via intertemporal consumption effects (Jacobs and Schindler, 2009), but this efficiency gain has to be traded-off against (downwards) distortions in savings. See $\varepsilon_{{alR}}^{aR} < 0$. Since education subsidies distort real savings downwards as well, they worsen the aforementioned trade-off, i.e., applying capital taxes becomes more costly. Hence, education subsidies make the capital tax a less effective instrument to boost labor supply. The stronger this interference ($\varepsilon_{as} \cdot \varepsilon_{{alR}}^{aR} > 0$) is, the lower education subsidies should be. They might ceteris paribus even turn negative in order to boost the capital-tax effect. In the following, we will call this interference effect “indirect complementarity effect”.

Fourthly, we see from equations (27) and (28) that the additive property of internalizing externalities in an optimal-tax setting (Sandmo, 1975) holds, if sufficient instruments are available. Contrary to mitigating labor supply distortions, the externality is corrected by relying on education subsidies only and in an additive manner. This is represented by $\frac{\pi_e}{1-\pi_e}$, the second summand on the right hand side of (27). Depending on the sign and the magnitude of the externality, education subsidies can also turn negative. The risk premium $\pi_e$ does not explicitly enter the formula for the optimal capital tax rate. Accordingly, when education subsidies are optimally chosen, inefficient educational investment does not affect capital taxation directly. The reason is that directly relying on the price of the “commodity”, which causes the externality, is more efficient (see Sandmo, 1975, pp. 92, 95). In our case, this commodity is education and its relevant price is directly linked with education subsidies.

Turning to the optimal capital taxation as given by equation (28), we find that, firstly, the capital tax rate decreases in distortions caused in compensated savings, $\varepsilon_{{aR}} > 0$. The more elastic savings are with respect to the interest rate, the higher are the efficiency losses from capital taxation. However, education subsidies can moderate distortions in savings, traded against distorting educational investment ($\varepsilon_{{as}}^{es} < 0$). This trade-off is the more important, the more a higher interest rate decreases educational investment ($\varepsilon_{{eR}} < 0$). Hence, this complementarity effect works in favor of higher capital taxes. Secondly, capital taxation improves efficiency by fostering labor supply via two channels: (i) By reducing second-period consumption, capital taxation increases the marginal utility of income and thus the opportunity costs of leisure. Consequently, capital taxation ceteris paribus boosts labor supply in the second period (cf. Jacobs and Schindler, 2009). (ii)
Capital taxation encourages human capital investment. Therefore, it fosters labor supply by increasing the opportunity costs of leisure on this account, as well. Consequently, capital taxation mitigates labor supply distortions. This is represented by the first term in the numerator, \(-\varepsilon_{IR} > 0\). Thirdly, there is an “indirect complementarity effect” at work. Education subsidies boost labor supply, but distort educational investment, see the discussion of equation (27). This trade-off is the more beneficial, the higher \(\frac{\varepsilon_{ls}}{\varepsilon_{es}} > 0\) is. The more a higher interest rate decreases educational investment \((\varepsilon_{eR} < 0)\), the more the aforementioned trade-off is improved and the lower should the capital tax be, ceteris paribus.

Taken together the second and the third aspect, the optimal capital tax can also be negative, contrary to models without endogenous educational investment (Cremer and Galvari, 1995a,b; Jacobs and Schindler, 2009). Capital taxation will be equal to zero in the special case, where its complementarity effect on labor supply \(\varepsilon_{IR}\) exactly cancels against deteriorating the complementarity effect of education subsidies on labor supply, implying \(\frac{\varepsilon_{IR}}{\varepsilon_{eR}} = \frac{\varepsilon_{ls}}{\varepsilon_{es}}\). If so, both instruments are, per “unit” of distortion in educational investment, equally effective in boosting labor supply, and capital taxation becomes redundant, since it additionally distorts intertemporal consumption. Generally, mitigation by capital taxation is the less important the more labor supply distortions are mitigated via education subsidies.

We summarize

**Proposition 1.** *If both savings and educational investment are verifiable, both capital taxation and education subsidies are used for mitigating labor supply distortions, but they do not provide any direct insurance. Both instruments increase in their complementarity effect on labor and decrease in induced net distortions and in harming the complementarity effect of the other instrument. The additive property for externalities holds and only education subsidies are used to internalize the external effect of missing insurance markets.*

Compared to models relying only on education subsidies (cf. Jacobs et al., 2009), the availability of capital taxation has significant effects. The intuition can be briefly summarized as follows: first, capital taxation is another way to mitigate distortions in labor supply by indirectly subsidizing educational investment. Second, there is a stand-alone effect of capital taxation on labor supply via intertemporal wealth effects (cf. Jacobs and Schindler, 2009). Therefore, capital taxation has an additional complementarity effect working independently of education.\(^{10}\) Still, both education subsidies and capital taxation are used. Education subsidies are less distortive in the sense that they distort only educational investment, but they affect labor supply only by complementarity between education and labor, and they are costly in the sense that the government has to col-

\(^{10}\)Without having shown this explicitly, this intertemporal mechanism is also relevant in extensions of models with centrally decided educational investment (e.g., Anderberg and Andersson, 2003).
lect tax revenue to finance subsidies. On the other hand, capital taxes not only distort educational investment, but also intertemporal consumption.

Consequently, extending and generalizing the modeling by Hamilton (1987) preserve the use of capital taxation, but its role fundamentally changes. In particular, capital taxation is no longer required for internalizing the fiscal externality, but only used to alleviate tax distortion in labor supply.

From rearranging and dividing equation (27) by equation (28), we obtain a Ramsey-type rule for the simultaneous use of education subsidies and capital taxation

\[
\frac{s}{1-s} = \frac{\varepsilon_{aR} - \varepsilon_{eR} \cdot \frac{\varepsilon_{as}}{\varepsilon_{ls}} \cdot \varepsilon_{ls} \cdot (1 - \pi_e)}{\varepsilon_{es} - \varepsilon_{ls} \cdot \frac{\varepsilon_{eR}}{\varepsilon_{R}}} \cdot \omega_e \cdot (1 - \pi_e) + \frac{\varepsilon_{aR} - \varepsilon_{eR} \cdot \frac{\varepsilon_{as}}{\varepsilon_{ls}}}{\varepsilon_{ls} \cdot \varepsilon_{es} \cdot \varepsilon_{eR} \varepsilon_{lR} \varepsilon_{es}} \cdot \frac{\pi_e}{1 - \pi_e}. \tag{29}
\]

The second term on the right hand side of equation (29) mirrors the effect of the fiscal externality. As implied by the additive property, the relative reliance on education subsidies ceteris paribus increases (decreases) in the magnitude of the fiscal externality \(\pi_e\) in case of underinvestment \(\pi_e > 0\) (overinvestment \(\pi_e < 0\)). The externality matters ceteris paribus the more, the higher the net distortions of capital taxation are \((\varepsilon_{aR} - \varepsilon_{eR} \cdot \frac{\varepsilon_{as}}{\varepsilon_{ls}} > 0)\), i.e., the more costly capital taxation is. These net distortions are positive from the second order conditions of the governmental optimization problem. The externality matters ceteris paribus the less, the more relevant labor supply is (viz., the larger is the share \(\omega_l\)) and the better capital taxation can alleviate labor supply distortions (i.e., the higher is \((-\varepsilon_{lR} + \varepsilon_{eR} \cdot \frac{\varepsilon_{ls}}{\varepsilon_{es}})\).

The first term on the right hand side encompasses two effects: on the one hand there is the standard distortion effect. The more net distortions capital taxation causes in savings relative to risk-adjusted, income-weighted net distortions in educational investment by education subsidies, i.e., the higher is \(\frac{\varepsilon_{aR} - \varepsilon_{eR} \cdot \frac{\varepsilon_{as}}{\varepsilon_{ls}}}{\varepsilon_{es} - \varepsilon_{ls} \cdot \frac{\varepsilon_{eR}}{\varepsilon_{R}}} \omega_e (1 - \pi_e)\), the more expensive capital taxation is in terms of welfare costs. Hence, the more education subsidies will ceteris paribus be used compared to capital taxation. Note that the “indirect complementarity effects”, discussed in equations (27) and (28), cancel, but that there are alleviating complementarity effects working via labor supply \((\varepsilon_{lR} \cdot \frac{\varepsilon_{as}}{\varepsilon_{ls}} > 0)\) and \(\varepsilon_{ls} \cdot \frac{\varepsilon_{eR}}{\varepsilon_{lR}} > 0\), respectively) at play, now. On the other hand, contrary to a standard Ramsey rule, the instruments differ in their beneficial effects. Thus, education subsidies are ceteris paribus also the more preferable to capital taxation, the better the former boost labor supply than the latter does, i.e., the higher is \(\frac{\varepsilon_{ls}}{(-\varepsilon_{lR})} > 0\).

Taken together, equation (29) indicates that education subsidies and capital taxes are (strategic) substitutes (i.e., if one instrument increases, the other one should optimally decrease). This substitutability establishes a policy-relevant linkage between educational policy and competition in personal tax rates on real capital. Winner (2005) provides strong evidence that there is tax competition going on since the mid-eighties by showing
a shift from taxing capital to taxing labor. This shift in tax burdens is not only due to
corporate tax competition, but also due to a decrease in personal capital income taxes,
as can be observed in all OECD countries. If fiercer ‘tax competition’ is interpreted as
globalization, which ceteris paribus raises the elasticity of savings due to a larger mobility
of capital, i.e., as an increase in $\varepsilon_{aR}$, we find from equation (28) that the optimal capital
tax decreases, because it becomes more costly, now. As can be seen from the Ramsey-
equation (29), education subsidies should be increased relative to capital taxation, - at
least as long as there is underinvestment $\pi_e > 0$.

The effect on the absolute level of optimal education subsidies implied by equation (27)
is, however, ambiguous. On the one hand, education subsidies are less necessary to reduce
capital-tax induced distortions in education by decreasing savings ($\varepsilon_{as} \cdot \frac{\varepsilon_{eR}}{\varepsilon_{aR}} > 0$). This
ceteris paribus decreases subsidies. On the other hand, it becomes less important that
education subsidies hamper the complementarity effect of capital taxation ($\varepsilon_{as} \cdot \frac{\varepsilon_{eR}}{\varepsilon_{aR}} > 0$),
since the latter is less effective. This ceteris paribus increases education subsidies. As
long as mitigating labor supply distortions has more weight than mitigating distortions in
educational investment, education subsidies increase absolutely, as well. Consequently,
under these conditions, capital tax competition should be accompanied by increasing
direct subsidies on education. We conclude

**Corollary 1.** Capital taxation and education subsidies tend to be (strategic) substitutes
as long as reducing labor supply distortions matters. Then, a lower capital tax rate due
to capital-tax competition should be accompanied by higher (direct) education subsidies.

### 3.4 Non-observable Educational Investment

Two relevant special cases can be analyzed. For the first one, where capital taxation is
not available, we refer to Jacobs et al. (2010). In this section, we analyze the other polar
case, where the government cannot observe educational investment. Hence, education
subsidies are not available. This setting allows to specify the results in Hamilton (1987).
The optimal capital tax rate in absence of education subsidies follows from setting $s = 0$
in equation (42) in Appendix B.2 as

$$\frac{\tau^*}{R} = -\left(\omega_l \cdot \frac{\varepsilon_{IR}}{\varepsilon_{aR}} + \pi_e \cdot \omega_e \cdot \frac{\varepsilon_{eR}}{\varepsilon_{aR}}\right) \cdot \dot{t},$$  
(30)

Again, equation (30) balances the marginal efficiency gains against the marginal excess
burden of capital taxation. However, without education subsidies, capital taxation has
to correct the fiscal externality as well. Hamilton (1987) assumes multiplicative risk,
unambiguously implying underinvestment into education. He argues that capital taxation
should be used to correct this inefficient educational investment, and he shows that
the optimal capital tax is positive, in case (i) labor supply is inelastic and (ii) either
equilibrium savings are zero or there is constant absolute risk aversion. Our approach shows that these very strong assumptions can be relaxed, and it extends the Hamilton-analysis by deriving a closed-form solution for the optimal capital tax.\footnote{Note that the capital tax rate $\tau$ also enters the elasticities on the right hand side. As usual in Public Finance, it still highlights in detail the trade-offs determining the optimal tax rate.}

Equation (30) confirms that capital taxation is increasing in the magnitude of the fiscal externality in case of underinvestment (i.e., $\pi_e > 0$). In other words, the more education is distorted downwards by uninsurable income risk, the stronger is the need for capital taxation in order to encourage education. Furthermore, the more effective capital taxation is in fostering education ($\varepsilon_{eR} < 0$), the higher its tax rate should be. Contrary to Hamilton (1987), however, the optimal capital tax rate can also turn negative, in case educational investment is a risk-reducing activity (i.e., if there is overinvestment and $\pi_e < 0$) and if the fiscal externality effect dominates the complementarity effect in labor supply, which is described in the following paragraph. In this case, interest income should be subsidized to discourage excessive overinvestment into education.

As we allow for endogenous labor supply, there is a second effect at play. Capital taxation boosts labor supply and moderates distortions from social insurance by fostering educational investment and decreasing second-period consumption, see the previous subsection. Hence, the optimal capital tax rate also increases in the complementarity between capital taxation and labor supply ($\varepsilon_{lR} < 0$).

All these beneficial effects are traded off against distortions in real savings ($\varepsilon_{aR} > 0$). A higher net interest rate increases the (intertemporal) opportunity costs of human capital investment ($\varepsilon_{eR} < 0$) and it increases the price of first-period consumption ($\varepsilon_{c1R} < 0$). Consequently, savings are increased by a higher net interest rate. These distortions decrease the optimal capital taxation.

**Proposition 2.** If education subsidies are not available, capital taxation is used for boosting endogenous labor supply and for internalizing the fiscal effect from under- or overinvestment into education. Depending on the risk properties of education ($\pi_e \gtrless 0$) and the magnitude of the fiscal externality, the optimal capital tax rate can be negative as well.

Grochulski and Piskorski (2006) show that the unobservability of educational investment makes incentive constraints more severe and that it leads to a larger wedge on real capital investment. The latter is implemented by a higher volatility of marginal capital tax rates. In our linear-taxation model, the optimal capital tax rate tends also to be higher in the absence of education subsidies, but only in case of underinvestment. It is because capital taxation is the only instrument to alleviate labor supply distortions and to internalize the fiscal externality. However, if education is risk-decreasing, capital taxation will be decreased ceteris paribus to fight against the effect of overinvestment in human capital.
3.5 Optimal Labor Tax Cum Catalyzers

Substituting equations (27) and (28) into equation (36) in the appendix finally leads to the optimal labor tax expression, where both education subsidies and capital taxation are optimally chosen:

\[
\xi = \frac{i}{1 - \ell} \cdot \omega_l \left( (-e_{it}) + e_{et} \left[ \frac{\varepsilon_{ls} - \varepsilon_{as} \cdot \varepsilon_{at}}{\varepsilon_{es} - \varepsilon_{as} \cdot \varepsilon_{aR}} \right] - e_{at} \left[ \frac{(-e_{tR}) + e_{aR} \cdot \varepsilon_{at}}{\varepsilon_{aR} - \varepsilon_{at} \cdot \varepsilon_{es}} \right] \right). \tag{31}
\]

The optimal labor tax rate increases in the welfare gain \(\xi\) from reducing income risk, but it decreases in the tax elasticity of labor supply \((\varepsilon_{lt})\). The labor supply distortions are, however, the more alleviated, the more labor taxation boosts the net complementarity effect of education subsidies by decreasing subsidy-induced distortions in education (i.e., the larger \(\varepsilon_{et} < 0\) is in absolute value). This is called the “s-effect” in equation (31). The same holds true for fostering the net complementarity effect of capital taxation by reducing capital-tax-induced distortions in savings (viz., by having a larger \(\varepsilon_{at} > 0\)). The latter is named the “\(\tau\)-effect”. These complementarity effects ceteris paribus increase the labor tax rate, allowing for a better social insurance.

As known from Jacobs et al. (2010), the fiscal externality ceases to enter the optimal labor tax formula. Thus, with optimal education subsidies, inefficient educational investment does not directly affect the optimal labor taxation any more. Compared to Jacobs et al. (2010), the availability of capital taxation increases the likelihood of better social insurance in equation (31), relative to the case without catalyzers in (26).

Our analysis provides a complement to the analysis of optimal non-linear taxation in the ‘new dynamic public finance’ literature (see Golosov et al., 2006, Diamond, 2006 for a survey). If only real savings are observable, Kocherlakota (2005) and Grochuksi and Piskorski (2006) point out that capital should bear a positive wedge for relaxing incentive constraints. For the case of verifiable educational investment, Anderberg (2009) and da Costa and Maestri (2007) show that education should bear a wedge as well, i.e., that both education subsidies and capital taxation are optimally used in order to provide social insurance efficiently.

Our approach confirms their results for the informationally less demanding case of linear tax instruments. The downside of linear taxation is that the tax structure is less flexible, the upside is, however, that the government only has to verify aggregate labor income, aggregate savings and aggregate investment into education. Our analysis sheds light on the driving forces and the main intuition behind optimally positive intertemporal and educational wedges for relaxing incentive constraints (namely increasing opportunity costs of leisure). In addition, we point out that, under linear tax instruments, the optimal
capital tax rate can become negative, if it severely interferes with boosting labor supply by education subsidies. To the best of our knowledge, this result is new to the existing literature.

Another advantage of linear instruments is that they are directly implementable. The reason is that successful (i.e., high-ability) agents cannot profit from mimicking unsuccessful (i.e., low-ability) agents. We derive explicit formulas for the optimal education subsidies and the optimal capital tax rate. Instead, for non-linear taxation in vein of ‘new dynamic public finance’, implementing the optimal intertemporal wedges is difficult and needs additional requirements (e.g., special assumptions about the distribution of shocks and record keeping as in Golosov and Tsyvinski, 2006). Implementing optimal educational wedges is, except for very special cases, even impossible (see Anderberg, 2009).

4 Conclusions

This paper examined the optimal social insurance package in an intertemporal model. Whilst income risk is only insured by labor taxation, both education subsidies and capital taxation, if available, serve as catalyzers for social insurance by mitigating labor supply distortions. Optimal education subsidies increase in their complementarity effect on labor supply via enhancing education, but they decrease in induced net distortions in educational investment. The optimal capital tax also increases in its complementarity effect, which boosts labor supply both by fostering education and by intertemporal wealth effects. It decreases in its distortions in real savings. Both instruments decrease in interfering with the complementarity effect of the other instrument. Since education subsidies and capital taxation differ both in their benefits and in their distortions caused, both instruments are, generally, used and their net marginal dead weight losses are balanced against each other.

Our results show that capital taxation should optimally be used under less restrictive assumptions than examined in Hamilton (1987). In case educational investment is not observable, capital taxation is used both for mitigating labor supply distortions and for internalizing a fiscal externality, which results from self-insurance of households by over- or underinvesting into education. If educational investment is verifiable, it follows from our analysis that capital taxation is not used anymore for internalization of the fiscal externality and that the additive property holds (see Sandmo, 1975). This is because education subsidies are the more preferable direct instrument. Nevertheless, capital taxation still plays a role in such a generalized Hamilton-model: it is applied for boosting labor supply. Furthermore, our analysis of linear taxes complements the ‘new dynamic public finance’ literature. We derive closed form solutions for optimal tax rates, which are directly implementable.
Our results have a clear policy implication: if tax competition decreases personal capital tax rates, education subsidies should rather increase. In Europe, (personal) capital taxes are indeed decreasing, but education subsidies are decreased as well. Based on our analysis, this policy should be questioned, if the aim shall be to foster labor supply and to overcome labor market distortions from providing social insurance.

A Appendix: Risk-adjusted Slutsky equations

For deriving the risk-adjusted Slutsky equations (see also Cremer and Gahvari, 1995a), we define the expenditure function \( X(t, s, R, V) \) as the minimum level of non-labor income \( T \) required to attain the expected indirect utility \( V \). \( X(.) \) can be obtained from setting \( X(t, s, R, V) \equiv T \) for the optimal level of indirect utility \( V \) as given in equation (14). Consequently, the compensated demand functions are defined as

\[
c^c_i(t, s, R, V) \equiv c_i(t, s, R, X(t, s, R, V)),
\]

where the superscript \( c \) denotes a compensated change. By totally differentiating the compensated demand functions for given \( V \) and using Shephard’s lemma we obtain the following risk-adjusted Slutsky equations with respect to the tax rate \( t \)

\[
\frac{\partial e}{\partial t} = \frac{\partial e^c}{\partial t} - ((1 - \xi)E[\Phi] + R \cdot (1 - (1 - s)e)) \frac{\partial e}{\partial T}.
\]

\[
\frac{\partial l}{\partial t} = \frac{\partial l^c}{\partial t} - ((1 - \xi)E[\Phi] + R \cdot (1 - (1 - s)e)) \frac{\partial l}{\partial T}.
\]

\[
\frac{\partial c^1_i}{\partial t} = \frac{\partial c^c_i}{\partial t} - ((1 - \xi)E[\Phi] + R \cdot (1 - (1 - s)e)) \frac{\partial c^1_i}{\partial T}.
\]

The Slutsky equations with respect to changes in the subsidy rate \( s \) are

\[
\frac{\partial e}{\partial s} = \frac{\partial e^c}{\partial s} + R(1 - t)e \frac{\partial e}{\partial T}.
\]

\[
\frac{\partial l}{\partial s} = \frac{\partial l^c}{\partial s} + R(1 - t)e \frac{\partial l}{\partial T}.
\]

\[
\frac{\partial a}{\partial s} = \frac{\partial a^c}{\partial s} + R(1 - t)e \frac{\partial a}{\partial T}.
\]

and the ones with respect to variations in the net (after tax) interest rate \( R \) are

\[
\frac{\partial e}{\partial R} = \frac{\partial e^c}{\partial R} + (\omega + (1 - t)(1 - (1 - s) \cdot e) - c_1) \frac{\partial e}{\partial T}.
\]

\[
\frac{\partial l}{\partial R} = \frac{\partial l^c}{\partial R} + (\omega + (1 - t)(1 - (1 - s) \cdot e) - c_1) \frac{\partial l}{\partial T}.
\]

\[
\frac{\partial c^1_i}{\partial R} = \frac{\partial c^c_i}{\partial R} + (\omega + (1 - t)(1 - (1 - s) \cdot e) - c_1) \frac{\partial c^1_i}{\partial T}.
\]
B Appendix: Deriving Optimal Tax Rules

B.1 Optimal Income Taxation

From Roy’s lemma, equation (18) and the Slutsky equations (see Appendix A), we find

\[- [\mathcal{E}[\Phi(.)](1 - \xi) + R \cdot (1 - (1 - s) \cdot e)] \cdot \left\{ \frac{\mathcal{E}[u_2]}{\eta} + \Delta_e \cdot \frac{\partial e}{\partial T} + \Delta_l \cdot \frac{\partial l}{\partial T} + \Delta_c_1 \cdot \frac{\partial c_1}{\partial T} \right\}
\]

\[+ \mathcal{E}[\Phi(.)] + R \cdot (1 - (1 - s) \cdot e) + \Delta_e \cdot \frac{\partial e}{\partial t} + \Delta_l \cdot \frac{\partial l}{\partial t} + \Delta_c_1 \cdot \frac{\partial c_1}{\partial t} = 0,\]

where we defined the insurance characteristic

\[\xi = - \frac{\text{cov}(u_2, \Phi(.))}{\mathcal{E}[u_2] \cdot \mathcal{E}[\Phi(.)]} > 0.\] (34)

Using \( b = 1 \) from equation (24) and rearranging (33) result in

\[\xi = - \frac{\Delta_e}{\mathcal{E}[\Phi(.)]} \cdot \frac{\partial e}{\partial t} - \frac{\Delta_l}{\mathcal{E}[\Phi(.)]} \cdot \frac{\partial l}{\partial t} - \frac{\Delta_c_1}{\mathcal{E}[\Phi(.)]} \cdot \frac{\partial c_1}{\partial t}.\] (35)

Defining the expected-utility compensated elasticities with respect to the tax rate as

\[\varepsilon_{et} = \frac{\partial e}{\partial t} \cdot s_{et}, \quad \varepsilon_{lt} = \frac{\partial l}{\partial t} \cdot s_{lt}, \quad \varepsilon_{c_1 t} = \frac{\partial c_1}{\partial t} \cdot s_{c_1 t},\]

inserting the definitions of the tax wedges (21) to (23) and collecting terms, we end up with

\[\xi = - \left( \omega_l \cdot \varepsilon_{lt} + \pi_e \cdot \omega_e \cdot \varepsilon_{et} + \frac{s}{1 - s} \cdot \frac{1 - \pi_e}{1 - t} \cdot \omega_e \cdot \varepsilon_{et} - \frac{\tau r}{R} \right) \cdot \varepsilon_{at}.\] (36)

Thereby \( \omega_l = \frac{\mathcal{E}[\Phi_l]}{\mathcal{E}[\Phi]} \) and \( \omega_e = \frac{\mathcal{E}[\Phi_e c]}{\mathcal{E}[\Phi]} \) are the expected shares of labor and education in total earnings respectively. Defining \( \gamma_e = \frac{R_e}{\mathcal{E}[\Phi]} \) and \( \gamma_{c_1} = \frac{R_{c_1}}{\mathcal{E}[\Phi]} \) as shares of expenditure on education and first-period consumption in total earnings respectively allows us to define \( \varepsilon_{at} = - (\gamma_e \cdot \varepsilon_{et} + \gamma_{c_1} \cdot \varepsilon_{c_1 t}) \) as the compensated elasticity of savings with respect to the labor tax rate \( t \). Setting \( s = \tau = 0 \) leads to equation (26) in the text.

B.2 Optimal Education Subsidies and Optimal Capital Taxation

Rearranging (19), substituting Roy’s lemma and separating income and substitution effects deliver

\[R \cdot (1 - t) \cdot e \cdot \left\{ \frac{\mathcal{E}[u_2]}{\eta} + \Delta_e \cdot \frac{\partial e}{\partial T} + \Delta_l \cdot \frac{\partial l}{\partial T} + \Delta_c_1 \cdot \frac{\partial c_1}{\partial T} - 1 \right\} + \Delta e \cdot \frac{\partial e}{\partial s} + \Delta l \cdot \frac{\partial l}{\partial s} + \Delta c_1 \cdot \frac{\partial c_1}{\partial s} = 0.\] (37)
Dividing equation (37) by \(\mathcal{E}[\Phi(.)]\) and applying equation (24) lead to

\[
\frac{\Delta e}{\mathcal{E}[\Phi(.)]} \cdot \frac{\partial e^c}{\partial s} + \frac{\Delta l}{\mathcal{E}[\Phi(.)]} \cdot \frac{\partial l^c}{\partial s} + \frac{\Delta c_1}{\mathcal{E}[\Phi(.)]} \cdot \frac{\partial c^c_1}{\partial s} = 0. \tag{38}
\]

Defining the expected-utility compensated elasticities with respect to the subsidy rate \(s\) as

\[
\varepsilon_{es} = \frac{\partial e^c}{\partial s} \cdot \frac{1-s}{e}, \quad \varepsilon_{ls} = \frac{\partial l^c}{\partial s} \cdot \frac{1-s}{l} \quad \text{and} \quad \varepsilon_{c_1 s} = \frac{\partial c^c_1}{\partial s} \cdot \frac{1-s}{c_1},
\]

we receive after inserting the tax wedges (21) to (23) and collecting terms

\[
\frac{s}{1-s} \cdot (1 - \pi_e) \cdot \omega_e \cdot \varepsilon_{es} = t \cdot (\omega_l \cdot \varepsilon_{ls} + \pi_e \cdot \omega_e \cdot \varepsilon_{es}) + \frac{\tau R}{R} \cdot \varepsilon_{as}. \tag{39}
\]

Thereby, the savings elasticity \(\varepsilon_{as} = - (\gamma_e \cdot \varepsilon_{es} + \gamma_{c_1} \cdot \varepsilon_{c_1 s}) < 0\) comprises the expenditure-share weighted effects of education subsidies on educational investment and on first-period consumption. Using the same techniques for optimal capital taxation, the first order condition (20) can be reformulated as

\[
[\omega + (1-t) (1 - (1-s) \cdot e) - c_1] \cdot \left\{ 1 - \left( \frac{\mathcal{E}[u_2]}{\eta} + \Delta e \cdot \frac{\partial e}{\partial T} + \Delta l \cdot \frac{\partial l}{\partial T} + \Delta c_1 \cdot \frac{\partial c_1}{\partial T} \right) \right\} = 0. \tag{40}
\]

Dividing both sides by \(\mathcal{E}[\Phi(.)]\) and utilizing the optimal lump-sum transfer (24), we receive

\[
\frac{\Delta e}{\mathcal{E}[\Phi(.)]} \cdot \frac{\partial e^c}{\partial R} + \frac{\Delta l}{\mathcal{E}[\Phi(.)]} \cdot \frac{\partial l^c}{\partial R} + \frac{\Delta c_1}{\mathcal{E}[\Phi(.)]} \cdot \frac{\partial c^c_1}{\partial R} = 0. \tag{41}
\]

By defining the corresponding elasticities with respect to a change in the after tax interest rate \(R\) as

\[
\varepsilon_{eR} = \frac{\partial e^c}{\partial R} \cdot R, \quad \varepsilon_{lR} = \frac{\partial l^c}{\partial R} \cdot R \quad \text{and} \quad \varepsilon_{c_1 R} = \frac{\partial c^c_1}{\partial R} \cdot \frac{R}{c_1},
\]

as well as taking the tax wedges (21) to (23) into account, we end up with

\[
\frac{\tau R}{R} \cdot \varepsilon_{aR} = -t \cdot (\omega_l \cdot \varepsilon_{lR} + \pi_e \cdot \omega_e \cdot \varepsilon_{eR}) + \frac{s}{1-s} \cdot (1 - \pi_e) \cdot \omega_e \cdot \varepsilon_{eR}, \tag{42}
\]

The savings elasticity is again defined as \(\varepsilon_{aR} = - (\gamma_e \cdot \varepsilon_{eR} + \gamma_{c_1} \cdot \varepsilon_{c_1 R}) > 0\). It is unambiguously positive, because a higher net interest rate \(R\) renders both educational investment and first-period consumption less attractive. Inserting equation (42) for \(\frac{\tau R}{R}\) in equation (39) and collecting terms, we arrive at equation (27) in the text.

**References**


